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SIMULATION OF SHIP YAWING

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SIMULATION OF SHIP YAWING

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APPENDIX - PROGRAM LISTINGS

1. INTRODUCTION

Simulations of manoeuvring trials and simulations of yaws performed by a yaw regulator are presented in this report. The simulations are performed on the computer UNIVAC 1108 by use of the interactive program SIMNON (see Elmqvist (1975)). The ship model used describes a 350 000 tdw tanker of Kockums' design.

The yaw regulator consists of different discrete, fixed gain PID-regulators. The reference values used by the yaw regulator are the yaw rate and the heading angle. Full-scale experiments on 255 000 tdw tankers with modified yaw regulators are described in Källström (1974) and (1975) where also straight course keeping experiments are presented.

Simulations of straight course keeping by different autopilots are discussed in Aspernäs and Foisack (1975), Aspernäs and Källström (1975) and Källström (1976).

Listings of the program used are given in the Appendix.

2. SHIP STEERING DYNAMICS

The following model, which describes a 350 000 tdw tanker of Kockums design, is used in the simulations (cf. Norrbin (1970)):

$$\dot{\delta} = -\frac{1}{T_r} \delta + \frac{1}{T_r \cdot CRG} \delta_c$$

$$|\dot{\delta}| \leq \frac{1}{CRG} \delta_{lim}$$

$$\begin{aligned} \left(1 - x_u''\right) \dot{u} &= \frac{1}{L} x_u'' |u| u |u| + \frac{1}{L} x_{uu}'' u^2 + \left(1 + x_{vr}''\right) v r + \\ &+ L \left(x_{rr}'' + x_G'' \right) r^2 + \frac{1}{gL^2} x_{uvv}'' |v| u v^2 |v| + \frac{1}{L} x_u'' |u| \delta \delta u |u| \delta^2 + \\ &+ (1-t) (T/m) - F_w \cos \left(\frac{\alpha}{CRG} - \psi \right) \end{aligned}$$

$$\begin{aligned} \left(1 - y_v''\right) \dot{v} &= \left(y_{ru}'' - 1\right) r u + \frac{1}{\sqrt{gL}} y_{ru}'' |u| r u |u| + \\ &+ \frac{1}{L} y_u'' |u| v |u| v + \frac{1}{\sqrt{gL^3}} y_u'' |u| v u |u| v + \frac{1}{L} y_v'' |v| v |v| + \\ &+ y_r'' |v| r |v| + y_r'' |r| v |r| v + \frac{1}{L} y_{uu\delta}'' u^2 \delta + \frac{1}{L} y_u'' |u| \delta u |u| \delta + \\ &+ y_{T\delta}'' (T/m) \delta + k_{TY} (T/m) - F_w \sin \left(\frac{\alpha}{CRG} - \psi \right) + w_1 \end{aligned}$$

$$\begin{aligned} \left(k_{zz}''^2 - N_r''\right) \dot{r} &= \frac{1}{L} \left(N_r'' |u| - x_G''\right) r |u| + \frac{1}{\sqrt{gL^3}} N_{ru}'' |u| r u |u| + \\ &+ \frac{1}{L^2} N_{uv}'' u v + \frac{1}{\sqrt{gL^5}} N_u'' |u| v u |u| v + \frac{1}{L^2} N_v'' |v| v |v| + N_r'' |r| r |r| + \\ &+ \frac{1}{L} N_r'' |v| r |v| + \frac{1}{L} N_r'' |r| v |r| v + \frac{1}{L^2} N_{uu\delta}'' u^2 \delta + \frac{1}{L^2} N_u'' |u| \delta u |u| \delta + \\ &+ \frac{1}{L} N_{T\delta}'' (T/m) \delta + \frac{1}{L} k_{TN} (T/m) + \frac{1}{L^2} F_w \ell_w \sin \left(\frac{\alpha}{CRG} - \psi \right) + w_2 \end{aligned}$$

$$\begin{aligned}
 \dot{\psi} &= r \\
 \dot{x}_o &= u \cos \psi - v \sin \psi \\
 \dot{y}_o &= u \sin \psi + v \cos \psi
 \end{aligned} \tag{2.1}$$

It is assumed that the number of propeller revolutions n is kept constant to the value 87.6 rpm by a regulator during all the simulations. The propeller thrust per mass unit (T/m) is computed by:

$$\begin{aligned}
 J &= \frac{u(1-w) \cdot 60}{n D} \\
 J' &= \frac{J}{\sqrt{1+J^2}} \\
 K_T' &= -0.33 \cdot J'^2 - 0.38 \cdot J' + 0.35 \\
 T &= K_T' \left(\frac{J}{J'} \right)^2 \rho_s n^2 D^4 / 3600 \\
 (T/m) &= \frac{T}{\rho_s \nabla}
 \end{aligned} \tag{2.2}$$

Notice that the terms $(T/m)\delta$ in (2.1) always are limited by the value $(T/m)_0\delta$, where $(T/m)_0$ is computed from (2.2) with the stationary forward speed corresponding to $n = 87.6$ rpm.

Input signal:

rudder command (or rudder servo position)	δ_c [deg]
--	------------------

States:

rudder angle	δ [rad]
forward velocity	u [m/s]
sway velocity	v [m/s]

yaw rate	r [rad/s]
heading angle	ψ [rad]
x-coordinate (system fixed earth)	x_o [m]
y-coordinate (system fixed earth)	y_o [m]

Disturbances:

sway acceleration disturbance	w_1 [m/s^2]
disturbance of yaw angle acceleration	w_2 [rad/s^2]

Other notations:

time constant of rudder servo	T_r [s]
limit of rudder rate	δ_{lim} [deg/s]
length of ship	L [m]
acceleration of gravity	g [m/s^2]
propeller thrust per mass unit	T/m [m/s^2]
number of propeller revolutions	n [rpm]
wind force per mass unit	F_w [m/s^2]
lever arm of wind force	ℓ_w [m]
angle of wind direction	α [deg]
conversion factor rad - deg	CRG [deg]

The following parameter values are used:

T_r	=	5	s
δ_{lim}	=	2.32	deg/s
L	=	350	m
g	=	9.80665	m/s^2
n	=	87.6	rpm
ℓ_w	=	25	m
CRG	=	57.2958	deg

The values of the other parameters are given in Dyne and Trägårdh (1975). Two different load conditions are considered corresponding to the mean draught $T = 22.3$ m (full load, forward and aft draught equal to 22.3 m) and $T = 10.5$ m (ballast, forward and aft draught equal to

9.0 m and 12.0 m, resp.). The forward speed u which corresponds to $n = 87.6$ rpm is equal to 15.8 knots when $T = 22.3$ m and equal to 17.25 knots when $T = 10.5$ m. These two values of the forward speed u are used as initial values in all the simulations. If the model (2.1) and (2.2) is linearized, the following transfer function relating the yaw rate r to the rudder angle δ is obtained:

$$G(s) = \frac{K (1 + sT_3)}{(1 + sT_1)(1 + sT_2)} \quad (2.3)$$

If the forward speed u is assumed to be constant and equal to 15.8 knots, then the following parameter values of (2.3) are obtained when $T = 22.3$ m:

$$\begin{aligned} K &= 0.0161 \text{ l/s} \\ T_1 &= -110.1 \text{ s} \\ T_2 &= 18.3 \text{ s} \\ T_3 &= 54.3 \text{ s} \end{aligned} \quad (2.4)$$

The corresponding values when $u = 17.25$ knots and $T = 10.5$ m are:

$$\begin{aligned} K &= 0.0707 \text{ l/s} \\ T_1 &= -337.1 \text{ s} \\ T_2 &= 19.9 \text{ s} \\ T_3 &= 69.5 \text{ s} \end{aligned} \quad (2.5)$$

Notice that the sign of the rudder angle in the model is chosen in such a way that a positive rudder angle (port rudder) gives a negative yaw rate (port yaw). From (2.4) and (2.5) it can be concluded that the tanker is unstable in full load condition as well as in ballast condition.

The disturbance signals w_1 and w_2 are obtained as white, gaussian noise filtered through a low pass filter. The covariance matrix of the white noise vector, which

generates w_1 and w_2 , is

$$R_w = \begin{pmatrix} 10^{-10} & 0 \\ 0 & 10^{-12} \end{pmatrix} \quad (2.6)$$

The measured outputs from the model (2.1) and (2.2) are

$$r_m = \bar{r} + e_1, \quad \bar{r} = CRG \cdot r$$

$$\psi_m = \bar{\psi} + e_2, \quad \bar{\psi} = CRG \cdot \psi$$

where e_1 and e_2 are white, gaussian measurement noise with covariance matrix

$$R_e = \begin{pmatrix} \sigma_r^2 & 0 \\ 0 & 0.01 \end{pmatrix} \quad (2.7)$$

where $\sigma_r = 0.01$ or 0.02 deg/s.

The measured yaw rate r_m [deg/s] and the measured heading ψ_m [deg] are used by the yaw regulator.

Three different cases of disturbances are used in the simulations:

1. No disturbances: $F_w = 0$, $w_1 = w_2 = e_1 = e_2 = 0$.
2. Constant wind force disturbance: $F_w = 0.002 \text{ m/s}^2$,
 $w_1 = w_2 = e_1 = e_2 = 0$.
3. Stochastic disturbances: $F_w = 0.002 \text{ m/s}^2$, R_w and R_e
according to (2.6) and (2.7), resp.

It should be pointed out that the model of the disturbances is extremely simplified. A more realistic approach is given in Berlekomm, Trägårdh and Dellhag (1975).

The program of the ship model, TANK1, is given in the Appendix.

3. YAW REGULATOR

A yaw performed by the yaw regulator consists of four different phases, viz. the initial phase (phase 1), the phase of constant yaw rate (phase 2), the checking rudder phase (phase 3) and the terminating phase (phase 4). However, if the requested heading change $\Delta\psi_{ref}$ is small, one or more of the phases may be skipped. The measurement signals used by the yaw regulator are the yaw rate r_m and the heading ψ_m , and the reference values used are the requested yaw rate r_{ref} and the new requested heading ψ_{ref} .

Modified discrete, fixed gain PID-regulators are used in the different phases (note that $n = 0, 1, 2, \dots$):

Phase 1:

$$\delta_c(nT_s) = k_4 [r_m(nT_s) - r_{ref}] + \bar{\delta}_c$$

$$\left| k_4 [r_m(nT_s) - r_{ref}] \right| \leq \left| c_1 r_{ref} \right|$$

Phase 2:

$$\delta_c(nT_s) = k_5 [r_m(nT_s) - r_{ref}] + k_6 T_s \sum_{i=0}^n [r_m(iT_s) - r_{ref}] + \bar{\delta}_c$$

Phase 3:

$$\delta_c(nT_s) = k_7 [\psi_m(nT_s) - \psi_{ref}] + k_8 r_m(nT_s)$$

$$\left| \delta_c(nT_s) \right| \leq \left| c_3 r_{ref} \right|$$

Phase 4:

$$\begin{aligned} \delta_c(nT_s) = & k_1 [\psi_m(nT_s) - \psi_{ref}] + k_2 r_m(nT_s) + \\ & + k_3 T_s \sum_{i=0}^n [\psi_m(iT_s) - \psi_{ref}] \end{aligned}$$

The sampling interval T_s is always equal to 10 s. The moving average $\bar{\delta}_c$ of the rudder commands δ_c is only updated during phase 4:

$$\bar{\delta}_c((k+1)T_s) = \bar{\delta}_c(kT_s) + \left(\frac{1-\gamma}{k+1} + \gamma\right)(\delta_c(kT_s) - \bar{\delta}_c(kT_s)),$$

$$k = 0, 1, 2, \dots$$

$$\bar{\delta}_c(0) = 0$$

The computation of $\bar{\delta}_c$ is initialized every time phase 4 is entered. The value of γ is always equal to 0.05.

