Effective Methods for Prediction and Visualization of Contaminated Soil Volumes in 3D with GIS

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*Effektiva metoder för att förutsäga och visualisera förorenade jordvolymer i 3D med hjälp av GIS*

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Master thesis, 30 credits, in Geomatics

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Preface

This thesis has been written in cooperation with Sweco in Linköping. I would like to thank my supervisor at Sweco, Patrik Andersson, for his time and valuable support. I would also like to thank everyone else at the office for answering questions and their company. I would like to thank my academic supervisor Helena Eriksson for her support throughout the project. Finally, I want to say a big thank to my family for their great support. This project would not have been possible to do without you.

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*Sofia Sjögren*
I. Abstract

Geographical Information Systems (GISs) have shown to be of great help in the work at contaminated sites. Today there is an increase in the development of 3D modeling in many fields. However, to combine the advantage working with spatial data in a GIS and 3D modeling for subsurface soil data is limited. In this study, the possibilities of interpolating volumes of soil contamination in 3D were investigated. The study is focused on the ability of integrating 3D modeling with the GIS-environment in projects for contaminated land. Three different interpolation techniques were evaluated; Kriging-, Inverse Distance Weighting (IDW)-, and Nearest Neighbor interpolation. The data used in the study originates from a contamination project at a former gasworks site in Norrköping, Sweden. The data was sampled by the consultancy company Sweco. Three major contaminants of different characteristics were evaluated for potential of volume interpolation in 3D (lead, benzene, and polycyclic aromatic hydrocarbons (PAHs)). The study also aimed at determining if the interpolation method with greatest potential differs in relation to contaminant type. Prior the 3D interpolation possible GIS software and other methods for 3D interpolation were identified. Geostatistical analyses were performed where the optimized parameters for the interpolations were determined. In the geostatistical analyses a spatial dependence at short distances was found for all contaminants in the vertical direction (1-2 m) but not in the horizontal plane. The lack of spatial dependence in the horizontal plane indicates an effect of the coarse sampling density (about 10 m compared to 0.5 m for the vertical direction). The distribution patterns of the three contaminants are expected. Lead and PAH are both distributed differently depending on the soil material. Benzene seems to be distributed equally in all material and was interpolated with the same parameters in all soil types. All contaminants show greatest potential for volume interpolation with Kriging and secondly IDW. The least accurate method was Nearest Neighbor. The optimized parameters for interpolation are similar for lead and PAH but differed for benzene. That reflects their difference in grade of mobility. Benzene shows the most accurate 3D volume interpolation while PAH the least. It is suggested that an effective volume interpolation of pollutants in 3D must combine regular GISs with software handling 3D volumes, or a development of the GIS-software is necessary.

Keywords: 3D interpolation, 3D volumes, GIS, geostatistics, Kriging, remediation, soil contamination
II. Sammanfattning


Nyckelord: 3D-interpolering, 3D-volymer, geostatistik, GIS, Kriging, markföroreningar, sanering
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1. Introduction

A major problem and important subject in the environmental protection field is the issue concerning remediation of contaminated land. Today large areas around Europe are exposed to contamination of soil and groundwater (Panagos et al., 2013). The contamination can be harmful when spread to the ground, ecosystem or humans (Fent, 2004). The problem with contaminated land is partly inherited from the past when the industrialization was intensive. Industrial activities such as sawmills and gasworks utilized toxic substances. Contaminated materials were used to level out or expand industry sites that today are abandoned. The remnants from the industrial activities have led to contamination of the ground (Panagos et al., 2013). Today urbanization and new developments demand for reusing the land for new purposes. Prior to exploitation of a contaminated area the land must be remediated from harmful levels of pollutants. Investigations and remediation of former industrialized sites are expensive and time consuming projects (Brandon, 2013).

A core problem with remediation of contaminated land includes how to predict the distribution of pollutants in the ground. How far and deep the pollutant is spread and to what degree must be measured to decide on an appropriate remediation method. However, the number of soil samples at a contaminated site is often limited. Moreover, every project requires the commitment of financial and human capital. A highly prioritized goal in remediation work is to find a method that is cost effective, and still accurate enough to minimize the risk of spread to the humans and the environment.

Geographical Information Systems (GISs) and geostatistical methods are an aid in determining pollution levels in soil volumes. Previous studies have shown that GIS-technology and geostatistical methods are useful in the evaluation of contaminated sites for characterizing contamination levels (Henshaw et al., 2004; Largueche, 2006; Henriksson et al., 2013). Most geostatistical studies focus on the horizontal dimensions. However, soil contamination is a three dimensional phenomenon. There is an advantage of working with quantitative spatial data in GISs but it has been a slow development of integrating 3D volumes (Abdul-Raman & Pilouk, 2008).

Another complicating factor for 3D evaluation at contaminated sites is the differences in vertical and horizontal sampling densities. The soil is usually sampled in boreholes with a high vertical sampling density and low horizontal sampling density. It is easy to take many samples in each borehole but time consuming and expensive to drill many holes. GIS-based systems for management of borehole data in 3D have been developed (Chen et al., 2002; McCarthy & Granerio, 2006; Ranga Vital et al., 2015), although, these systems do not visualize volumes of the data. The study of Delarue et al., (2009) applies a 3D approach for soil horizons with a capability of 3D volume rendering. However, it is not built on geostatistics and not applied on soil contaminants. Nevertheless, there are studies as Neteler (2001), Piedade et al. (2014) and Wei et al. (2014) that show a great potential of predicting soil contamination volumes in 3D.

The advances in computer technology allow for increasingly applied 3D models. There are examples on various applications in studies of chemical dispersion in the atmosphere (Nichol et al., 2010; Zahran et al., 2013). The advantages working with 3D models are that they resemble the reality, and are more easily interpreted than 2D maps. The 3D evaluation are historically and today common in mining geology and reservoir modeling (Mallet et al., 1989; Cairns & Feldkamp, 1993; Chambers et al., 1999; Xikui et al., 2016) but rarer in soil science.
Hence, the application of subsurface volume models for contamination evaluation is still scarce.

Sweco is a consultancy company that performs remediation and risk assessments of contaminated sites. They are currently working with a project at the harbor in Norrköping, Sweden (Sweco, 2015). The site has a complex contamination history due to industrial activities and the utilization at former gasworks. Therefore, there is a need to increase the information base at the contaminated site. Three contaminants have shown to be of importance in the area; lead, benzene and polycyclic aromatic hydrocarbons (PAHs). These are common soil pollutants expected to be found at former gasworks sites (Luthy et al., 1994). Metals and PAHs are known as the most widespread contaminants around the world (Swartjes, 2011). The three contaminants are also contaminants with different characteristics regarding degradation and transportation in the ground.

A large amount of data is sampled and the use of GIS is well developed throughout the remediation project at Sweco. The soil samples are collected as features with depth attributes and other information of importance for each sample within a GIS. Today the contamination levels are visualized as 2D maps or as 3D points. To get further information about the contamination situation volume interpolation in 3D is requested. There is also a need for a method for 3D interpolation to use in remediation projects. The method should preferably be applicable within the work method with GIS in projects for contaminated sites.

**Aim**

The overall objective of this study is to investigate the possibilities to predict variations of soil pollution levels from soil samples in 3D. Based on a preferable prediction model an aim is also to investigate a work method for 3D interpolation and volume visualization in projects for contaminated land. The study focuses on 3D interpolation from a GIS perspective.

The specific objectives of this study are:

- Is it possible to predict 3D volumes of contaminated soil?
- If so, which prediction model or interpolation method is preferable?
- Does the preferred method depend on type of contaminant?
- Propose a suitable methodology for performing analyses and visualizations of contaminated soils in 3D.

To achieve the aim data sampled by Sweco at the contaminated area in Norrköping that will undergo remediation is used as a case study. The three contaminants lead, benzene and PAH are investigated. Geostatistical analyses of the contaminants are performed in order to find suitable prediction parameters. Various interpolation methods in 3D are tested and evaluated, both geostatistical and deterministic methods. The work method with projects for contaminated sites and GIS at Sweco is studied, as well as suitable software and methods for 3D interpolation and visualization.
2. Background

a) Contaminated Land

The definition of contaminated land differs around the world. The European Environment Agency define a contaminated site as “a potentially contaminated site in which the quantities and/or concentrations of waste or harmful substances are such that – on the basis of the results of risk assessment- they constitute danger to human health and/or the environment” (Prokop et al., 2000). Soil contamination has mainly an anthropogenic source and is found in proximity to cities (Swartjes, 2011). Local soil contamination is a result from intensive industrial activities, insufficient waste disposal, mining, military activities or accidents that have introduced excessive amounts of contaminants to the soil (Brandon, 2013).

Industrialization in more than 200 years in Europe has led to a widespread problem of soil contamination. There are approximately 2.5 million sites in Europe where potential polluting activities have occurred (Panagos et al., 2013). The Swedish Environmental Protection Agency (Swedish EPA) estimates contaminated sites with high risk to about 8000 in Sweden. Most are associated with past or present industrial activities (Naturvårdsverket, 2016). Contamination from past industrial activities mainly originates from the time before 1970. At that time there was not yet any environmental legislation or concern of contaminants (Brandon, 2013).

i) Soil Pollutants and their Characteristics

Soil contamination can be constituted of inorganic and organic pollutants. The most common pollutants in European soils and groundwater are heavy metals, mineral oils, chlorinated hydrocarbons (CHC), PAHs, cyanides, phenols, and BTEX (benzene, toluene, ethylbenzene, and xylenes) (Brandon, 2013).

Depending on contaminant it might end up in water by leaching through the soil to the underlying groundwater, evaporate into the air or bind to the soil. The main processes occurring when pollutants are introduced to the soil are:

- **Adsorption to soil particles**: this is a process where the pollutant is bound to the surface of a soil particle. The degree of adsorption is dependent on both the chemical properties of the pollutant and the soil particle where pH is an important factor. Clay minerals are for example in general adsorbing fewer amounts of heavy metals than organic pollutants.

- **Evaporation to the atmosphere**: the pollutant might volatilize into gaseous form and evaporate into the atmosphere which most commonly occur with organic compounds.

- **Biological uptake or degradation**: once the pollutants are in the ground they become bioavailable to organisms in the soil that metabolizes the contaminant. The contaminant might accumulate or degrade in the organism.

- **Abiotic degradation**: the influences of light (photolysis) or water (hydrolysis) might change the composition of the pollutant compound.
- **Transportation through the soil:** the pollutants may diffuse down in the soil system where main factors regulating the transportation are amount of infiltrating water, soil pore space, and dimensions of the pollutant. At last the contaminant will end up in the ground- or surface water.

The aggregative effect from these processes will decide the distribution in the ground system and further transport to the hydrosphere, biosphere and atmosphere (Warfinge, 1997; Mirsal, 2008).

**Lead**

One of the most common heavy metals found at contaminated sites are lead (Pb) (Wuana & Okieimen, 2011). Lead in surface soils origin from high-temperature processes such as lead ore smelting, coal burning, and leaded petrol. In uncontaminated soils lead is present at concentrations of < 20 mg/kg (Steinnes, 2013). Compared with many other pollutants lead has a long residence time in the environment (Wuana & Okieimen, 2011). The tendency to accumulate can be derived from the low solubility in water (Table 1) and that no microbial or chemical degradation occurs (Steinnes, 2013).

The chemical behavior of lead has shown to be dependent on the content of organic matter. It is strongly adsorbed to soil particles of humic matter, although that requires a pH in the soil above 4. If organic material is absent, lead will bound to clay minerals. In mineral soils adsorption occurs mainly on iron oxides. According to Steinnes (2013) lead is immobile in the soil unless very high concentrations are present. The findings of Jensen (2005) show that the first factor determining the bonding of lead in industrially contaminated soils are the contamination levels.

**Benzene**

Benzene is an easily evaporated compound belonging to the group of volatile organic compounds (VOCs). The main sources of benzene to the environment are petroleum and chemical industries. The high volatility is the controlling physical property in the environmental transportation of benzene. Benzene is highly mobile in the soil and easily transported to the groundwater. This is due to its low adsorption capacity, although with a higher organic content in the soil the adsorption of benzene to the soil tends to increase. Other parameters that influence leaching potential include the soil type, amount of rainfall, depth of the groundwater, and extent of degradation. Benzene is moderately soluble in water and has a high vapor pressure (Table 1). In aerobic conditions benzene is biodegraded in the soil (ATSDR, 2007a).

**Polycyclic aromatic hydrocarbon (PAH)**

PAHs are a group of organic compounds highly persistent and widespread in the environment. The major source of PAHs is the incomplete combustion of organic material such as coal, oil and wood and is commonly related to energy production. The PAHs consist of only carbon and hydrogen compounds. They have two or more aromatic rings with a pair of carbon atoms shared. PAHs that share up to six rings are called “small PAHs” and those with more than six aromatic rings are called “large PAHs”. Polycyclic aromatic carbons are persistent in the environment since they have high melting and boiling points, low vapor pressure, and have a
very low solubility in water (Table 1). The solubility and vapor pressure decreases with heavier compounds and additional aromatic rings. In this investigation the group of large PAHs is studied.

When the PAHs are introduced to the soil the major part will bound to soil particles and become mobile. The factors that are influencing the grade of mobility is sorbent particle size and pore size of the soil. If the PAHs are bound to particles that cannot move through the soil then the mobility of PAHs are limited as well. The tendency to be adsorbed to soil particles has been found to have the most significant correlation with organic carbon content (Abdel-Shafy & Mansour, 2016).

<table>
<thead>
<tr>
<th>Chemical type</th>
<th>Lead</th>
<th>Benzene</th>
<th>PAHs</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chemical formula</td>
<td>Pb</td>
<td>C₆H₆</td>
<td>C13-22H10-14</td>
</tr>
<tr>
<td>Molecular weight</td>
<td>207.2</td>
<td>78.11</td>
<td>152.2 - 276.3</td>
</tr>
<tr>
<td>Melting point</td>
<td>327.4 °C</td>
<td>5.5 °C</td>
<td>11 - 273 °C</td>
</tr>
<tr>
<td>Boiling point</td>
<td>1740 °C</td>
<td>80.1 °C</td>
<td>96.2 - 530 °C</td>
</tr>
<tr>
<td>Water solubility (at 25°C)</td>
<td>Insoluble</td>
<td>1900 mg/L</td>
<td>&gt; 3.93 mg/L</td>
</tr>
<tr>
<td>Vapor pressure</td>
<td>2.77 mm Hg</td>
<td>75 mm Hg</td>
<td>&gt; 0.00032 mm Hg</td>
</tr>
<tr>
<td>Soil adsorption</td>
<td>high (organic)</td>
<td>low</td>
<td>moderate</td>
</tr>
<tr>
<td>Soil transportation</td>
<td>immobile</td>
<td>mobile</td>
<td>immobile</td>
</tr>
<tr>
<td>Degradation in soil</td>
<td>low</td>
<td>moderate</td>
<td>low</td>
</tr>
</tbody>
</table>

### ii) Environmental Pollutant Effects

Once contaminants are in the soil they can undergo chemical changes or degrade into toxic products of different degrees (Fent, 2004). People can be exposed to soil contaminants through ingestion (eating and drinking), skin contact or inhalation. The contaminant can undergo bioaccumulation in the food chain; from a plant growing in the soil to an animal and end up in humans (Wuana & Okieimen, 2011). Soil contaminants may be responsible for a number of health effects from symptoms as skin eruption, to cancer and deaths. The likelihood that health effects occur from exposure to soil contaminants depend on the toxicity, how much of the contaminant is in contact with humans, how long and often the exposure occurs (Swartjes, 2011).

In addition to possible health effects on humans, contamination of the ground can have negative effect on the environment. Elevated levels of contaminants in the soil can harmfully affect plant uptake, animal health, microbial processes and overall soil and groundwater health. Contaminants may change plants metabolic processes and reduce yields or cause visible damage to crops. Reduced plant uptake will decrease the food quality and the soils usability for agricultural production. Contaminated groundwater that ends up in surface waters will cause negative effects on aquatic organisms (Fent, 2004).
iii) The Soil Remediation Process

The term ‘soil remediation’ refers to actions designed to eliminate or reduce the risk associated with contaminated sites (Carlon et al., 2009). A soil remediation project is performed if contamination of a site can be suspected due to the history and past activities. The remediation processes differ depending on type of site and remediation aim. However, there are a variety of general steps performed in all projects for cleaning up contaminated sites (Table 2). These are performed at Sweco and also presented in Mirsal (2008).

Table 2: The general steps performed in projects for soil remediation (Mirsal, 2008).

<table>
<thead>
<tr>
<th>General steps in soil remediation projects</th>
</tr>
</thead>
<tbody>
<tr>
<td>1) Site information gathering</td>
</tr>
<tr>
<td>2) Creating sampling plan</td>
</tr>
<tr>
<td>3) Field sampling</td>
</tr>
<tr>
<td>4) Lab analysis</td>
</tr>
<tr>
<td>5) Risk assessment and description of</td>
</tr>
<tr>
<td>contamination situation</td>
</tr>
<tr>
<td>6) Remediation action</td>
</tr>
</tbody>
</table>

The preliminary preparation in a soil remediation project (step 1, Table 2) is to collect all available information of a contaminated site in order to characterize it. The geographic and geologic conditions are reviewed as well as photographs, maps, and data about previous land use activities. A sampling plan is determined to form the framework of the data collection (step 2, Table 2). The sampling design and sampling locations are dependent on the sampling purpose, topography and geologic conditions of the area. A common design is to specify a grid with equal space covering the investigation area. In each grid cell either a systematic or random sampling pattern is applied.

The soil and groundwater in the contaminated area are sampled (step 3, Table 2). The samples are then sent to a lab for analysis of their chemical concentrations (step 4, Table 2). These results are the information basis to specify the spatial dimensions of the contamination (step 5, Table 2). The analyses of the soil and ground water samples are the foundation for a risk assessment. The general purpose of a risk assessment is to estimate the risks associated with a contaminated site. It aims to evaluate to what degree the risks need to be minimized (Naturvårdsverket, 2009a).

In Sweden, generic guideline values that should not be exceeded are defined by the Swedish EPA (Naturvårdsverket, 2009b). Risk values for two types of land use are defined: ‘sensitive land use’ and ‘less sensitive land use’. At sites with sensitive land use contamination levels should not limit activities for residents, agriculture, and schools. Additionally, surface- and ground water should be protected from contamination in areas classified as sensitive land use. Areas defined as less sensitive land use should allow for activities like commerce, industry, and transport facilities. The generic guideline values for the studied contaminants are shown in Table 3. In the risk assessment the sampled contamination concentrations are compared to the generic guideline values (Naturvårdsverket, 2009a).
Table 3: The generic guideline values for the studied contaminants lead, benzene, and PAH (Naturvårdsverket, 2009b).

<table>
<thead>
<tr>
<th></th>
<th>Sensitive land use (mg/Kg)</th>
<th>Less sensitive land use (mg/Kg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lead</td>
<td>50</td>
<td>400</td>
</tr>
<tr>
<td>Benzene</td>
<td>0.012</td>
<td>0.04</td>
</tr>
<tr>
<td>PAH</td>
<td>1</td>
<td>10</td>
</tr>
</tbody>
</table>

At last an action for reducing the risk or other necessary measures is designed (step 6, Table 2). There are a variety of available remediation methods; removal of the soil, in-situ and ex-situ methods. The action used is a trade-off between the degree of remediation desired to lower the exposure for humans and the environment, what is technically possible to accomplish and economically reasonable (Carlon et al., 2009).

b) Geostatistics

Geostatistics is a set of statistical techniques used in the analysis of georeferenced data that can be applied to environmental contamination and remediation studies. The geostatistical theory originates from the gold mining industry where it evolved from requirements for improved prediction of gold grades in the 1960s. The application incorporates location, spatial relationships and classical statistics into the estimation process (Goovaerts, 1997).

Matheron (1963) developed the geostatistical techniques and introduced the concept regionalized variables. According to the theory regionalized variables exhibit a statistically measurable degree of continuity within a limited region. Within that region a statistical relationship between the value of a pair of regionalized variables and their distance apart can be determined. At greater distances the difference should be statistically independent of each other (Matheron, 1971). The theory of the regionalized variables was later stated in Tobler’s first law of geography ‘Everything is related to everything else, but near things are more related than distant things’ (Tobler, 1971).

If the spatial variation (or spatial autocorrelation) of a regionalized variable can be determined, then that information can be used to predict the values at unknown locations. A regionalized variable has a spatial variation that is unknown but its variability with respect to distance is statistically measurable within a finite area. An underlying assumption in geostatistics is that the regionalized variables have a statistical normal distribution (Houlding, 2000).
i) The Variogram

Variogram modeling is an analysis for establishing the variance of regionalized variables and the distance between them (Houlding, 2000). Samples are divided into lags (distances intervals) to compute the variogram and determine the variance. Sample pairs in each lag with similar distances are compared. The variogram can be derived from the equation (1) of semi-variance.

\[ \hat{\gamma}(h) = \frac{1}{2p} \sum_{i=1}^{p} (z_i - z_{i+h})^2 \]  

(Equation 1)

where

\( \hat{\gamma}(h) \) is the semivariance in lag \( h \),
\( p \) is the number of sample pairs within the lag \( h \),
\( z_i \) is the measured value of sample \( i \), and
\( z_{i+h} \) is the measured value for a sample within the lag distance \( h \) from sample \( i \) (Goovaerts, 1997).