The conditions to jump from one phase to another read (notice that phase 4 also is used for straight course keeping):

Phase 4 → phase 1:

$$\Delta\psi_{ref} > \psi_{max}$$

Phase 1 → phase 2:

$$r_{ref} > 0 \text{ and } r_m - r_{ref} > -\varepsilon_1$$

or

$$r_{ref} < 0 \text{ and } r_m - r_{ref} < \varepsilon_1$$

or

$$(\text{time in phase 1}) > T_1$$

Phase 1 or 2 → 3:

$$\psi_m - \psi_{ref} < 0 \text{ and } -c_2 r_m < \psi_m - \psi_{ref}$$

or

$$\psi_m - \psi_{ref} > 0 \text{ and } -c_2 r_m > \psi_m - \psi_{ref}$$

Phase 3 → 4:

$$|r_m| < \varepsilon_2$$

or

$$r_{ref} > 0 \text{ and } \psi_m - \psi_{ref} > -\varepsilon_3$$

or

$$r_{ref} < 0 \text{ and } \psi_m - \psi_{ref} < \varepsilon_3$$

or

$$(\text{time in phase 3}) > T_3$$

Two sets of yaw regulator parameters are used. The first set contains rather large gain factors:

$k_1 = 5$	$\varepsilon_1 = 0 \text{ deg/s}$
$k_2 = 200 \text{ s}$	$\varepsilon_2 = 0.02 \text{ deg/s}$
$k_3 = 0.005 \text{ 1/s}$	$\varepsilon_3 = 1 \text{ deg}$
$k_4 = 200 \text{ s}$	$c_1 = 60 \text{ s}$
$k_5 = 200 \text{ s}$	$c_2 = 50 \text{ s}$
$k_6 = 8$	$c_3 = 60 \text{ s}$
$k_7 = 2$	$T_1 = 30 \text{ s}$
$k_8 = 200 \text{ s}$	$T_3 = 80 \text{ s}$
	$\psi_{\max} = 2.5 \text{ deg}$

The values of the parameters k_1-k_8 are decreased in the second set:

$k_1 = 2.5$	$k_5 = 100 \text{ s}$
$k_2 = 100 \text{ s}$	$k_6 = 4$
$k_3 = 0.0025 \text{ 1/s}$	$k_7 = 1$
$k_4 = 100 \text{ s}$	$k_8 = 100 \text{ s}$

The program of the yaw regulator, YAW1, is given in the Appendix. A special indicator M_y is used to describe the actual yaw phase, i.e. $M_y = 1,2,3$ corresponds to phase 1,2,3, resp. Notice, however, that phase 4 is indicated by $M_y = 0$.

4. SIMULATION OF MANOEUVRING TRIALS

Simulations of turning circle manoeuvres, spiral tests and zig-zag tests are presented in this chapter. No disturbances are applied, i.e.

$$F_w = 0, \quad w_1 = w_2 = e_1 = e_2 = 0.$$

Plots of the simulations are shown in Figs 4.1 - 4.8. The total speed

$$v = \sqrt{u^2 + v^2}$$

and the angle of drift

$$\beta = -\arctg(v/u)$$

are shown in some of the figures. The plots may be compared to the simulations in SSPA (1974), where almost the same ship model as in this report was used.

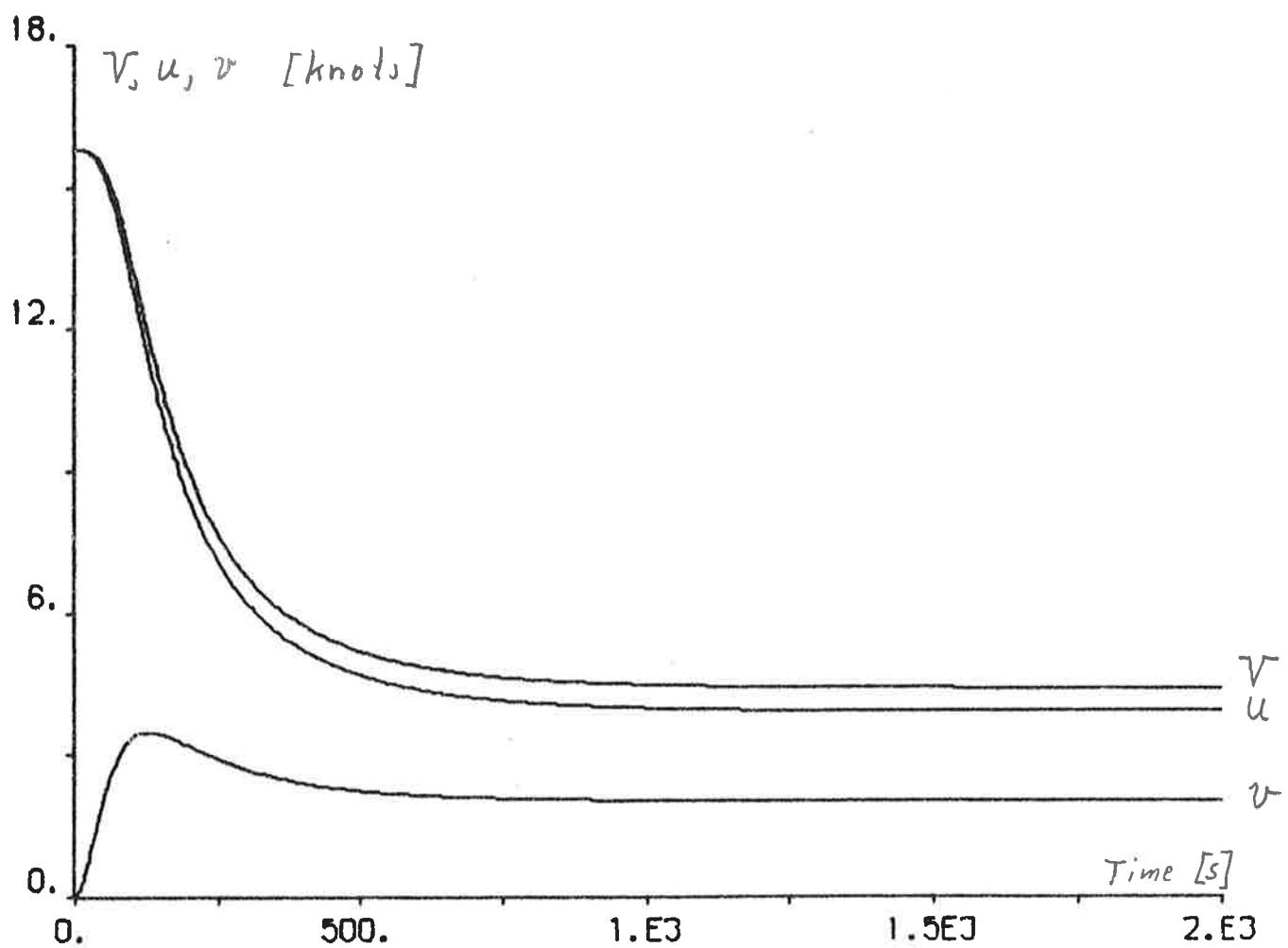
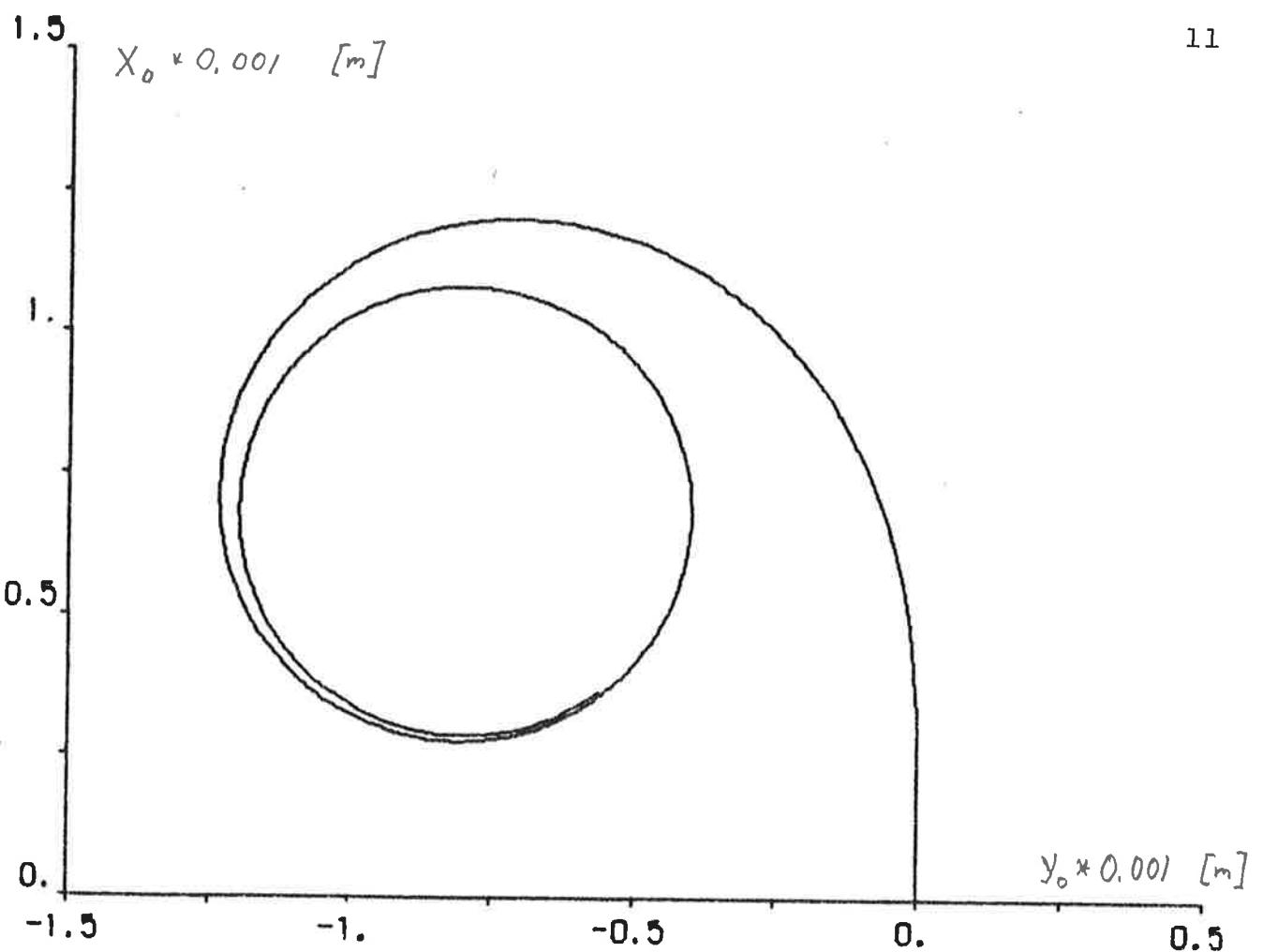


Fig. 4.1 a - Turning circle manoeuvre: $T = 22.3 \text{ m}$, $\delta_C = 35 \text{ deg}$.

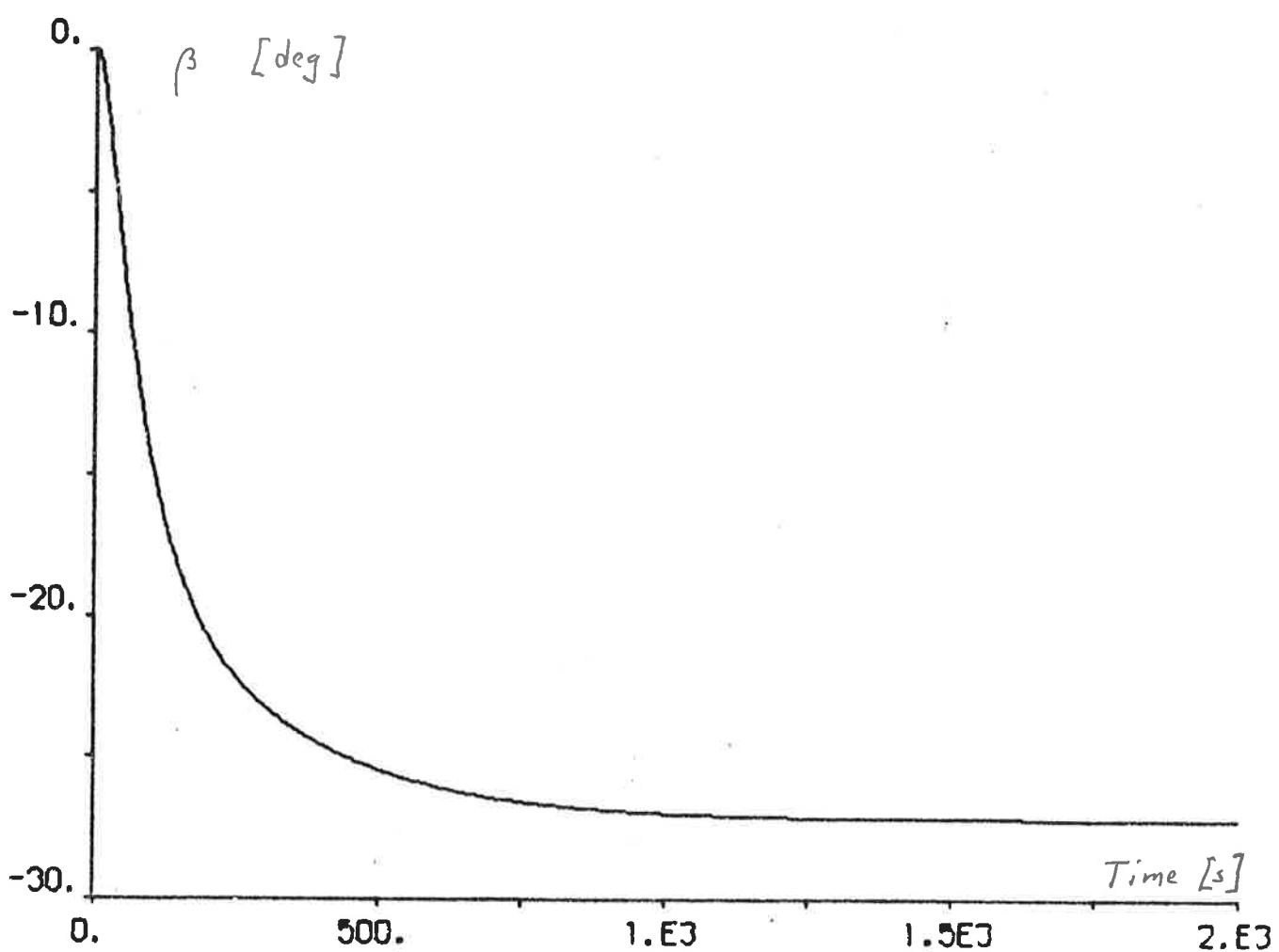
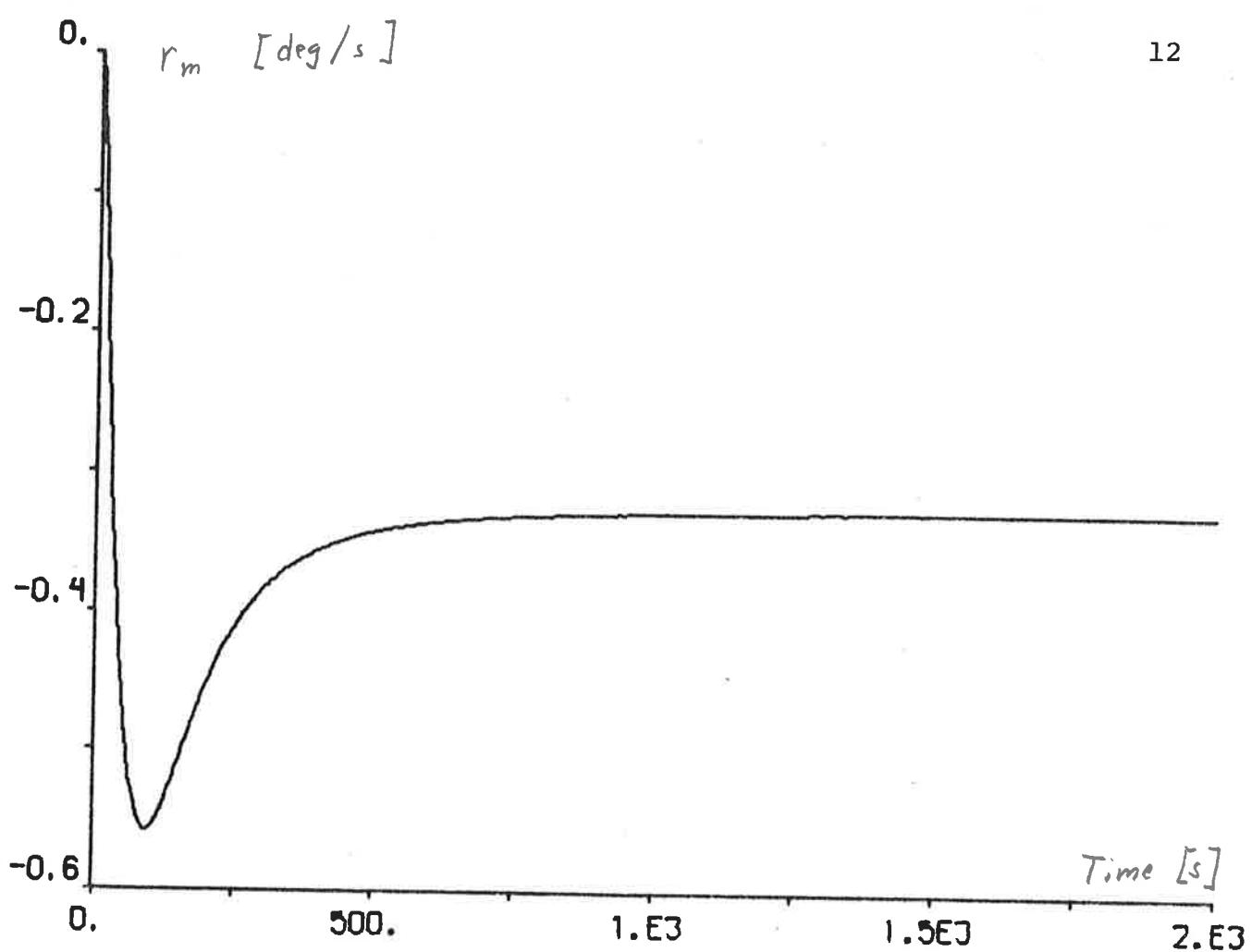


Fig. 4.1 b

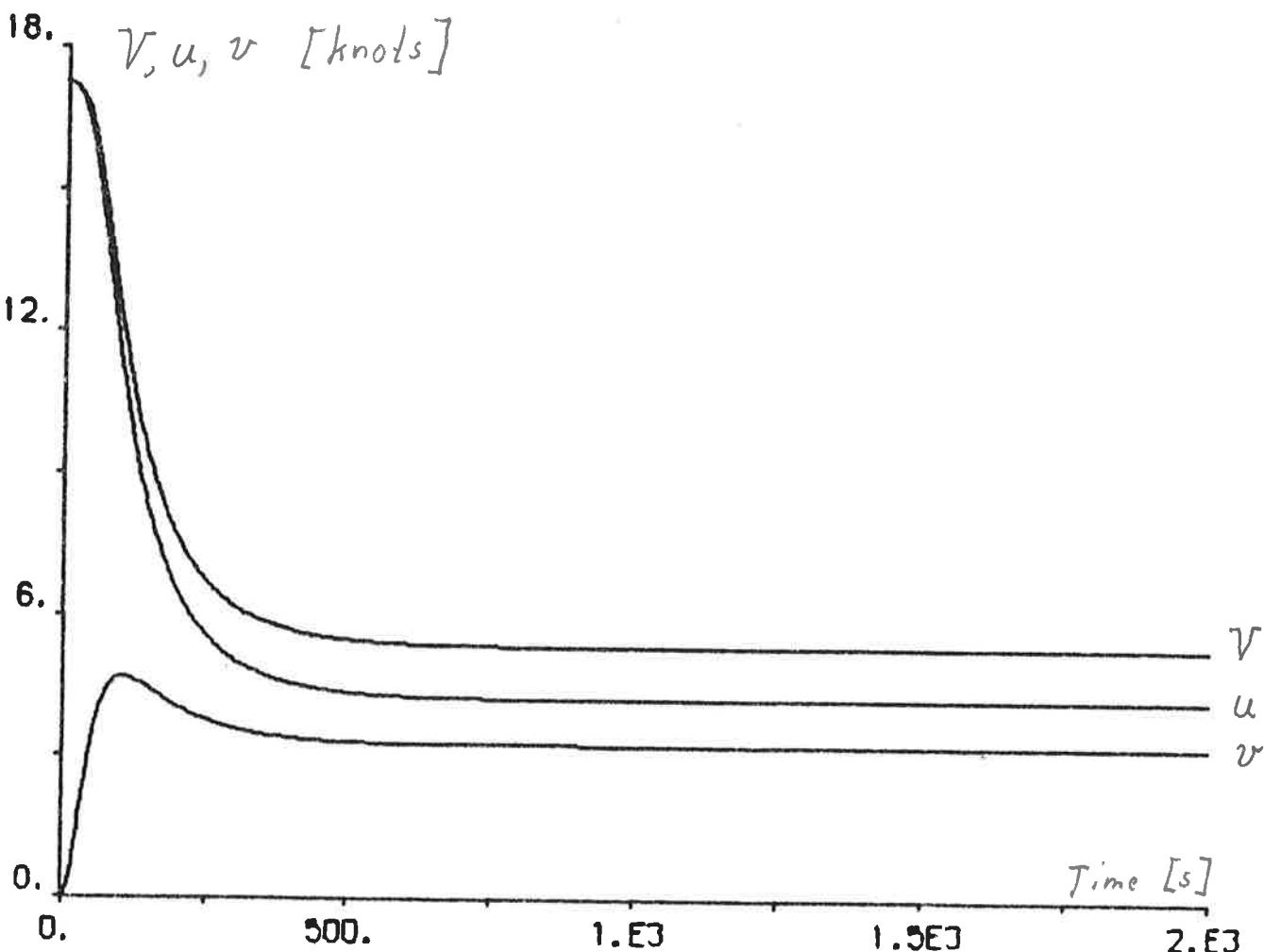
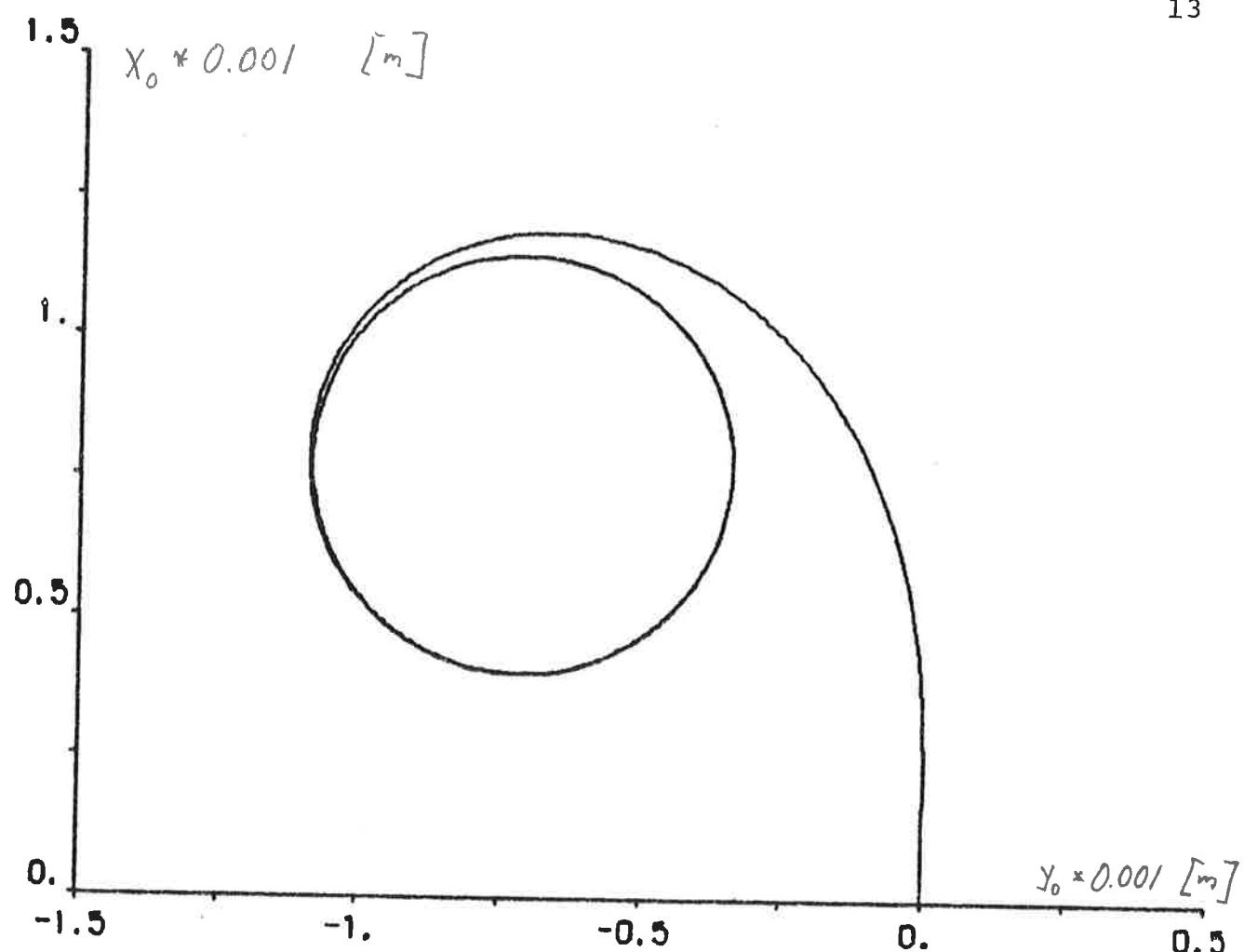


Fig. 4.2 a - Turning circle manoeuvre: $T = 10.5 \text{ m}$, $\delta_c = 35 \text{ deg}$.