Each lag distance in the variogram must be large enough to contain a sufficient number of pairwise sample comparisons and small enough for detecting the spatial variability. Figure 1a shows a typical appearance of a variogram with a determined spatial variability. Such variogram has three properties; a sill, range and a nugget. The sill is the semi-variance value where the spatial variance ends. The range is the lag distance at which the spatial variance ends. The nugget is the noise in the data or variability in the data at distances smaller than the sampling space. Figure 1b shows a variogram where the spatial variability is random and independent from the distance (Isaaks & Srivastava, 1989).

Geostatistical interpolation methods need to replace the experimental variogram (points in Figure 2) with a variogram model (lines in Figure 2). Variogram values for lag distances that are not computed (between the points) need to be accessed. Spherical, experimental and Gaussian models are the most frequent used. These are commonly fitted by an iterative least squares estimation. As seen in Figure 2 the different models result in different properties for the sill, range and nugget (Goovaerts, 1997).
Within a region the sampled values can have different spatial variance in different directions. This is called anisotropy. To determine if anisotropy exists in a dataset the variogram must be computed in different directions. If the spatial variability only depends on the lag distance the variogram is isotropic (Figure 3a). If the variogram changes with respect to both lag distance and direction (Figure 3b) the variogram is anisotropic (Manto, 2005).

There are two kinds of anisotropy; geometric and zonal anisotropy. Zonal anisotropy occurs when the sill of a variogram changes in different directions. Geometric anisotropy is a more common model for anisotropy. The geometric anisotropy variogram reaches the same sill in all directions but at different ranges. That implies a stronger correlation in one direction than in other directions (Goovaerts, 1997). Directions in both the plane and vertical direction must be considered when working with subsurface data. Geometric anisotropy is commonly occurring in geological settings due to stratification of different soil material. In such a setting the vertical variogram reaches the sill at much shorter distances than the horizontal variogram (Bohling, 2005).
Plotting the directional ranges of a variogram with geometric anisotropy in 3D space they would fall on the surface of an ellipsoid (Figure 4a). The major and minor axes of the ellipsoid correspond to the largest and shortest ranges of the directional variogram. Six parameters are needed to specify the ellipsoid: three ranges \((h_x, h_y, h_z)\) and three rotation angles \((a_x, a_y, a_z)\) to quantify orientation in a coordinate system (Manto, 2005).

Geostatistical interpolation methods are based on isotropic variogram models. To implement such interpolations correction for anisotropic structures are necessary. The six parameters defining the ellipsoid of anisotropic variogram can be used to transform it to an isotropic one. A three-dimensional lag vector can be transformed into an equivalent isotropic lag vector \((h)\) (Equation 2). Plotting the ranges in 3D space after the transformation they would correspond to a sphere (Figure 4b) (Bohling, 2005).

\[
h = \sqrt{\left(\frac{h_x}{a_x}\right)^2 + \left(\frac{h_y}{a_y}\right)^2 + \left(\frac{h_z}{a_z}\right)^2}
\]

*(Equation 2)*

**ii) Interpolation Techniques**

There are various techniques available for predicting values between locations of existing samples. Some of them are more sophisticated and based on statistical analysis and geostatistics while others are deterministic and based on subjective parameters. The simplest form of interpolation is the average value of all sampled points. The equation (3) for the weighted average value is the foundation for the more sophisticated interpolations.

\[
\hat{z}_p = \frac{\sum_{i=1}^{n} \lambda_i \times z_i}{\sum_{i=1}^{n} \lambda_i}
\]

*(Equation 3)*

where

- \(\hat{z}_p\) is the interpolated value in point \(p\),
- \(n\) is the number of observed samples,
- \(z_i\) is the attribute value of sample \(i\),
- \(\lambda_i\) is the weight of \(z_i\)

The mean value interpolation has a \(\lambda_i\) value of 1 for all sample observations.
Nearest Neighbor
The Nearest Neighbor interpolation assigns an interpolated value to an unknown point the same value as the nearest sampled point. It is an area based method where Thiessen polygons are created around the sampled value. The method aims to preserve the local differences. In a three dimensional approach if the vertical sampling resolution is denser than the horizontal a scale effect can be added to reduce the resolution differences. In this case all the weight \((\lambda_i)\) in Equation 3 are given to the Nearest Neighbor of a sampling point. It is a simple form of interpolation where no further parameter needs to be assigned to the Nearest Neighbor.

Splines
Another deterministic group of interpolation techniques are based on splines. A spline is a type of piecewise polynomial that generates smooth, curved lines that can be conformed to a smooth surface. The interpolated values in spline interpolation are not adapted to the measured values to avoid local maximum and minimum values. This method aims to keep the global smoothness. There are many versions of spline interpolation where one of the most widely used is regularized spline with tension and smoothing (RST) (Mitášová and Mitáš, 1993). The RST interpolation is deterministic in the way that both a smoothing and a tension parameter need to be determined. The equation for RST can be obtained from Mitášová and Mitáš (1993).

Inverse distance weighting (IDW)
IDW interpolation is another deterministic interpolation technique described by Shepard (1968). IDW interpolation gives a weight for each measured sample inversely proportional to its distance from the point being interpolated. The principle of using inverse distances are based on Tobler’s first law of geography (Tobler, 1970), and emphasizes the spatial similarity of near points.

The equation for IDW interpolation is similar to the mean value (Equation 3). However, the weight \((\lambda_i)\) in Equation 3 is equal to the inverse of the distance from sample \(i\) to point \(p\) \((\frac{1}{d^k})\) \(k\) is an estimated weight exponent for the spatial dependence. The exponent \(k\) decides how strong the influence of near points should be. A high value of \(k\) corresponds to a strong spatial influence. Another factor influencing the values of the interpolated points is the search radius and how many points that should be included in the interpolation. The search radius in both horizontal and vertical directions must be considered when interpolating subsurface data at different depths (Isaaks & Srivastava, 1989).

Kriging
Kriging is a geostatistical interpolation method for optimal spatial estimation. It was first published by Krige (1951). The Kriging interpolation is more advanced than previous mentioned interpolation methods and requires a geostatistical analysis and variogram modeling before it can be applied. Kriging interpolation produces more objective maps, and apart from interpolating based on the spatial autocorrelation it can produce an error estimation of the prediction.

The simplest form of Kriging and most commonly applied is called ‘Ordinary Kriging’. In Kriging interpolation the weights \((\lambda_i)\) in Equation 3 is based on the variogram properties. The
The kriging algorithm will give more importance to semi-variance values with a large number of sample pairs and at short distances (Oliver, 2009). Important requirements for Ordinary Kriging interpolation are that no trend exists in the data, the variogram is constant in the studied area, and that the interpolated value follows a normal distribution (Hengl, 2007).

c) Geographical Information Systems (GISs) in Three Dimensions

GISs are tools for capturing, storing, manipulating, and analyzing data with a spatial dimension. Many GISs used within geoscience are based on two-dimensional (2D) or two-and-a-half-dimensional (2.5D) spatial data. Spatial objects are represented in the form of vector points, lines, polygons and raster surfaces. A general GIS has difficulties managing and visualizing geographical data with a greater dimension. There are limits in 3D representation of such data since multiple z-values cannot be displayed within the same surface (Figure 5). Samples from the subsurface and borehole data have in most cases multiple z-values at the same location. Therefore, for a general GIS there are limitations in subsurface geologic modeling (Abdul-Rahman & Pilouk, 2008). To find boundary and limits of soil contamination there is a need of representing the samples as volumes rather than surfaces. Subsurface data requires exploratory interpolation tools that traditionally are not part of a GIS (Setijadji, 2003). GIS software that handles 3D representations is rarer due to the complexity of the 3D data structure (Abdul-Rahman & Pilouk, 2008).

![Figure 5: A 3D surface and samples with multiple z-values that are not represented in the surface.](image)

i) 3D Data Structures

In a GIS the most common and simple data structure representing a volume or a body is the “voxel”. The term voxel represents “volume”, “pixel” and “element”. That is a regular 3D grid of cells, each with its unique attributes and coordinates (Figure 6a). Typically these data structures are stored as a one-dimensional array of element (Abdul-Rahman & Pilouk, 2008). Each element is defined by the x, y, and z coordinates of the voxel centroid. Each voxel centroid in the data structure represents a finite equal volume. In that way the 3D grid simulates a spatially continuous measure of a variable. That by assigning values which are representative of a determined, small volume to points at regular intervals. One disadvantage of this data structure is that it requires large computer space for a high resolution grid (Houlding, 2012).
A more sophisticated form of the 3D grid structure is the Octree (Figure 6b). The Octree structure allows for irregular voxels with different sizes. The Octree voxels are stored in a tree data structure. The root in the tree structure is conceptually a “universe cube” containing all voxels in the object. The cube has eight nodes representing eight identical cubes inside the root cube called octants. These cubes can either be inside or outside the object. Each octant is subdivided into eight octants repetitively until the smallest size of the object is represented (Abdul-Rahman & Pilouk, 2008).

Constructive solid geometry (CSG) is a way of representing objects as predefined geometric solids (Figure 6c). These could be spheres, cubes, cylinders etc. and are more commonly used in solid 3D modelling such as CAD (Mallet, 1992), and will not be presented further in this study.

Another way of representing 3D volumes in GIS is a 3D tetrahedral network (TEN) (Figure 6d). That is an extension of the 2D triangular network (TIN). An object is described by connected tetrahedral with four vertices, six edges, and four faces. The TEN structure has the advantage of having a simple data structure and fast topological structure. However, the representations of TENs in many GIS are limited (Abdul-Rahman & Pilouk, 2008).

**ii) 3D Software**

In the following section examples of identified software for interpolation and visualization of 3D soil contamination volumes are presented. A further overview of geostatistical 3D software is found in Goovaerts (2009). Table 4 summarizes the general characteristics of the identified software.

**Mining Visualization System (MVS)**

C'Techs Mining Visualization System (MVS) is a solid 3D modeling software for visualization of subsurface data. It is used as extension to a GIS for computing and visualizing 3D models. MVS is just one of many solid 3D modeling software and it is not the only one concentrated on subsurface data. This kind of software is in general licensed and expensive.
MVS uses its own type of modeling language to perform operations. It is a visual programming environment where modules are connected in a flow chart of input and output ports. Necessary inputs are coordinates, elevation, surface elevation, and contaminant concentrations for a chosen number of contaminants. To compute volumes MVS perform Kriging interpolation. The computation is completely automated where no previous knowledge from the user is needed. That is, without specifying any parameters the optimal variogram and Kriging interpolation is performed according to the system. However, there are options for specialists with knowledge of the data to manipulate the variogram variables. MVS displays the data in a format of a regular grid. For example, there are options for visualizing soil pollution concentrations in different geological layers and as volumetric plumes of certain soil pollution concentrations (C’Tech, 2015).