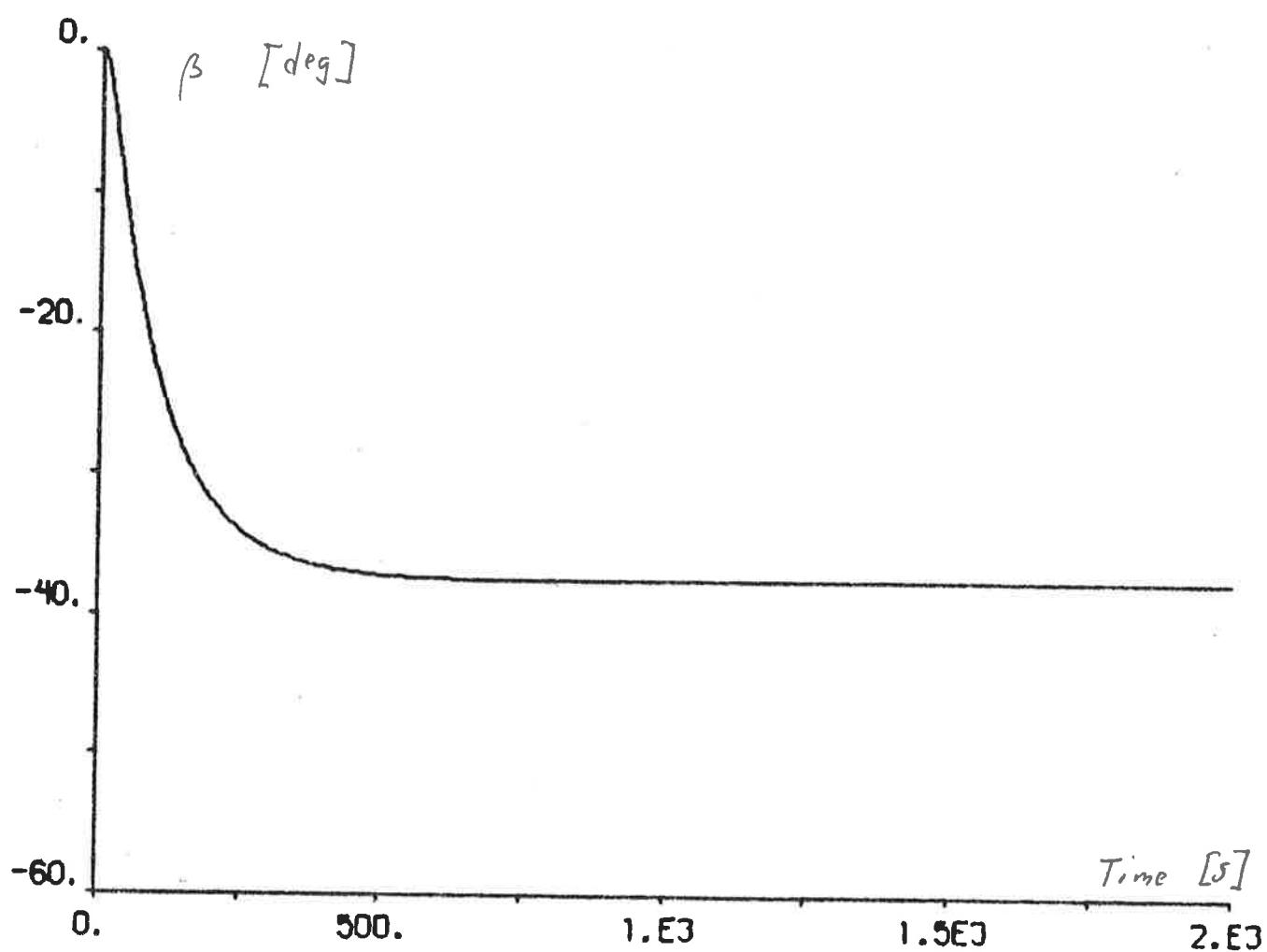
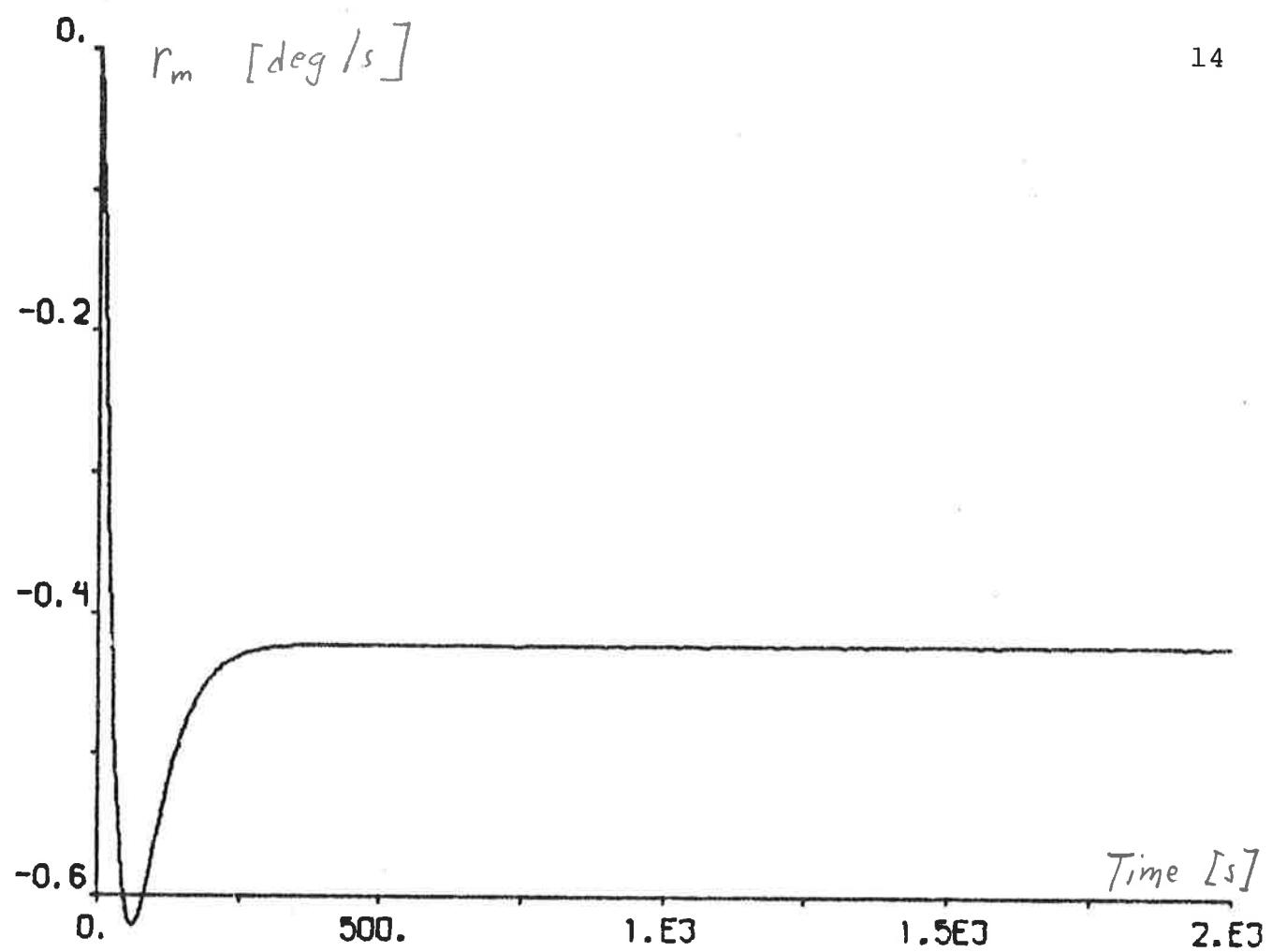


Fig. 4.2 b

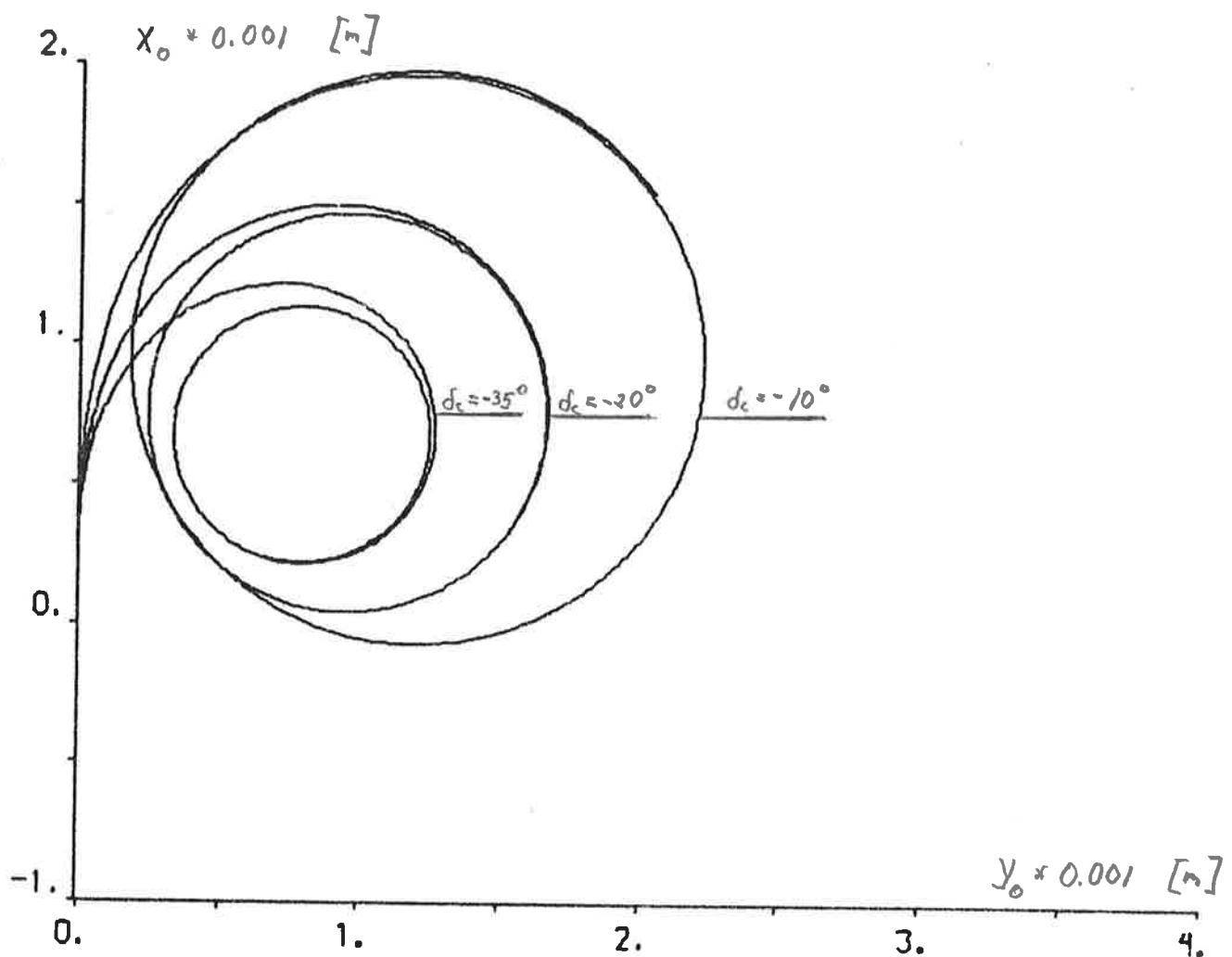


Fig. 4.3 - Turning circle manoeuvres: $T = 22.3$ m, $\delta_c = -35, -20, -10$ deg.