**SADA**

Spatial Analysis and Decision Assistance (SADA) is a freeware program developed at the University of Tennessee. It is designed for environmental characterization and remediation. The functionalities of SADA are multidisciplinary and provide tools recognized from a GIS but include also sampling design, risk assessment, remedial design, and cost/benefit analysis. SADA comes with the possibilities of 2- and 3D interpolation and visualization (Purucker et al., 2009).

The available 3D interpolation methods in SADA are: Nearest Neighbor, IDW, Ordinary Kriging, Ordinary Cokriging, and Indicator Kriging. The input to SADA requires a strict format where only one contaminant can be imported at the time. No elevation surface is used, the samples are computed as depth below the surface. The workflow for computing volumes and visualize the data in SADA is an approach where the user is lead through a number of steps. At first the site is set up, and grid spacing and vertical layers are defined. The grid and vertical layers defines the voxels used to visualize the data. An interpolation method is chosen and parameters are specified. In Kriging interpolation the variogram must be computed and the optimal parameters defined. SADA suggest default values for the variogram but these are not intended to be the optimal ones (SADA, 2005).

**ArcGIS**

ArcGIS is one of the most developed and widespread GISs in various fields. It is a group of software routines developed by Environmental Sciences Research Institute (ESRI). ArcGIS requires a license but in Sweden many municipalities and consultancy companies have access to the software. The most common ArcGIS software is ArcMap that handles and visualizes geospatial information in 2D. In the software ArcScene and ArcGIS Pro the data can be visualized in 3D as well. ArcGIS does not have a data type for volumes but can still render data in 3D. The outputs of the 3D analyst tools found in the software are 2.5D surfaces and not volumes.

The software can be manipulated to perform 3D interpolation and then render points as 3D cubes. A proposed method for volume interpolation and visualization is presented in figures 7 and 8. At first a 3D point grid is created at the site to be interpolated. It is created from a 2D grid that is copied with changing z-values for the desired depth.
The 3D distance from sampled data to the grid points are computed. The 3D distance can be used to perform interpolations such as IDW or Nearest Neighbor. When the interpolation equations are implemented predicted values are joined to the 3D grid points. At last, these are rendered as rectangular cubes with the same size as the distance between the points in ArcScene or ArcGIS Pro.

**GRASS GIS**

Geographic Resources Analysis Support System (GRASS) is a free and open source GIS from Open Source Geospatial foundation. It includes all regular tools for storing, manipulating, and analyzing data with a spatial dimension. It is one of few GISs supporting 3D interpolation and visualization.

The 3D data in GRASS is stored in regular grids as voxels with the octree structure. It is represented in the same way as a 2D raster with an additional dimension. The import data for sampled data to GRASS should be as 3D vector points. The available methods for interpolating volumes in GRASS are the spline interpolation RST and IDW. To compute a volume from 3D vector points a 3D mask raster must be created with a defined region and size of the grid that should be interpolated.

<table>
<thead>
<tr>
<th>Interpolation methods</th>
<th>3D Data structure</th>
<th>Licensed</th>
<th>GIS</th>
<th>Input</th>
<th>Usability</th>
</tr>
</thead>
<tbody>
<tr>
<td>MVS</td>
<td>Kriging, IDW</td>
<td>Solid 3D models</td>
<td>Yes</td>
<td>Compatible</td>
<td>Software specific modeling language</td>
</tr>
<tr>
<td>SADA</td>
<td>Kriging, IDW, Nearest Neighbor</td>
<td>Voxels</td>
<td>No</td>
<td>Compatible</td>
<td>Software specific user interface with working steps</td>
</tr>
<tr>
<td>ArcGIS</td>
<td>IDW, Nearest Neighbor</td>
<td>3D points</td>
<td>Yes</td>
<td>Yes</td>
<td>3D points</td>
</tr>
<tr>
<td>GRASS</td>
<td>RST, IDW</td>
<td>Octree voxels</td>
<td>No</td>
<td>Yes</td>
<td>3D points</td>
</tr>
</tbody>
</table>

**Table 4: A summary of the characteristics of identified software for 3D interpolation and visualization.**
3. Methods

a) Site Description

The study site is a 140 x 280 m large area in central Norrköping, Sweden (58°35'43.8"N 16°11'55.5"E (WGS 84)) (Figure 9). It is located in an industrial area at the harbor by the river Motala Ström. The municipality of Norrköping is planning to exploit and build a residential area at the site. Today the site is a paved quayside with open areas, small industries and commerce (Figure 10a).

The site has been used as shipbuilding industry from the 18th Century to the early 20th Century. In mid-19th Century a 1000 m² large dock was built (Figure 10b). At the same time period as the dock was built a gasworks was constructed for gas making from coal. The gasworks activity was expanding in the area and was located at different locations until it ended in the late 20th Century (Figure 10c). Apart from the gas making from coal, extraction of benzene took place, and another gasworks with gas generation from naphtha took place. One waste product from the gas generation was tar. The dock and the abandoned sites of the gasworks were later filled with coal remnants from the gasworks (Sweco, 2015).

The site is located on a 1 to 5 m deep layer of landfill made up by gravel, sand and a mix of waste products as brick, glass, asphalt, coal, slag and oil (Figure 10d). Beneath the landfill layer the soil consist of clay and mud. This layer varies between 16 and 28 m. The clay layer translates into silt and boulders have been found at depths of about 13 to 28 m (Sweco, 2015).
b) Sampling Procedure

At the request of Norrköping municipality Sweco has performed various investigations, and has sampled the soil and groundwater. The data used in this study was sampled during December 2015. A grid resolution of 20 x 20 m that covers the sampled area was used. A systematic sampling pattern was performed with the goal of a sampling point for each corner in the grid. Additional points in the center of each grid cell at areas of more concern were also sampled (Figure 11). Missing or relocated points in the grid are due to that older samples exist, cables or pipes in the ground, or other obstructions at the concerned location. A previous sampling dataset from July 2015 are used for validation. The validation data is distributed across the study area.

Prior the field sampling a Web Map Service (WMS) was set up at ArcGIS Online. It included a map of the area, the sampling grid, and a feature for each sampling point with its ID. Related tables were created supplementary to the point features. Attributes for the related tables were set up as predefined choices for soil types and soil classes. Additionally, columns for sampling depths were defined. Via the app Collector people working within the project can reach the sampling map and edit the point features in the field and fill in the attributes regarding depth and soil type for each sample.

The map in Collector was used to identify the sampling locations in the field. The drilling was performed with a screw auger. It drilled in 0.5 m intervals down in the ground. Soil samples from each interval was collected and sent to the lab. The drilling continued until natural soil was reached and an additional 0.5 m down in the soil. Due to obstructions in the ground the borehole might not correspond exactly to the location in Collector. The exact location and height was later measured with a total station.

In Collector information about each point feature was added. Facts about sampling depths, soil types, soil classes and other relevant information are completed in the related table for each sampling point. The related tables were later used within ArcMap to join point features and the related tables. In that way one feature for each depth is created. These are linked to the lab results and used to describe the contamination situation in ArcMap or ArcScene.
c) Data

The data used in the study is summarized in Table 5. In total 763 samples from 126 boreholes were used. The validation dataset consist of 188 samples. The validation data has a mean depth of 1.9 m and maximum depth of 2.9 m. An elevation model was used for surface height information.

Table 5: A summary of the data used in the study.

<table>
<thead>
<tr>
<th>Data</th>
<th>Type</th>
<th>Coordinate System</th>
<th>Projection</th>
<th>Origin</th>
</tr>
</thead>
<tbody>
<tr>
<td>763 samples</td>
<td>Feature class</td>
<td>SWEREF 99 TM</td>
<td>SWEREF 99 1630</td>
<td>Field sampling, 12-2015 (Sweco)</td>
</tr>
<tr>
<td>188 validation samples</td>
<td>Feature class</td>
<td>SWEREF 99 TM</td>
<td>SWEREF 99 1630</td>
<td>Field sampling, 07-2015 (Sweco)</td>
</tr>
<tr>
<td>Elevation model</td>
<td>TIN</td>
<td>SWEREF 99 TM</td>
<td>SWEREF 99 1630</td>
<td>Laser scanning (Sweco)</td>
</tr>
</tbody>
</table>

d) Choice of Software

SADA was chosen for the computation of 3D interpolations (Table 6). In SADA it is possible to define the parameters that should be used in the computation. Moreover, SADA allows for evaluation of many different interpolation methods, both geostatistical and deterministic methods which was not possible in the other software (Table 4). It was also the only comprehensive software available where no programming or license is necessary.

Prior the interpolations, the statistical and geostatistical analyses were performed in R and the subprogram Rstudio (Table 6). R allows for handling data in three dimensions. With the GSTAT package it is also possible to compute variogram models in three dimensions (Pebesma, 2004). Beyond that, R is used due to the large freedom and control of the analyzed data. Variogram computation is also available in SADA but R allows for more detailed and controlled analyses necessary for some of the aims of the study.

The interpolated outcomes were later transferred back into ArcGIS (Table 6) for validation and the subsequent visualization since the possibilities to control the data are limited in SADA. The reason for that is to be able to use the validation dataset, combine the interpolated outcome, and easily work with the data. ArcGIS was used for visualization to avoid more data processing than necessary. To keep the data in ArcGIS allows for continuous data processing at Sweco and further risk assessments.

Table 6: A summary of the software used in the study.

<table>
<thead>
<tr>
<th>Software</th>
<th>Application</th>
<th>Origin</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rstudio</td>
<td>Statistical and geostatistical analysis</td>
<td>Rstudio Team (2015)</td>
</tr>
<tr>
<td>R 3.2.4</td>
<td>Statistical and geostatistical analysis</td>
<td>R Core Team (2016)</td>
</tr>
<tr>
<td>SADA 5.0</td>
<td>3D interpolation, validation</td>
<td><a href="http://www.sadaproject.net/">http://www.sadaproject.net/</a></td>
</tr>
<tr>
<td>ArcMap 10.3.1</td>
<td>Validation, 2D visualization</td>
<td><a href="http://www.arcgis.com/">http://www.arcgis.com/</a></td>
</tr>
<tr>
<td>ArcScene 10.3.1</td>
<td>3D visualization</td>
<td><a href="http://www.arcgis.com/">http://www.arcgis.com/</a></td>
</tr>
</tbody>
</table>
**e) Geostatistical Analysis**

The procedure to investigate the spatial dependence in the data is described in Figure 12 (*step a-e*). At first, a statistical analysis is performed in R to get an idea of the distribution of the data (*a*). Since the normal distribution is an underlying assumption in geostatistics the data must be transformed if the data is skewed (*b*). Another underlying assumption is that there should not be any trend in the data. The data is investigated to find any existing trend (*c*).