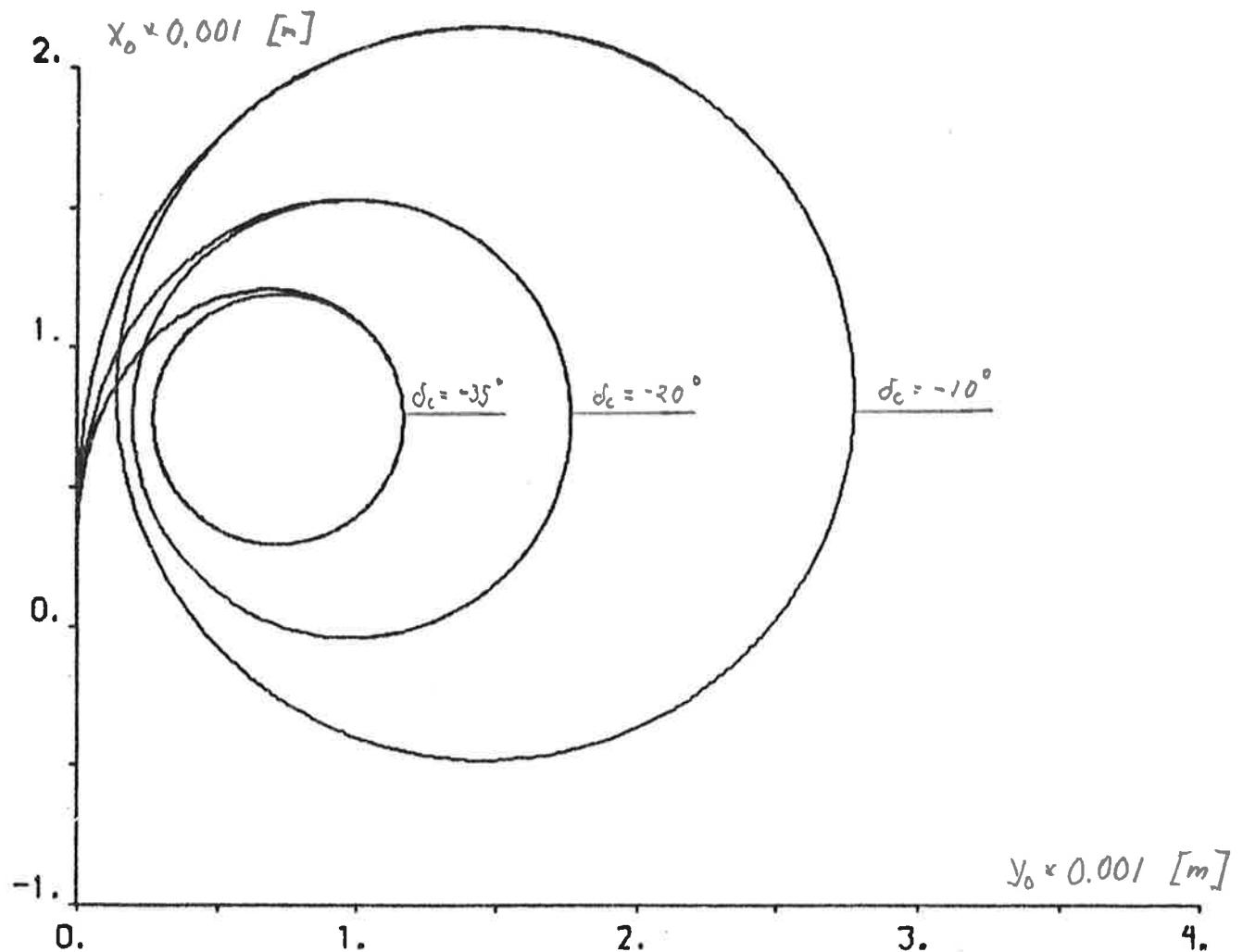


Fig. 4.4 - Turning circle manoeuvres: $T = 10.5$ m,
 $\delta_c = -35, -20, -10$ deg.

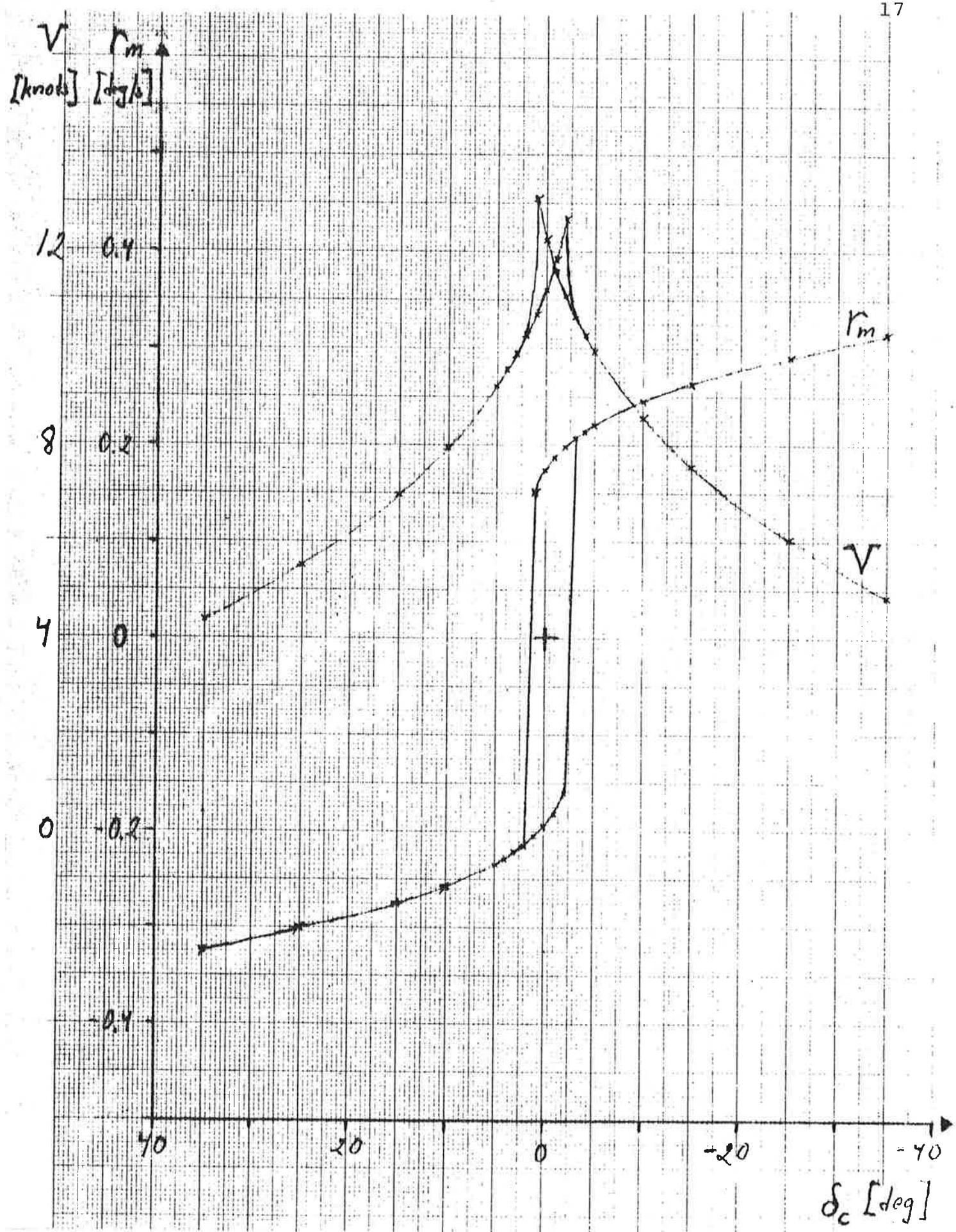


Fig. 4.5 - Spiral test: $T = 22.3$ m.

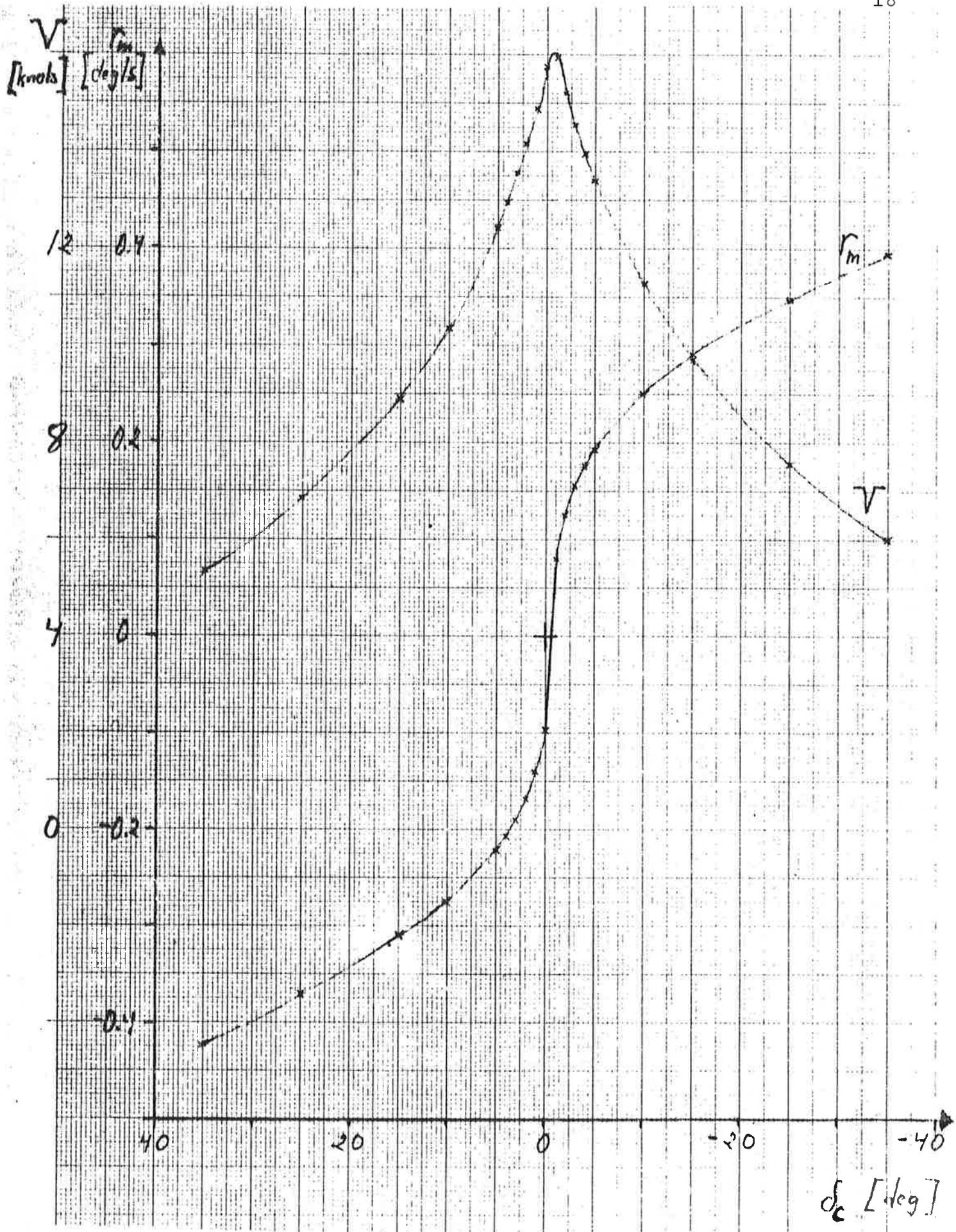


Fig. 4.6 - Spiral test: $T = 10.5$ m.

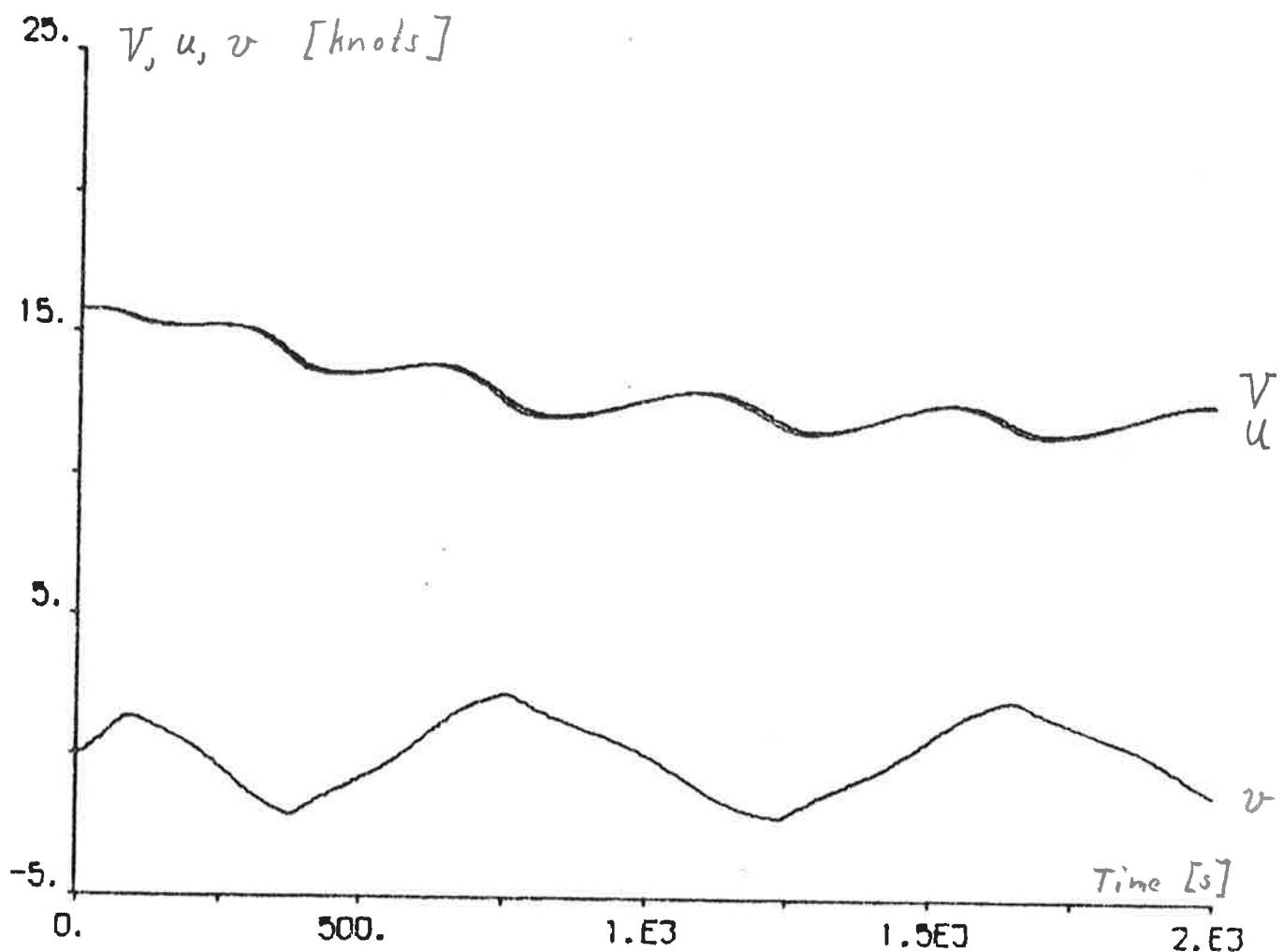
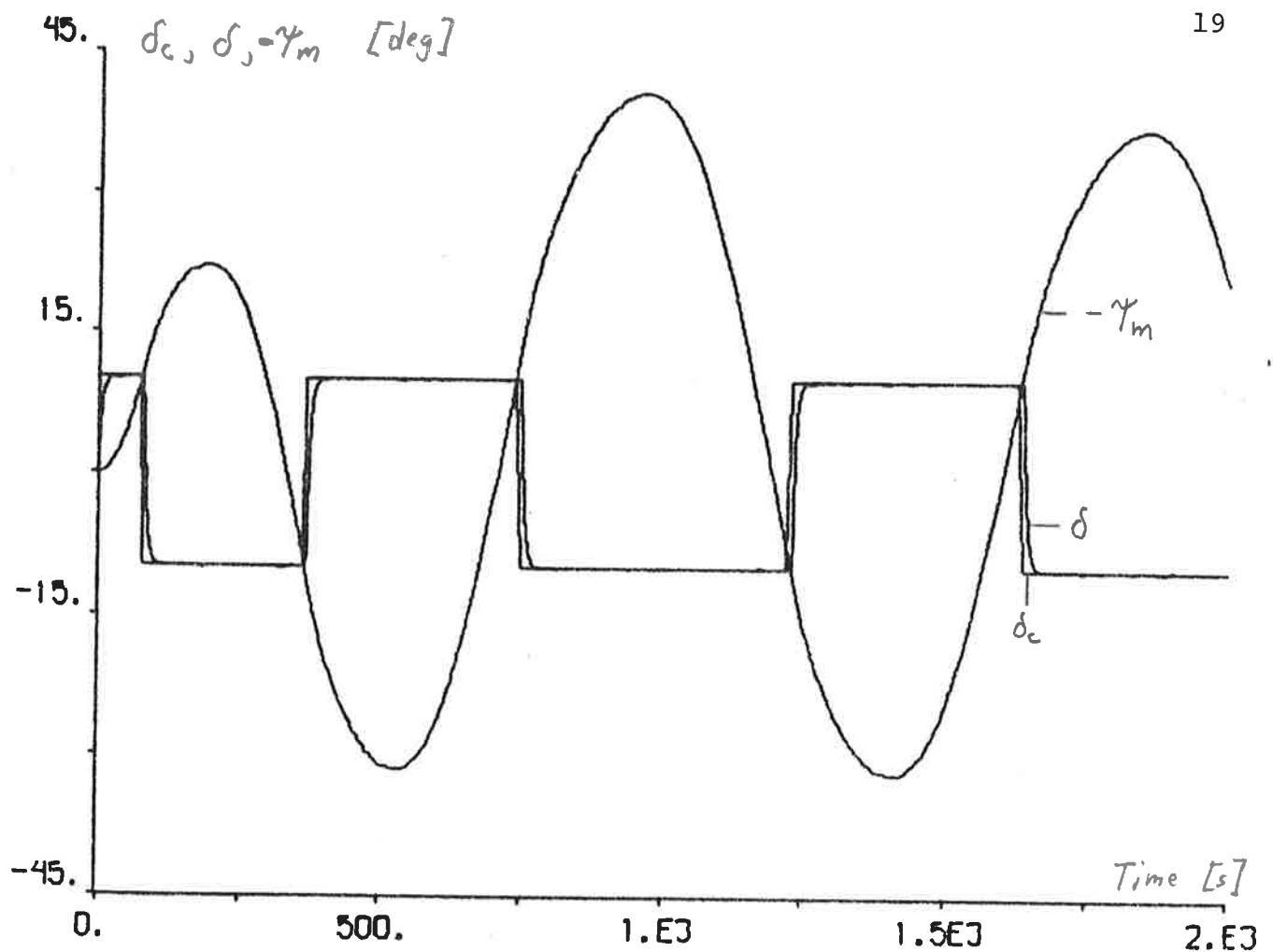


Fig. 4.7 a - Zig-zag test ($10^\circ/10^\circ$): $T = 22.3$ m.

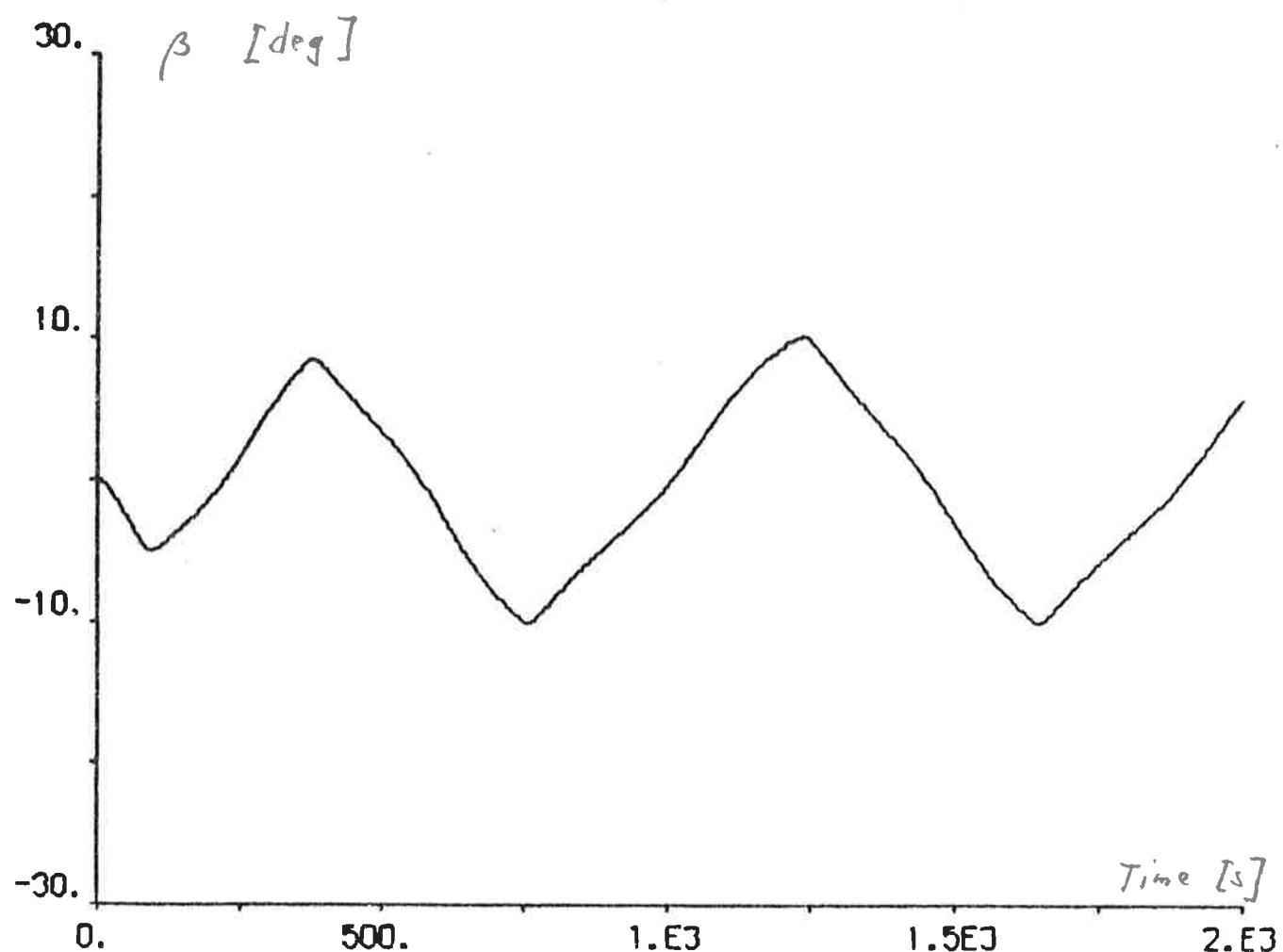
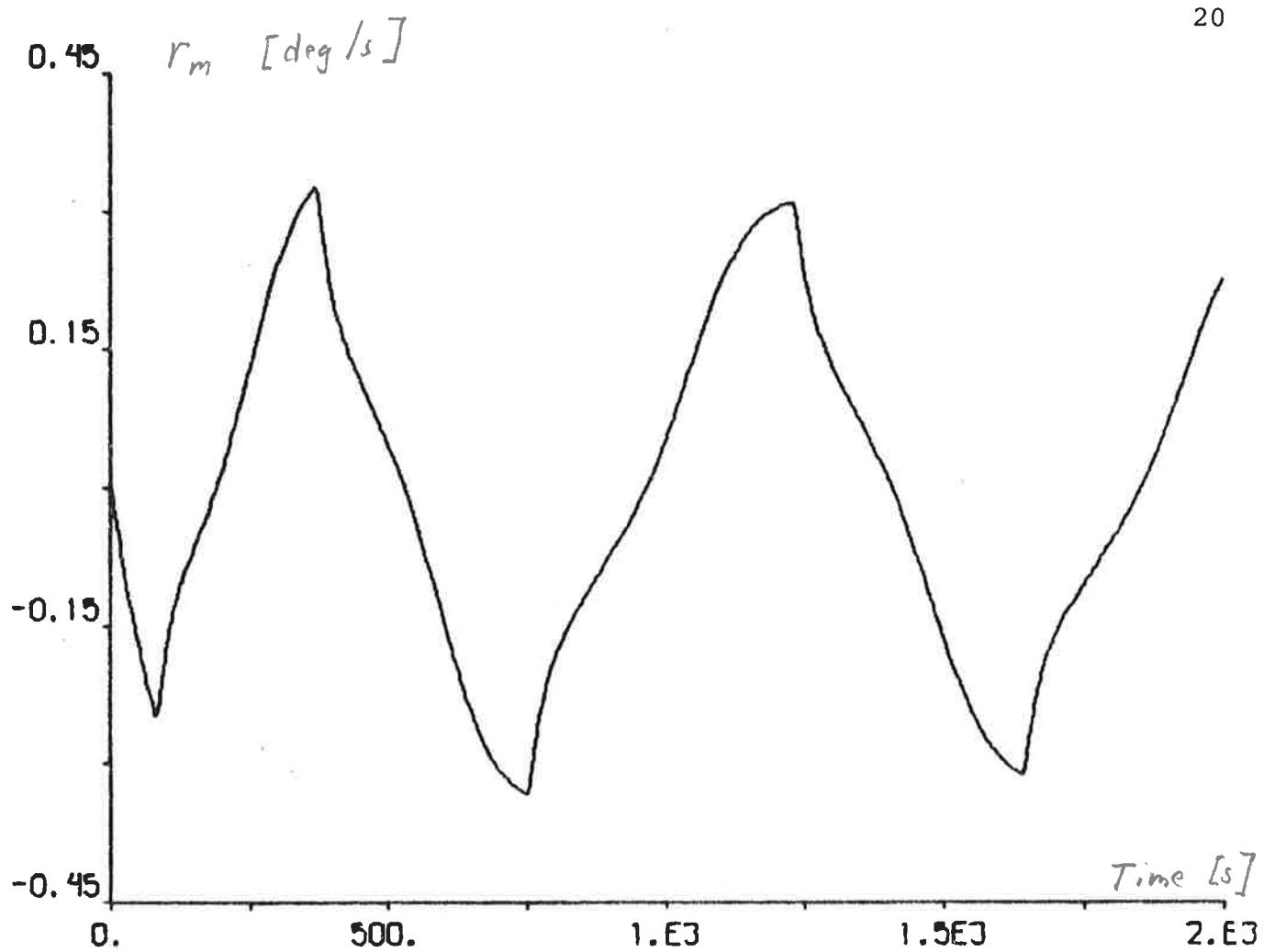