At last, variogram can be computed to look for any spatial dependence in the data, and if that dependence is correlated (*e-f*). The variogram parameters that are determined in R are described in Figure 13.

The covariance of the regionalized variable and the lagged regionalized variable is computed. It is used to confirm the correlation and is computed with Equation 4.

\[
C(h) = \frac{1}{n-1} \sum_{i=1}^{n}(z(x_i) - \mu) \times (z(x_i + h) - \mu_h)
\]  
*(Equation 4)*

where

- \(C(h)\) is the covariance in lag \(h\)
- \(n\) is the number of samples in lag \(h\)
$z(x_i)$ is the attribute value at location $x$ of pair $i$

$z(x_i + h)$ is the attribute value at location $x + h$ of pair $i$

$\mu$ is the mean value in the corresponding lag (Goovaerts, 1997).

Additionally, correlation with soil types and soil classes were investigated. If a significant correlation was found it was investigated if the spatial dependence varied in different soils.

**f) 3D Interpolations**

The method from interpolation to implementation is described in Figure 14. 3D interpolations are performed in SADA with parameters based on the geostatistical analysis. Three different interpolation methods available in SADA were tested; Ordinary Kriging, IDW and Nearest Neighbor. All parameters in the interpolations cannot be determined from the geostatistical analyses. One of these was the length of the search radius which was tested for in the Kriging and IDW interpolations. The IDW interpolation was also tested for different exponents, whereas the Nearest Neighbor interpolation was tested for different vertical exaggerations.

The 3D distances between points that will be interpolated with new values must be predefined. That is the thickness of the vertical layering and the horizontal grid spacing. The grid spacing and layering should be set to 5-10 times smaller than the range, or in general one fifth of the sampling density (Houlding, 2000). This was considered when deciding on the resolution of the interpolations.

In SADA, the outcomes of the interpolations with different parameters were evaluated with cross validation. In cross validation the interpolations are computed where one sample at the time is excluded and then used for validation with the predicted value. From cross validation an RMSE value can be obtained. The RMSE is a measure of the difference between sampled data and predicted data. It is a common measure for validity prediction. The RMSE value was computed using Equation 5 (Isaaks & Srivastava, 1989).

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^{N} \{ z(x_i) - \hat{z}(x_i) \}^2} \quad (Equation \ 5)$$

where

$N$ is the number of samples

$z$ is the sampled value at location $x_i$

$\hat{z}$ is the predicted value at location $x_i$

The predictions with parameters resulting in lowest RMSE from cross validation were chosen. These were imported into ArcGIS for back transformation and adding the trend back for the Kriging interpolations. The validation dataset was used to find the nearest interpolated values in 3D distance from a validation sample. The value of the validation sample and the predicted value were compared. The validity of the final predictions was obtained from the RMSE value.
To see how the predicted contamination levels change with depth, the mean concentration of each contaminant at different depths are computed. Lastly the predicted models for each interpolation method and contaminant are visualized based on their risk levels. The contaminated volumes are computed from the number of samples and their grid size.

4. Results

a) Geostatistical Analysis

In the following sections the outcomes of the statistical and geostatistical analyses are presented.

i) Statistical Analysis and Data Transformation

The results from the lab analysis are shown in figure 16a-c and are based on the risk levels in Table 3. The results are the foundation for the continued statistical analyses. There is a high frequency of samples close to the surface and down to about 2.5 m (Figure 17). The sampling frequency deeper than 4 m is less than 20 in each 0.5 m interval.
Figure 16a: The sampling and concentration distributions of lead.

Figure 16b: The sampling and concentration distributions of benzene.

Figure 16c: The sampling and concentration distributions of PAH.

Figures 16a-c: The classifications originate from Table 3. Less sensitive land and sensitive land are divided into two classes for each contaminant.
In Table 7 the descriptive statistics of the contaminant levels are presented. All three contaminants have lower medians than mean values. That indicates positively skewed data. That is a result of a high frequency of low concentrations and some exceptional high concentrations in the datasets. This is a common distribution of soil contaminants (Juang et al., 2001).

<table>
<thead>
<tr>
<th></th>
<th>Lead (mg/Kg)</th>
<th>Benzene (mg/Kg)</th>
<th>PAH (mg/Kg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Min.</td>
<td>0.55</td>
<td>0.00175</td>
<td>0.15</td>
</tr>
<tr>
<td>1st Quartile</td>
<td>9.2</td>
<td>0.00175</td>
<td>0.15</td>
</tr>
<tr>
<td>Median</td>
<td>18</td>
<td>0.00175</td>
<td>1.1</td>
</tr>
<tr>
<td>Mean</td>
<td>106.5</td>
<td>13.11</td>
<td>37.81</td>
</tr>
<tr>
<td>3rd Quartile</td>
<td>58.5</td>
<td>14</td>
<td>13</td>
</tr>
<tr>
<td>Max.</td>
<td>8300</td>
<td>130</td>
<td>1700</td>
</tr>
<tr>
<td>NA</td>
<td>8</td>
<td>0</td>
<td>8</td>
</tr>
<tr>
<td>Std</td>
<td>464.14</td>
<td>25.05</td>
<td>152.12</td>
</tr>
<tr>
<td>Variance</td>
<td>215426.2</td>
<td>627.26</td>
<td>23139.71</td>
</tr>
</tbody>
</table>

The skewed distributions of the data required a transformation (Figure 18). The most commonly used transformation is the logarithmic transformation (Houlding, 2000). Logarithmic transformations of the data result in a normal distribution for lead. The other two contaminants were transformed with a normal score transformation. A normal score transformation ranks the data from highest to lowest. The ranks are matched to equivalent ranks generated from a normal distribution. The mean and median in a distribution of normal scores are 0.
ii) Trend Analysis

The mean concentrations and standard variations at depth intervals of 0.5 m from the elevation surface and down in the ground are shown in Figures 19a-c.

Lead shows a pattern of lower concentrations at the surface and an increase in concentrations just below the surface 0.5-1.5 m down. Levels of lead and PAH (Figure 19a and c) are low or nonexistent from 2 to 4 m down in the ground. The lead concentrations are close to 0 while the PAH concentrations are a bit higher. There are some exceptional high values from 4 to 6 m below the surface for PAH and lead. Although, at these depths the standard variations are high and sampling frequency low (Figure 17). The differences for minimum and maximum values (Table 7) in the datasets for PAH and lead are very large. One single high value will have large effect on the mean value. It is therefore difficult to tell if a real increase in concentration levels exist. The concentrations of benzene show a slightly different pattern than the other two pollutants (Figure 19b). The level is varying with depth but show a general trend of increase with depth.
A regression line is fitted to see if there is a trend in depth. As seen in figure 20a-c, visually looking at the trend lines and the $R^2$ values, there are no strong correlation with concentrations and depths. The PAH concentrations are decreasing with depth as well as the lead concentrations, although not that strong. Benzene behaves differently and indicates an opposite trend or no trend at all in concentration level and depth. It needs to be considered that the samples are clustered closer to the surface and less frequently sampled at deeper levels (Figure 17).

Another analysis was performed to search for significant global trend surfaces in the area. Linear trend surfaces and polynomial trend surfaces (degree 2) were fitted to the data in 3D. As seen in Figure 21, all three contaminants have significant (*) trend surfaces at a 0.001 significance level. Benzene and PAH have significant trend surfaces for both linear and polynomial trends. The residuals of the linear trend surfaces for benzene and PAH were used in the continued analyses since the simplest trend is preferred. The residuals of the polynomial trend surface for lead were used in the continued analyses.

Figure 20a-c: The concentrations variation with depth for samples of lead (a), benzene (b), and PAH (c), and their trend lines.

Figure 21: Linear and polynomial trend surfaces fitted to the three contaminants. The trend surfaces used in continued analysis are marked with dashed lines.
iii) Variogram Modeling

The parameters of the variogram are specified in Table 8, and were set to suit the sample spacing in the studied area. The lag width for the variogram analyses in the vertical and horizontal directions was set equal to the sampling spacing. The maximum distance to compute semi-variance in was set to the maximum width and depth of the sampling area. Various horizontal- and vertical tolerances (Figure 14) were tested to include a sufficient amount of samples. Different dip- and plane directions were tested to detect any spatial dependence in the area. The main directions are presented in Figures 22 and 23.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Horizontal Parameters</th>
<th>Vertical Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lag width</td>
<td>10 (m)</td>
<td>0.5 (m)</td>
</tr>
<tr>
<td>Max. distance</td>
<td>250 (m)</td>
<td>9 (m)</td>
</tr>
<tr>
<td>Direction in plane (x,y)</td>
<td>0°</td>
<td>0°</td>
</tr>
<tr>
<td>Horizontal tolerance</td>
<td>30°</td>
<td>30°</td>
</tr>
<tr>
<td>Dip direction (z)</td>
<td>0° (-90°)</td>
<td>-90°</td>
</tr>
<tr>
<td>Vertical tolerance</td>
<td>30°</td>
<td>30°</td>
</tr>
</tbody>
</table>

The actual lag widths and number of pairs in each lag that the parameters were set to are found in Table 9. The number of sample pairs in each lag must contain a sufficient amount of pairs to detect the variance of the samples (Isaaks & Srivastava, 1989). In the horizontal variograms sample pairs up to about 140 m are included, and samples down to about 4 m in the vertical variograms.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Horizontal</th>
<th>Vertical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of pairs</td>
<td>Lag distance</td>
<td>Number of pairs</td>
</tr>
<tr>
<td>2571</td>
<td>2.08</td>
<td>595</td>
</tr>
<tr>
<td>2780</td>
<td>16.74</td>
<td>509</td>
</tr>
<tr>
<td>2884</td>
<td>24.12</td>
<td>371</td>
</tr>
<tr>
<td>3394</td>
<td>34.68</td>
<td>300</td>
</tr>
<tr>
<td>5566</td>
<td>44.87</td>
<td>202</td>
</tr>
<tr>
<td>5863</td>
<td>55.37</td>
<td>132</td>
</tr>
<tr>
<td>4704</td>
<td>65.68</td>
<td>92</td>
</tr>
<tr>
<td>5135</td>
<td>74.27</td>
<td>83</td>
</tr>
<tr>
<td>5171</td>
<td>84.82</td>
<td>60</td>
</tr>
<tr>
<td>3585</td>
<td>95.34</td>
<td>45</td>
</tr>
<tr>
<td>3446</td>
<td>104.17</td>
<td>35</td>
</tr>
<tr>
<td>2848</td>
<td>114.75</td>
<td>31</td>
</tr>
<tr>
<td>1627</td>
<td>125.58</td>
<td>19</td>
</tr>
<tr>
<td>704</td>
<td>134.23</td>
<td>6</td>
</tr>
<tr>
<td>550</td>
<td>143.06</td>
<td>2</td>
</tr>
<tr>
<td>94</td>
<td>153.94</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>173.14</td>
<td></td>
</tr>
</tbody>
</table>
Figure 22 shows the results of the experimental variogram for the contaminants in the horizontal and vertical direction. Both the original transformed concentrations and their residuals after trend removal are plotted. Benzene is the only contaminant showing a clear difference after trend removal.