Fig. 4.7 b

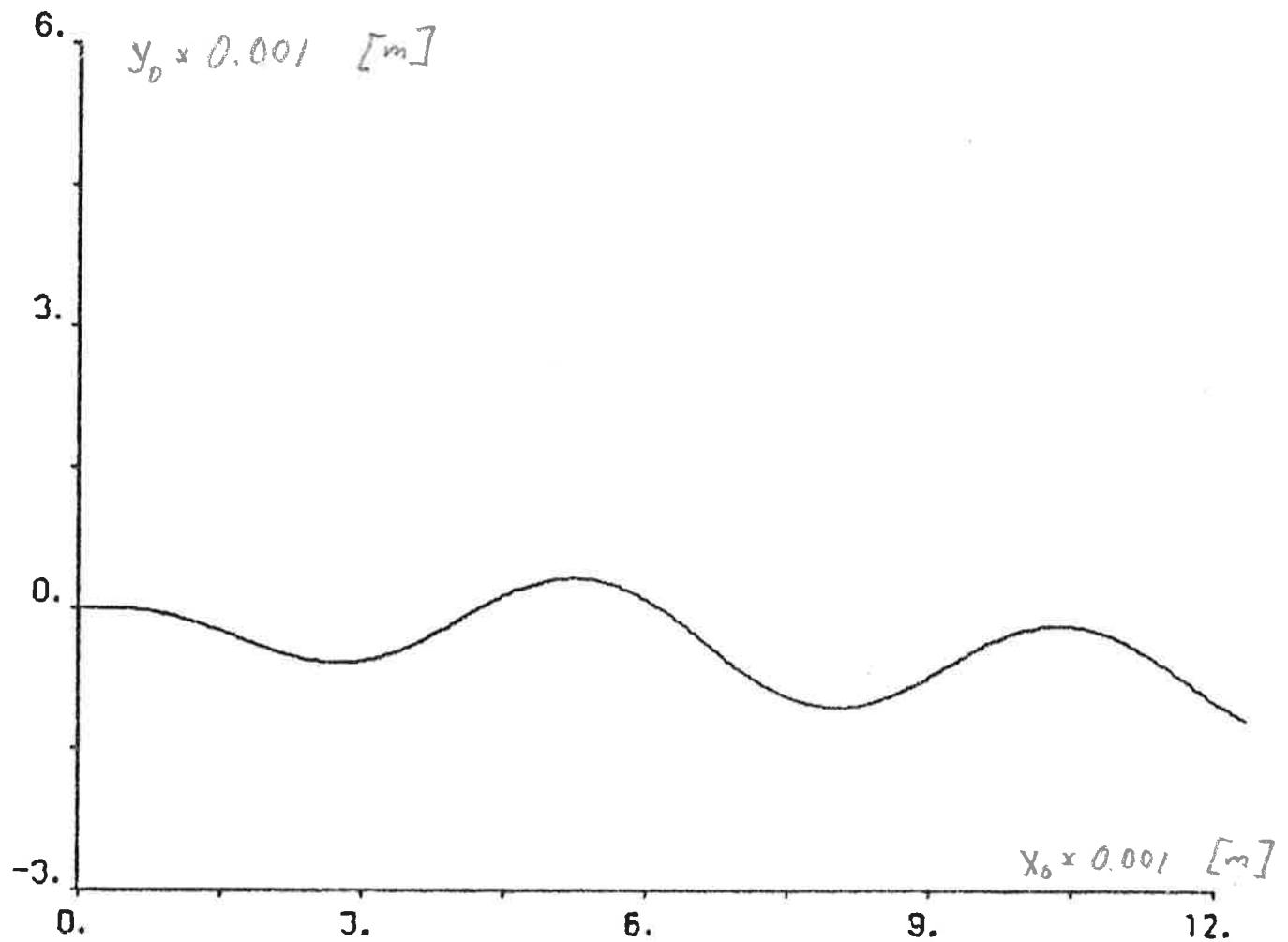


Fig. 4.7 c

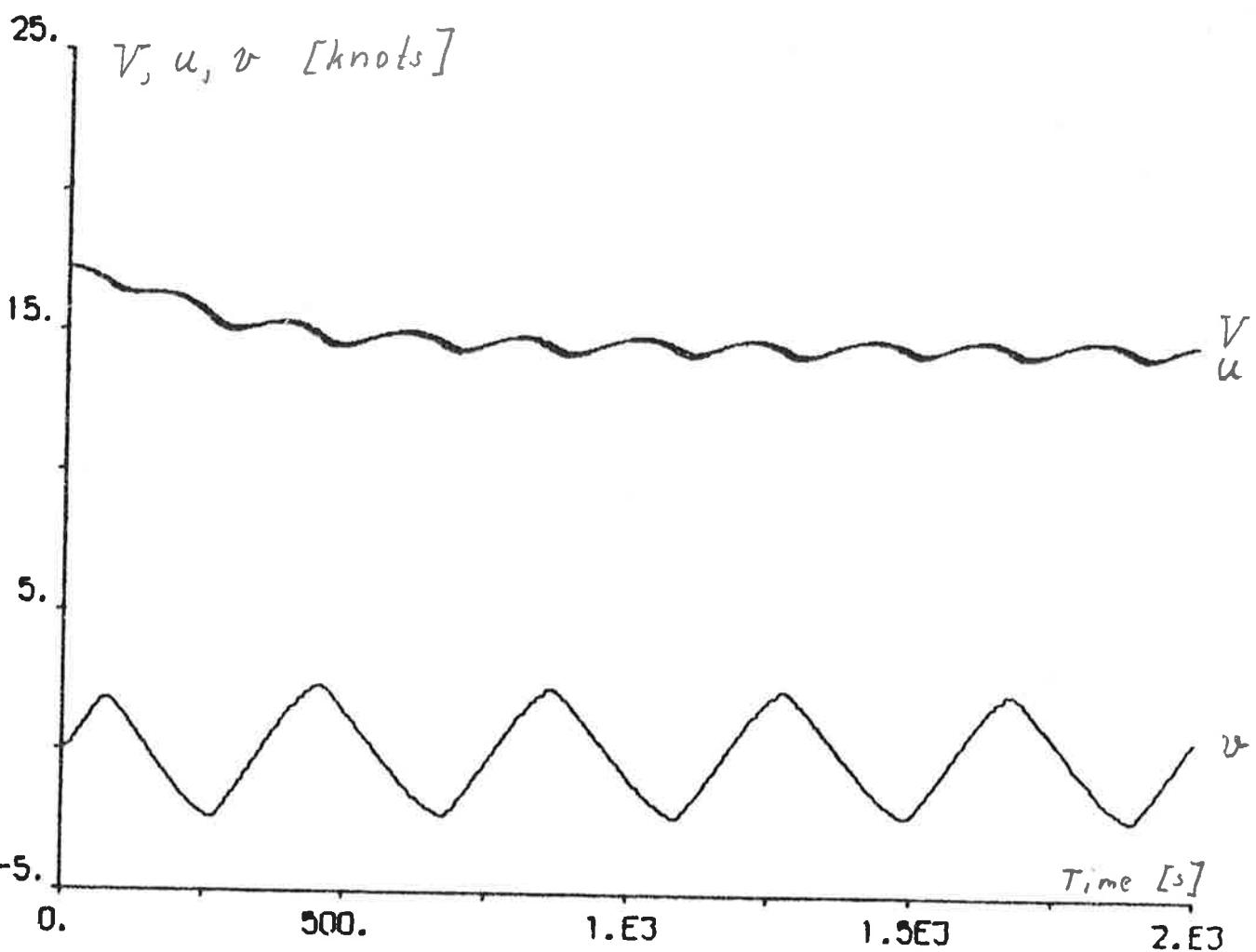
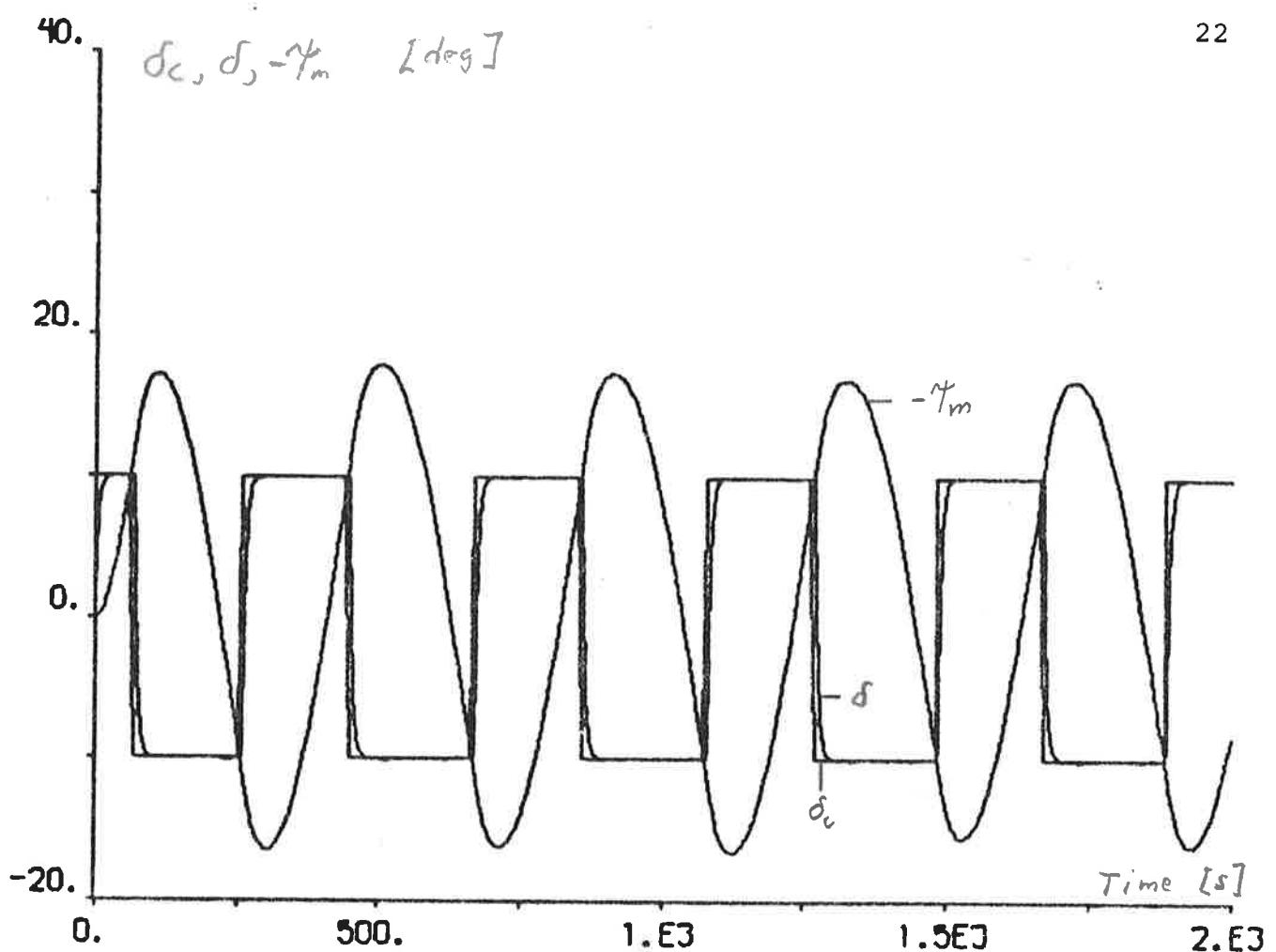


Fig. 4.8 a - Zig-zag test ($10^\circ/10^\circ$): $T = 10.5$ m.