The first lag in the horizontal plots is shorter than the sample spacing in the plane (Table 9). That lag is present due to the vertical tolerance (Table 8) that include pairs with a vertical sampling spacing of 0.5 m. If the first lag in the horizontal plots is disregarded no increase or range in semi-variance can be found. The semi-variance structure for all three contaminants in the horizontal plane does not seem to be related to distance; at this scale no spatial dependence is detected. The semi-variance structures in the vertical plots show a sign of spatial dependence. All contaminants have an increasing semi-variance up to about 2 m before they reach the sill. At larger distances the plots become noisy due to decreasing pair numbers.

*Figure 22: The results of the horizontal and vertical variogram computations of the studied contaminants.*
In Figure 23a-c, directional variogram in the plane are plotted. The sill values do not change for any of the contaminants in different directions. Neither spatial dependence nor differences in dependence are found for any of the contaminants for various directions.

Figure 23a: Directional variogram of lead samples in six directions in the plane (0 equals North and 180 South).

Figure 23b: Directional variogram of benzene samples in six directions in the plane (0 equals North and 180 South).

Figure 23c: Directional variogram of PAH samples in six directions in the plane (0 equals North and 180 South)
In Figure 24a the covariance of different lags in vertical direction for lead concentrations are shown. The first lag (0-0.5 m) shows a correlation of lead concentrations with lagged concentrations. In the next lag (0.5 – 1 m) the correlation decreases. In the following lags the correlation continues to decrease. A decreasing correlation at larger distances is a sign of spatial dependence. There is an indication of spatial autocorrelation up to about 1 m. No correlation was found in covariance for concentrations in the horizontal plane.

In Figure 24b, the covariance of different lags in vertical direction for benzene concentrations are shown. The correlation is strongest in the first lag (0-0.5 m) and decreases with lag distance. The correlation seems to be stronger for low concentrations than for high concentrations. There is a sign of spatial dependence up to about 2 m.
In Figure 24c, the covariance of different lags in vertical direction for PAH concentrations are shown. As for the other contaminants, the correlation is strongest in the first lag (0-0.5 m) and decreases with increase in lag distance. There is a sign of spatial dependence up to about 1 m.

![Figure 24c: The covariance of PAH in short lags of 0.5 m intervals in the vertical plane down to a depth of 9 m.](image)

Variogram models are fitted to the variogram where a spatial dependence was found (Figures 25a-c). The variogram model used was the spherical model since this is one of the most common models for variogram fit (Goovaerts, 1997), although other models were also investigated in case of a better fit. The initial model parameters were set from the experimental variogram. A nugget needs to be defined to get an adequate suit of the variogram model for benzene. The final parameters are defined in Table 14.

![Figure 25a-c: The vertical variograms where a spatial dependence was found and fitted variogram models.](image)

iv) Soil Dependence

The transportation in the ground of the three contaminants is expected to differ in different soils, as well as their ability to travel with the groundwater. Each sample in the datasets has attributes for soil type and soil class (fill material or natural soil). Initially, a geologist at Sweco (Sweco, 2016) divided the soil types into seven soil groups with similar properties for analysis. It turned out that the frequency of samples in the soil groups vary from 7 to 412 (Table 10). There is a difficulty performing accurate statistics on groups with these differences in size. Finally, the division into two soil classes was used for analysis.
Table 10: Soil groups and soil classes determined for each sample in the dataset.

<table>
<thead>
<tr>
<th>Soil class</th>
<th>Fill material</th>
<th>Frequency</th>
<th>Natural soil</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>Peat</td>
<td>8</td>
<td>Clay</td>
<td>125</td>
<td></td>
</tr>
<tr>
<td>Loam</td>
<td>12</td>
<td>Silt</td>
<td>7</td>
<td></td>
</tr>
<tr>
<td>Gravel/Sand</td>
<td>412</td>
<td>Mud</td>
<td>57</td>
<td></td>
</tr>
<tr>
<td>Coal</td>
<td>34</td>
<td>Total</td>
<td>189</td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>466</td>
<td>Total</td>
<td>189</td>
<td></td>
</tr>
</tbody>
</table>

An analysis of variance was performed to investigate if the contaminant concentrations in the two soil classes are significantly different. Figures 26a-c show boxplots of the contaminant levels in each soil class. According to the variance analysis (Tables 11 and 13) there is a significant difference in concentrations in the two soil classes for lead and PAH, at a 0.0001 significance level. There is no significant difference in concentrations for benzene (Table 12).

Table 11: Variance analysis of lead concentrations in soil classified as fill material and natural soil.

<table>
<thead>
<tr>
<th>Source</th>
<th>df</th>
<th>SS</th>
<th>MS</th>
<th>F</th>
<th>p</th>
</tr>
</thead>
<tbody>
<tr>
<td>Between groups</td>
<td>1</td>
<td>138.81</td>
<td>138.81</td>
<td>83.976</td>
<td>&lt; 2.2e-16</td>
</tr>
<tr>
<td>Within groups</td>
<td>626</td>
<td>1034.75</td>
<td>1.653</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>627</td>
<td>1173.56</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 12: Variance analysis of benzene concentrations in soil classified as fill material and natural soil.

<table>
<thead>
<tr>
<th>Source</th>
<th>df</th>
<th>SS</th>
<th>MS</th>
<th>F</th>
<th>p</th>
</tr>
</thead>
<tbody>
<tr>
<td>Between groups</td>
<td>1</td>
<td>3.11</td>
<td>3.1067</td>
<td>3.5833</td>
<td>0.05882</td>
</tr>
<tr>
<td>Within groups</td>
<td>633</td>
<td>548.81</td>
<td>0.86701</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>634</td>
<td>551.92</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 13: Variance analysis of PAH concentrations in soil classified as fill material and natural soil.

<table>
<thead>
<tr>
<th>Source</th>
<th>df</th>
<th>SS</th>
<th>MS</th>
<th>F</th>
<th>p</th>
</tr>
</thead>
<tbody>
<tr>
<td>Between groups</td>
<td>1</td>
<td>119.36</td>
<td>119.363</td>
<td>154.07</td>
<td>&lt; 2.2e-16</td>
</tr>
<tr>
<td>Within groups</td>
<td>626</td>
<td>484.98</td>
<td>0.775</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>627</td>
<td>604.34</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Variation in spatial dependence in the two soil classes were investigated for lead and PAH. A difference in the semi-variance in the two soil classes for both lead and PAH is detected (Figures 27a-b). The sill value for lead concentrations in natural soil is about 0.6 and in fill material about 2. The sill value for PAH concentrations in natural soil is about 0.6 and in fill material about 0.8. That indicates that different semi-variance weights should be applied when interpolating in the soil classes.

![Figure 27a-b: Variogram for lead (a) and PAH (b) in two different soil classes as well as semi-variance values for the whole dataset.](image)

**v) Summary**

In the following interpolations residuals from the trend surface of the log transformed lead concentrations are used. For benzene and PAH, the residuals of the normal score transformed values are used.

No anisotropic relationship was found in the data, therefore no correction for 3D anisotropy needs to be performed (Equation 2). A spatial dependence was found at short scales up to about 2 m. The spatial dependence could only be seen in vertical directions. The shortest sampling spacing in the horizontal plane is about 10 m. Therefore, the spatial dependence in the horizontal plane shorter than 10 m is unknown.

There is a significant difference in concentrations in the upper fill material and the underlying natural soil for lead and PAH. The semi-variance values vary in the two soil classes. Therefore, the following interpolations of concentration levels in fill material and natural soil for lead and PAH will be performed separately.

The final outcome of the geostatistical analysis and parameters used in the following interpolations are presented in Table 14.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Lead (fill material)</th>
<th>Lead (natural soil)</th>
<th>Benzene</th>
<th>PAH (fill material)</th>
<th>PAH (natural soil)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>Spherical</td>
<td>Spherical</td>
<td>Spherical</td>
<td>Spherical</td>
<td>Spherical</td>
</tr>
<tr>
<td>Sill</td>
<td>1.81</td>
<td>0.6</td>
<td>0.66</td>
<td>0.84</td>
<td>0.6</td>
</tr>
<tr>
<td>Range</td>
<td>1.18</td>
<td>1.18</td>
<td>2.36</td>
<td>1.32</td>
<td>1.32</td>
</tr>
<tr>
<td>Nugget</td>
<td>0</td>
<td>0</td>
<td>0.31</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>
b) 3D Interpolations

Considering computational complexity, sampling density and ranges a common 3D grid for all interpolations and contaminants were decided. It was set to 5 x 5 m in the horizontal plane and 0.20 m in the vertical plane. Other common parameters in the interpolations were the minimum and maximum included samples. These were set to include at least 2 samples and maximum 20 samples which is default in SADA. In Tables 15, 16 and 17 the final parameters used in the interpolations for the three contaminants are summarized.

The interpolations of fill material and natural soil are separated by the mean depth of the fill material. SADA cannot handle interpolations of a final volume with a varying depth. Points deeper than the mean depth of the fill material (2.6 m) are interpolated with the parameters of the natural soil. Points above 2.6 m are interpolated with parameters for the fill material.

The determined ranges for all three contaminants are shorter than the horizontal sampling spacing. If these ranges were used as search radius in both horizontal and vertical plane there would be no volume outcome. Therefore, different search radius was tested from the shortest sampling spacing to the maximum separated distance between points. It was tested for three different horizontal search radius; 10, 50, and 150 m. The final horizontal search radius for all interpolations was the shortest radius (10 m), except from Kriging of benzene and lead in fill material.

In the Kriging interpolations the discovered range, sill, and nugget parameters were used. The length of the vertical search radius was set to the mean depth of the fill material and the maximum depth of the natural soil. In the IDW interpolation the discovered ranges were used as the vertical search radius length. For each of the search radius lengths three different exponents \((k)\) were tested as well; 1, 2, 3. The final exponent in the IDW interpolation differed among the contaminants. An exponent of 2 was used for PAH interpolations, the exponent 1 was used for benzene, as well as for lead in fill material. The exponent for lead in natural soil was 2.

In the Nearest Neighbor interpolation three different vertical exaggerations were tested; no exaggeration (1), double horizontal distance than vertical (10), and equal distance in horizontal and vertical plane (20). The exaggeration did not affect the error validation since the closest point was the same in all interpolations. The vertical exaggeration of 20 was used in the final interpolations.

<table>
<thead>
<tr>
<th>Table 15: The parameters used in the interpolations of lead concentrations.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Lead</strong></td>
</tr>
<tr>
<td>----------</td>
</tr>
<tr>
<td>OK</td>
</tr>
<tr>
<td>Fill material</td>
</tr>
<tr>
<td>Natural soil</td>
</tr>
<tr>
<td>IDW</td>
</tr>
<tr>
<td>Fill material</td>
</tr>
<tr>
<td>Natural soil</td>
</tr>
<tr>
<td>NN</td>
</tr>
<tr>
<td>Fill material</td>
</tr>
<tr>
<td>Natural soil</td>
</tr>
</tbody>
</table>
Table 16: The parameters used in the interpolations of benzene concentrations.

<table>
<thead>
<tr>
<th>Benzene</th>
<th>Range</th>
<th>Sill</th>
<th>Nugget</th>
<th>Horizontal search radius</th>
<th>Vertical search radius</th>
<th>Exponent</th>
<th>Vertical exaggeration</th>
</tr>
</thead>
<tbody>
<tr>
<td>OK</td>
<td>2.36</td>
<td>0.66</td>
<td>0.31</td>
<td>150</td>
<td>9</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>IDW</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>10</td>
<td>2.36</td>
<td>1</td>
<td>-</td>
</tr>
<tr>
<td>NN</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>20</td>
<td>-</td>
</tr>
</tbody>
</table>

Table 17: The parameters used in the interpolations of PAH concentrations.

<table>
<thead>
<tr>
<th>PAH</th>
<th>Range</th>
<th>Sill</th>
<th>Horizontal search radius</th>
<th>Vertical search radius</th>
<th>Exponent</th>
<th>Vertical exaggeration</th>
</tr>
</thead>
<tbody>
<tr>
<td>OK</td>
<td>1.32</td>
<td>0.84</td>
<td>10</td>
<td>2.6</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Fill material</td>
<td>1.32</td>
<td>0.6</td>
<td>10</td>
<td>6</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Natural soil</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>IDW</td>
<td>-</td>
<td>-</td>
<td>10</td>
<td>1.32</td>
<td>2</td>
<td>-</td>
</tr>
<tr>
<td>Fill material</td>
<td>-</td>
<td>-</td>
<td>10</td>
<td>1.32</td>
<td>2</td>
<td>-</td>
</tr>
<tr>
<td>Natural soil</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NN</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>20</td>
<td>20</td>
</tr>
<tr>
<td>Fill material</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>20</td>
<td>20</td>
</tr>
<tr>
<td>Natural soil</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

i) Validation

The error validation with the validation dataset has an RMSE value for each interpolation. An acceptable interpolation should have a low RMSE as close to 0 as possible. The RMSE values depend on the data range in the original dataset. Therefore, the RMSE cannot be compared among the contaminants.

The RMSE values from the predictions of lead shows that the Kriging interpolation and IDW interpolation are equally good, and better than the Nearest Neighbor interpolation (Figure 28). The difference in RMSE between Kriging and IDW when the interpolations in fill material and natural soil are combined is negligible. The interpolations in the natural soil show the least accurate result from the Kriging interpolation.

Figure 28: The RMSE values for lead interpolations when compared to the validation dataset in the fill material, natural soil and total RMSE when the two are combined.
The RMSE values from the predictions of benzene shows a difference in accuracy among the three interpolation methods (Figure 29). The most accurate interpolation method for benzene is Kriging and the least accurate is the Nearest Neighbor interpolation.

The RMSE values from the predictions of PAH show the least difference in accuracy among the interpolation methods (Figure 30). The interpolations in the fill material and the combined interpolations show equal accuracy for all interpolations, although Kriging and IDW are slightly better than the Nearest Neighbor interpolation. As for the lead interpolations in natural soil, Kriging is the least accurate method for PAH in natural soil.

Figure 29: The RMSE values for benzene interpolations when compared to the validation dataset.

Figure 30: The RMSE values for PAH interpolations when compared to the validation dataset in the fill material, natural soil and total RMSE when the two are combined.
ii) Visualization and Implementation

In this section the final visualizations of the different interpolation methods are presented. The figures show the combined interpolations in fill material and natural soil for lead and PAH. The vertical dimension is exaggerated 5 times to enhance the vertical differences.

**Lead**

It is clear that the estimates of lead show enhanced levels from the surface and 2 m down in the ground (Figure 31). At deeper levels no enhanced levels are estimated. It is due to few samples and low concentrations in the original samples (Figure 17). The Kriging interpolation is the method with largest effect of smoothing. The Nearest Neighbor interpolation does not build on any geostatistics and interpolates the whole volume of natural soil (Figure 32). This method also estimates a larger volume of high concentrations (Figure 33). The estimated volume is just over 10,000 m$^3$ for the Kriging and IDW interpolations. The least accurate interpolation is Nearest Neighbor and estimates a contaminated soil volume of above 40,000 m$^3$ (Figure 33).

![Figure 31: The estimated mean concentrations of lead in 0.5 m depth intervals in the sampled volume for Kriging (OK), IDW and Nearest Neighbor (NN) interpolations. In the background the standard deviation of the original samples are shown.](image1)

![Figure 32: Estimated volumes in percentage above risk levels for lead interpolations in the sampled volume.](image2)

![Figure 33: Estimated contaminated volumes above risk levels for lead interpolations in the sampled volume. Less sensitive land (400 mg/kg) and sensitive land (50 mg/Kg)](image3)
The difference in level of smoothing between the interpolation methods for lead is also found visually in Figure 34a-c. The few original samples at deeper levels in the natural soil results in that no volume can be estimated in Kriging and IDW. All interpolations show similar areas of highest concentrations.

Figure 34a-c: The results from the different interpolations of lead. The concentration classes are based on the limits in Table 3.

Figure 35 shows the contaminated volume in 3D for the most accurate prediction, the Kriging interpolation. It is only the upper soil layer close to the surface that shows contamination levels above the risk level of lead. The major lead contamination does not exceed the risk level of less sensitive land use nor sensitive land use.

Figure 35: The soil volume estimated to be contaminated with lead according to the Kriging interpolation.
Benzene

Figure 36 shows that the IDW interpolation and Nearest Neighbor interpolation to a large extent follow the distribution of the original samples of benzene concentrations. The Kriging interpolation shows another pattern of lower mean values from the surface down to about 4 m below the ground to increase further down in the soil volume. That shows the difference in a geostatistical interpolation and deterministic.

Figure 36: The estimated mean concentrations of benzene in 0.5 m depth intervals in the sampled volume for Kriging (OK), IDW and Nearest Neighbor (NN) interpolations. In the background the standard deviation of the original samples are shown.

The Kriging and Nearest Neighbor interpolations are able to estimate concentrations in larger volumes than the IDW interpolation (Figure 37). The Kriging and Nearest Neighbor interpolations also estimate larger contaminated volumes, from 160,000 m$^3$ to almost 200,000 m$^3$ (Figure 38). The IDW interpolation estimates the contaminated volume to less than 60,000 m$^3$.

Figure 37: Estimated volumes in percentage above risk levels for benzene interpolations in the sampled volume.

Figure 38: Estimated contaminated volumes above risk levels for benzene interpolations in the sampled volume. Less sensitive land (0.012 mg/kg) and sensitive land (0.04 mg/Kg)
All three interpolations show high benzene concentrations allocated around the old gasworks (Figures 39a-c). There are also traces of contamination by the old dock. The Kriging interpolation estimates high concentrations at deeper levels to a larger extent than can be seen in the Nearest Neighbor interpolation. The IDW interpolation does not estimate the concentrations at deeper levels.

Figure 39a-c: The results from the different interpolations of benzene. The concentration classes are based on the limits in Table 3.

Figure 40 shows the most accurate prediction of benzene contamination, the Kriging interpolation. The prediction shows a large volume of high concentrations and a transportation of benzene to deeper levels in the ground. The contamination is concentrated in close proximity to the approximate locations of the old gasworks and dock. The contamination is estimated to be spread further down in the volume and towards the river (South).

Figure 40: The soil volume estimated to be contaminated with benzene according to the Kriging interpolation.
PAH

As seen in Figure 41 as well as in Figures 42 to 44 the Kriging and IDW interpolations for PAH are very similar. The Kriging interpolation is slightly smoother than the IDW estimation. Neither the Kriging nor the IDW interpolation is able to estimate the whole volume like the Nearest Neighbor interpolation (Figures 42). The Kriging and IDW interpolations estimates similar soil volumes of PAH contamination between 30,000 and 40,000 m³ (Figure 43). The Nearest Neighbor prediction estimates a twice as large volume.

![Figure 41](image)

*Figure 41: The estimated mean concentrations of PAH in 0.5 m depth intervals in the sampled volume for Kriging (OK), IDW and Nearest Neighbor (NN) interpolations. In the background the standard deviation of the original samples are shown.*

![Figure 42](image)

*Figure 42: Estimated volumes in percentage above risk levels for PAH interpolations in the sampled volume.*

![Figure 43](image)

*Figure 43: Estimated contaminated volumes above risk levels for PAH interpolations in the sampled volume. Less sensitive land (1 mg/kg) and sensitive land (10 mg/Kg)*

All interpolations show highest concentrations of PAH allocated at the surface soils around the old gasworks, and lower concentrations at deeper levels (Figure 44a-c). Some elevated levels are also found in proximity to the old dock. There are similarly low concentrations at deeper locations where all methods have been able to estimate the concentrations.
Figure 45 shows the most accurate prediction of PAH contamination, the Kriging interpolation. The prediction of PAH concentrations above the risk level for less sensitive land are in the upper layer of the soil in close proximity to the gasworks. The concentrations decrease to above the risk level for sensitive land at deeper locations and at the old dock.

Figure 44a-c: The results from the different interpolations of PAH. The concentration classes are based on the limits in Table 3.

Figure 45: The soil volume estimated to be contaminated with PAH according to the Kriging interpolation.
5. Discussion

a) Evaluation of 3D Interpolation Models

Three different interpolation methods have been compared; Kriging, IDW, and Nearest Neighbor. The parameters of the Kriging and IDW interpolations were optimized using the results from geostatistical analyses and validations while the Nearest Neighbor does not allow for such optimization.

All three interpolation methods detected the assumed locations of the former gasworks as areas of high risk levels. The Nearest Neighbor method was able to estimate the whole volume of the study area. Yet it was the least accurate, and if the predicted volume is inaccurate it will not help the evaluation of remediation measures. From the RMSE values (Figure 28-30) and since a spatial relation was found, the best method of the evaluated ones are Kriging and secondly the IDW interpolation for all contaminants. Both are based on the parameters from the geostatistical analyses. A similar 3D evaluation of the three methods on lead contamination was performed by Wei et al. (2014). They also found that Kriging was the most accurate method. This is also in line with previous studies on soil contamination data in 2D (Xie et al., 2011).

The findings emphasize the importance of a geostatistical analysis before a useful interpolation can be performed. In most cases the Kriging and IDW methods are able to estimate around 25% of the volume in the study area (Figure 34a, 39a, 44a). That means that the interpolations will help to size up a picture of the contamination situation, especially compared to a situation where the actual sampling points are the only available information.

The evaluated interpolations were restricted to the available methods in one software. Therefore, spline interpolation for example was not evaluated. Some studies suggest that the spline method RST is the optimal interpolation method. One example is the study of Piedade et al. (2014) that evaluated the RST method in three dimensions for lead with a satisfying result. According to Mitáš & Mitášová (1999) RST is the easiest and best interpolation method to use for unexperienced users.

b) Evaluation on Contaminant Differences

Contaminants with different characteristics were studied. From the analyses, their different characteristics induced varying parameters and methods for interpolation. Benzene was distinguished from the other two contaminants having a larger spatial dependence and being spread into the natural soil. This is in line with the characteristics of benzene being a lightweight pollutant easily traveling with the groundwater (Table 1). The benzene interpolations were also the ones with the greatest potential of a valid prediction model. The differences in RMSE among the studied interpolation methods were greatest for benzene compared to the other two contaminants. It gives a clear indication on that Kriging interpolation is a good method for modeling soil contaminants that easily transports down into the ground.

The analyses of lead and PAH showed more similarities than differences. That is presumably due to their similar characteristics of being persistent in the environment and too large for transportation downwards (Table 1). Their persistence is also detected in their short ranges determining the spatial dependence (Table 14). The results show that Kriging and IDW interpolations give equal results for these types of contaminants. Lead has the highest sill of
the three contaminants. The high sill emphasizes the inability of lead to be distributed in the ground resulting in a large variability of high and low concentrations. The estimated contamination of lead is low (below the level of less sensitive land) and concentrated at the surface (Figure 45). According to Steinnes (2013) high concentrations of lead are necessary for transportation downwards indicating that the result is valid.

The results of the analyses show that PAH is not spread extensively in the natural soil. The fill material consists of more organic soils than natural (Table 10). A high organic content is important for transportation of PAH (Abdel-Shafy & Mansour, 2016). Therefore, it is reasonable to believe that the estimated contamination levels at deeper locations in the natural soil are valid.

According to the RMSE values the interpolation results of PAH might be questioned. The standard variation of the PAH samples (Table 7) is smaller than the RMSE values (Figure 30). That means that the variation of PAH might not be captured in the interpolation. The standard variation of the benzene samples are a lot larger than the RMSE values from both Kriging and IDW, the same goes for lead. Lead and benzene are both on the extremes, lead is a very persistent contaminant and benzene a very volatile one. PAH however, is more intermediate. PAH is persistent but not to the same extent as lead. Noticeably, it is more difficult to predict the distribution of a more varying contaminant (Xie et al., 2011).

The lower concentrations of lead and PAH in the natural soil (Figure 26a and c) suggests that the contaminants have not been transported to a large extent to the natural soil. Therefore, samples in the natural soil could be excluded to speed up the process when these are interpolated.

c) Evaluation on Methods for 3D Interpolation with GIS

To keep the contamination data within a GIS-environment increases the possibilities for further analyses. Compared to a 3D modeling software a GIS keeps the spatial attributes and relationships. Information that is important for remediation decisions and other conclusions that should be drawn from the data.

The ultimate solution for a project with risk assessment of soil contamination would be to work within the GIS-environment from start to end with planning, sampling, analysis and describing the situation, to the remediation measure. That could give a more effective work process as well as ease the work for people with less GIS- and computer skills. In ArcGIS, as Sweco use, many of these steps are possible today. With further work of the suggested prototype for 3D interpolation (Figures 7-8) the possibility exists to perform 3D interpolation in ArcGIS. In reality, this is not an optimal solution. The optimal solution has a wide range of interpolation techniques to choose from since different sampling densities and contaminants might need different approaches. Instead the technique of integrating 3D volumes in GISs needs to be further developed before a complete work process including 3D interpolation within a GIS is feasible in a comprehensive way.

GRASS GIS was suggested as software for 3D interpolation that is both a GIS and can handle 3D volumes. The study of Neteler (2001) suggests that the methods in GRASS are good for volume interpolation of soil contaminants with the strength of seamless integration into a GIS. However, GRASS lacks the streamlined approach from sampling to visualization. These are important qualities in a method suitable for larger projects for contaminated sites. The largest
downside with GRASS is the lacking possibility of Kriging interpolation suggested to be the most accurate method. Programming and additional open source alternatives might be useful to overcome these issues and still use GRASS.

MVS and other 3D modeling software are certainly alternatives for robust and reliable 3D models. The downside is the high license cost that might not increase the final outcome of the remediation measure distinctly from more simple software. Furthermore, these are not incorporated in any GIS and need time consuming data processing before performance. They also need a certain skill of data processing to be used. On the positive side, MVS performs the geostatistical analyses with optimal solutions in an automatic way. SADA is free but has the same problem with data processing as other more sophisticated 3D software. However, the interface of SADA is easy to use and ordered in a logic manner for both beginners and experts in data processing. In SADA geostatistical analysis can be performed within the user interface giving the user more control on the final outcome. Although compared to MVS that can perform optimal interpolations without integration from the user, geoscientific knowledge is needed in SADA.

According to Mitáš & Mitášová (1999) methods have been presented which are capable of treatment of multi-dimensional data. However, the current GIS computational infrastructure does not effectively support a wide application of multi-dimensional modeling. This seems to be valid today as well. Until the technique is further developed or other methods exists the proposed method for 3D interpolation is to perform the geostatistical analysis and interpolations in another software, as SADA or MVS, and then transfer the data back into a GIS again to make use of the pros a GIS comes with. The method for geostatistical analyses and interpolation performed in this study is too complex for a general contamination project since too many software is involved.

**d) Reliability of the Results and Future Research**

The results suggest that soil contamination prediction in 3D is possible to different extents and certain degree of reliability. However, the sampling density in the horizontal plane is too coarse to find any spatial dependence. Or possibly, the study area is too small to detect the spatial dependence. That makes the result more unreliable than if a clear spatial dependence was found also in the horizontal plane. Although, one might suggests, as in the study, that the relationship is isotropic and the spatial dependence very small. That means a fine layering and grid spacing must be used to interpolate in 3D. Consequently, that increases the computational complexity especially working within a GIS where each grid point is stored as a separate unit.

All parameters in the interpolations have not been optimized. Grid size and included samples are examples of non-optimized parameters. However, the sampling density does not allow for a finer grid. There is a possibility that the number of included samples for each estimated point could have an effect on the results. It is something that could have been further studied in future research. Furthermore, since no spatial dependence was found in the horizontal plane three different lengths of search radius were tested for Kriging and IDW interpolations. The optimal search radius of these three were used, although it can still be another search radius with another length not investigated that is more suitable.

Another weakness of the study is the interpolations at deeper levels. Firstly, the numbers of samples in natural soil at levels deeper than about 2.5 m are less than half of the samples in the fill material. Still, the natural soil is interpolated as a separate part although the samples might be too few for interpolation.
Secondly, the division in natural soil and fill material is performed on the mean depth of the fill material. Since the depth in reality is varying, samples in fill material has been interpolated with natural soil parameters and vice versa. This is a limitation in the software used which might be solvable in more solid 3D modeling software. For more reliable results more samples at deeper levels are necessary as well as a higher sampling density in the horizontal plane.

An additional suggestion for future research is to compare the 3D volume interpolations with 2D interpolations at surfaces on different depths. If the result is similar, that would mean an easier interpolation approach where the whole process can be performed in a GIS.

The back transformation of logarithmic transformed with exponentiation might exaggerate the data values (Goovaerts, 1997). The exaggeration affect can in the future be mitigated with the use of an unbiased back transformation (Deutsch & Journel, 1998). Also, the normal score transformation of the data can have an effect on the result. In this case, the back transformation was set to keeping the original minimum and maximum from the samples in the interpolated values. However, it is the exceeding of the two risk levels that is important in projects for contaminated land. Small differences as transformation errors would not affect the final outcome of the risk levels.

The results in the study are validated with RMSE values from another sampling dataset. That means that these samples are not located at the same spot as the interpolated points. The distribution of the validation points might also have an effect. The outcomes of the interpolations had volumes not estimated. That means that a varying numbers of validation points were included in the validation. Also, to state with confidence which method that is the best, even more types of validations are desirable.

All in all, every model is just an estimate about the real world situation. There is not only one model that can describe the whole reality. Finally, the approach is based on the assumption that the samples used are representative in themselves, this is not always true (Houlding, 2000).

6. Conclusion

Volume interpolation of soil pollutants has a high potential to add knowledge and insight into the contamination situation at a site. The interpolations performed here were able to detect differences regarding the distribution patterns of the three contaminants. Estimates of volumes above risk levels could be computed, areas of high risk have been detected as well as the transportation down in the ground. However, no spatial dependence in the horizontal plane was found making the results more unreliable. A higher sampling density is necessary for a more solid result.

Lead, benzene, and PAH all show the greatest potential of interpolation with Kriging. Nevertheless, for lead and PAH the IDW interpolations show similar potentials. The different characteristics of the three contaminants resulted in different optimal parameters for the interpolations. A major detected difference was the distribution in the ground which was notable for benzene but not for the other two contaminants. Mobile contaminants as benzene should be interpolated with different parameters than the more immobile contaminants lead and PAH.
Benzene showed the greatest potential of interpolating 3D volumes. It had a high accuracy and the whole volume in the study area could be interpolated. Lead showed a good potential of interpolating in the fill material of the soil. For a reliable interpolation in the natural soil more samples are needed. PAH showed the least potential of volume interpolation with a low accuracy of the interpolation and only parts of the whole volume of the study area could be interpolated.

Based on the results a complete, accurate and effective interpolation of 3D volumes is today difficult to perform in a GIS-environment alone. It is therefore suggested to combine the work with contamination data in a GIS with more solid 3D modeling. The geostatistical analysis is an important part in the interpolation since the method not based on geostatistics was least accurate. Geostatistical analysis of 3D data is difficult to perform within a GIS and additional software is needed. The effectiveness is higher in software as MVS which optimize the parameters within the software while software as SADA gives more control to the user.

A three dimensional visualization of the contamination may increase the understanding and increase the foundation for remediation measures. Nevertheless, one must be aware of that it is a model and not the real situation.
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