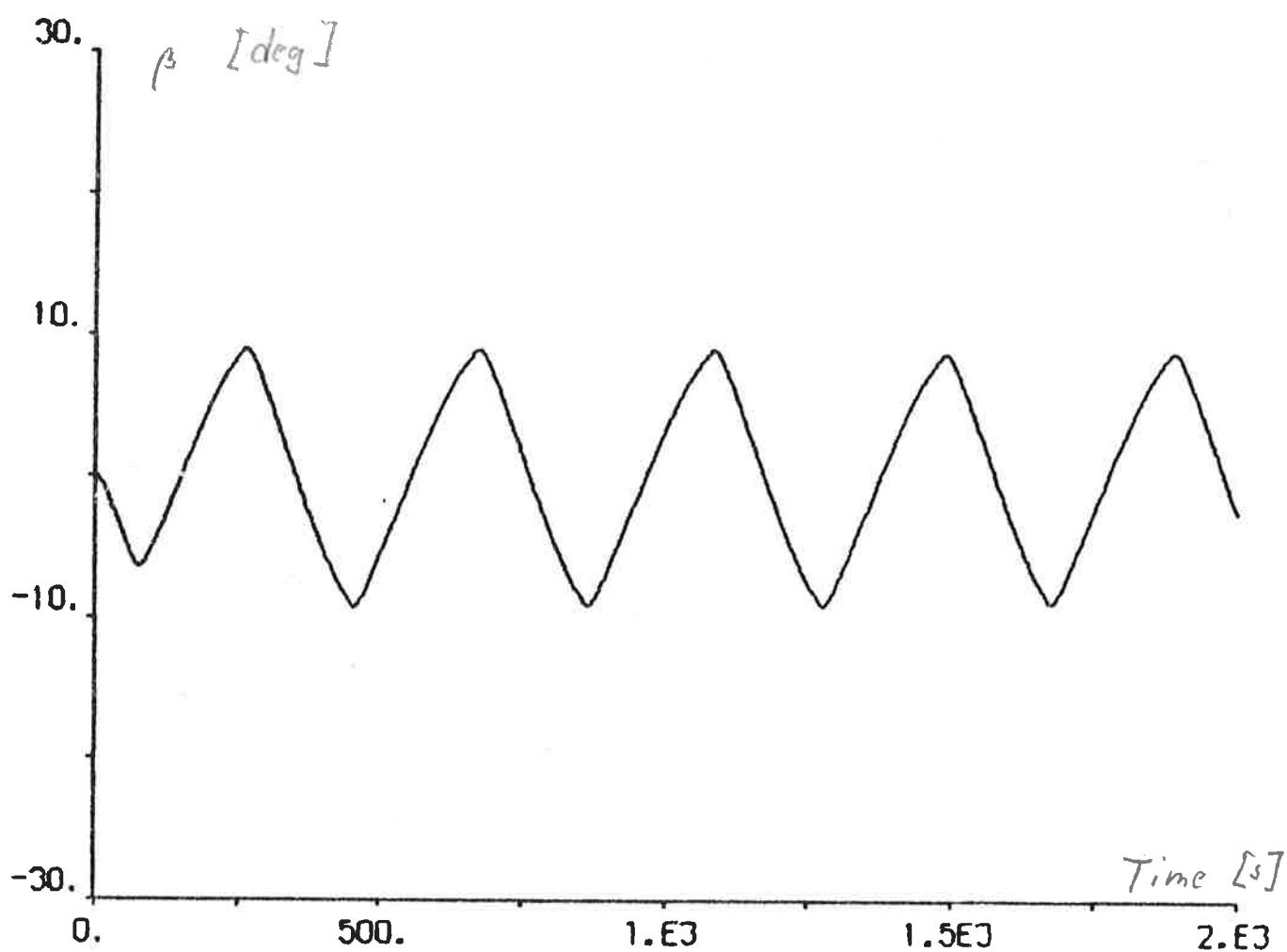
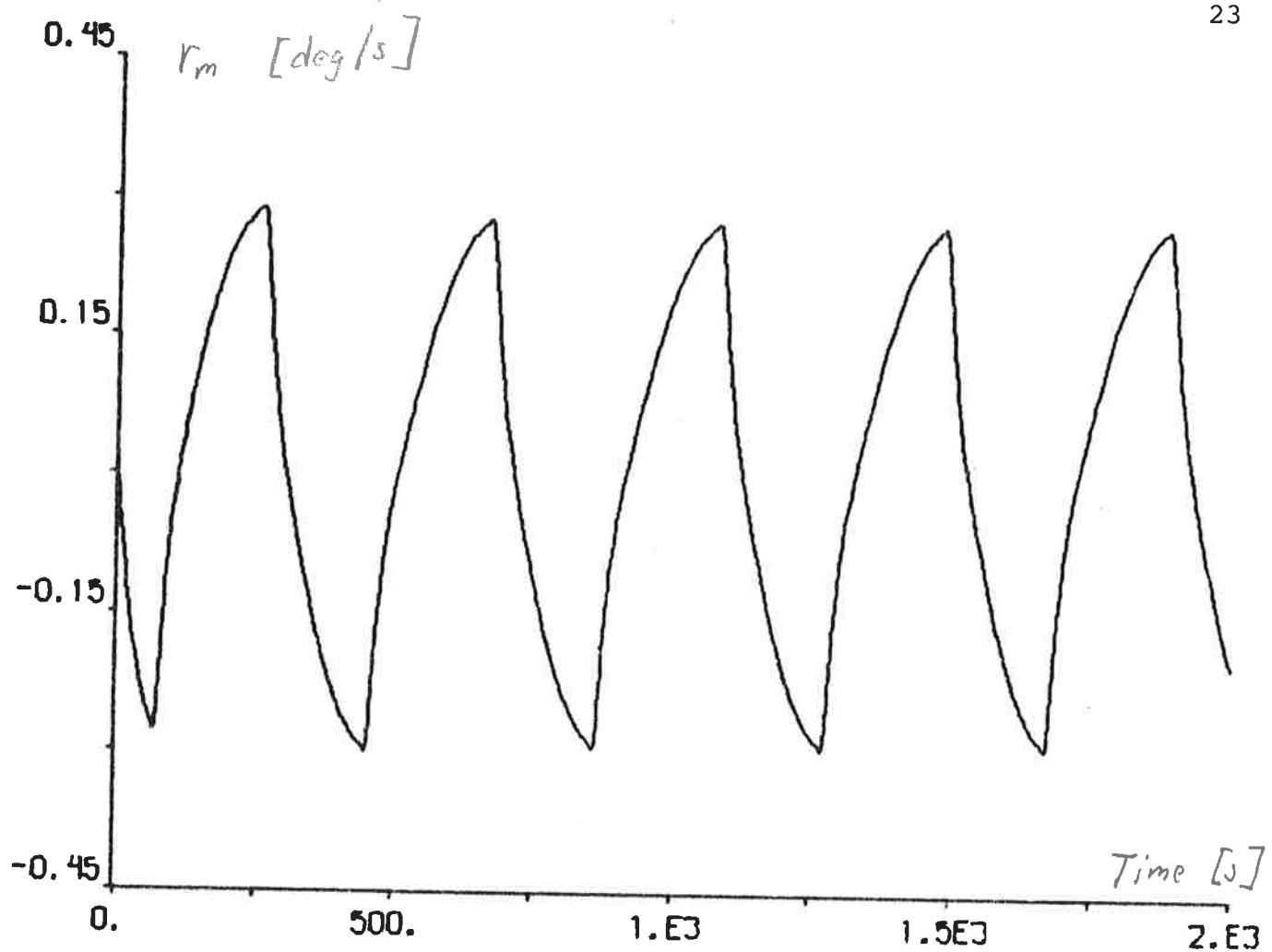


Fig. 4.8 b

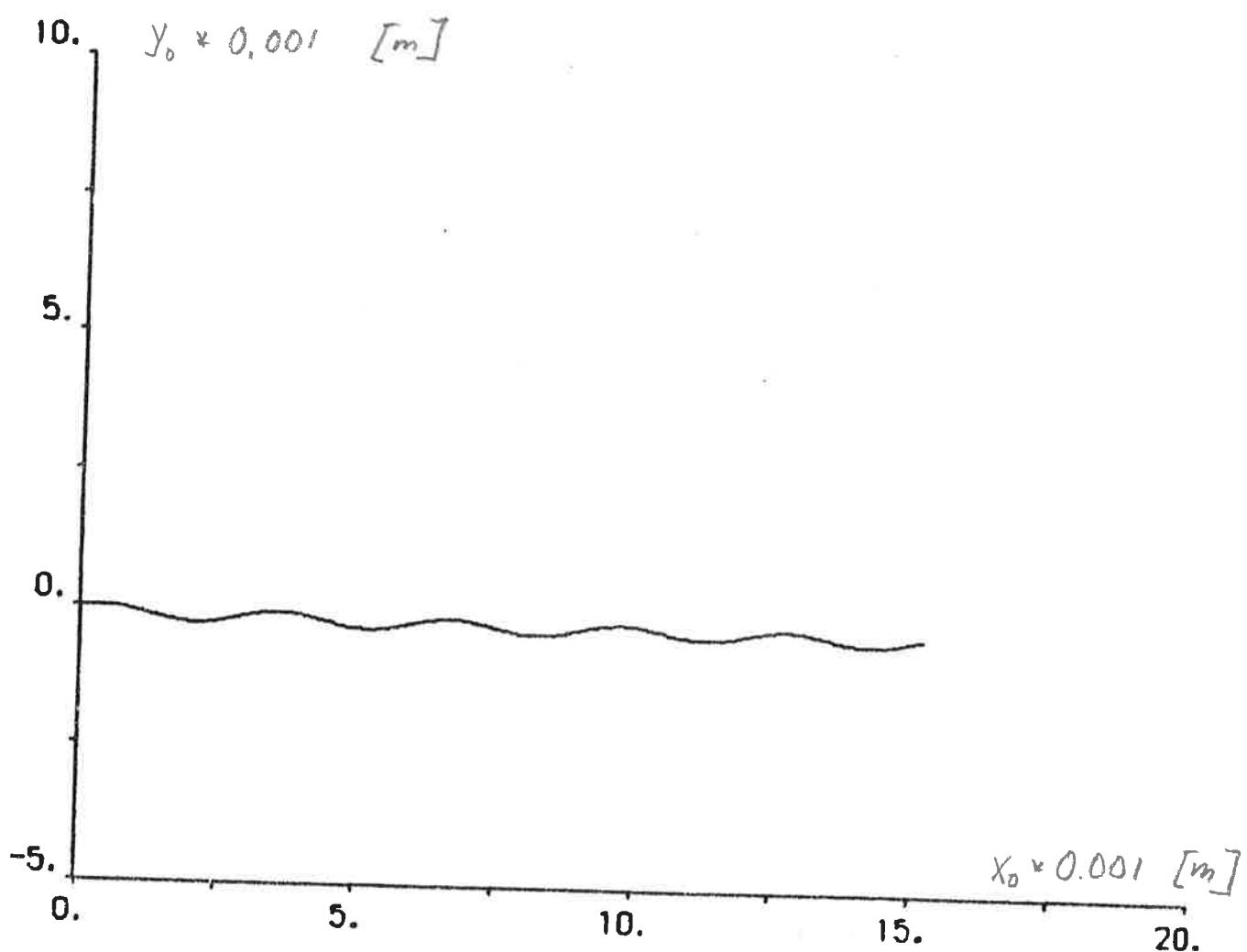


Fig. 4.8 c

5. SIMULATION OF YAWS

The yaw regulator described in Chapter 3 is used to perform course changes $\Delta\psi_{ref}$ of 2, 4, 45 and 120 deg when the mean draught of the ship T is 22.3 m and 10.5 m. The reference values of the yaw rate used in the simulations are $r_{ref} = 0.05, 0.1, 0.2$ and 0.3 deg/s . The initial reference course is always equal to 0 deg and the course change is requested after 100 s.

Simulations when no disturbances are applied, i.e. $F_w = 0$, $w_1 = w_2 = e_1 = e_2 = 0$, are shown in Figs. 5.1 - 5.14. Constant wind force disturbance ($F_w = 0.002 \text{ m/s}^2$, $w_1 = w_2 = e_1 = e_2 = 0$) is used in Figs. 5.15 - 5.22. Finally, stochastic disturbances (cf. Chapter 2) are applied in the simulations of Figs. 5.23 - 5.32 ($\sigma_r = 0.01 \text{ deg/s}$) and Figs. 5.33 - 5.42 ($\sigma_r = 0.02 \text{ deg/s}$). The angle of the wind direction α is equal to 90 deg or 270 deg. The upper curves of each figure show the result when the first parameter set of the yaw regulator (cf. Chapter 3) is used, the lower curves show the result when the second parameter set is used. The following scalings are performed before the plotting:

$$10 \times \psi_m, \quad 10 \times \psi_{ref}, \quad 100 \times r_m, \quad 100 \times r_{ref}, \quad -8 \times M_y$$

when

$$\Delta\psi_{ref} = 2 \text{ or } 4 \text{ deg},$$

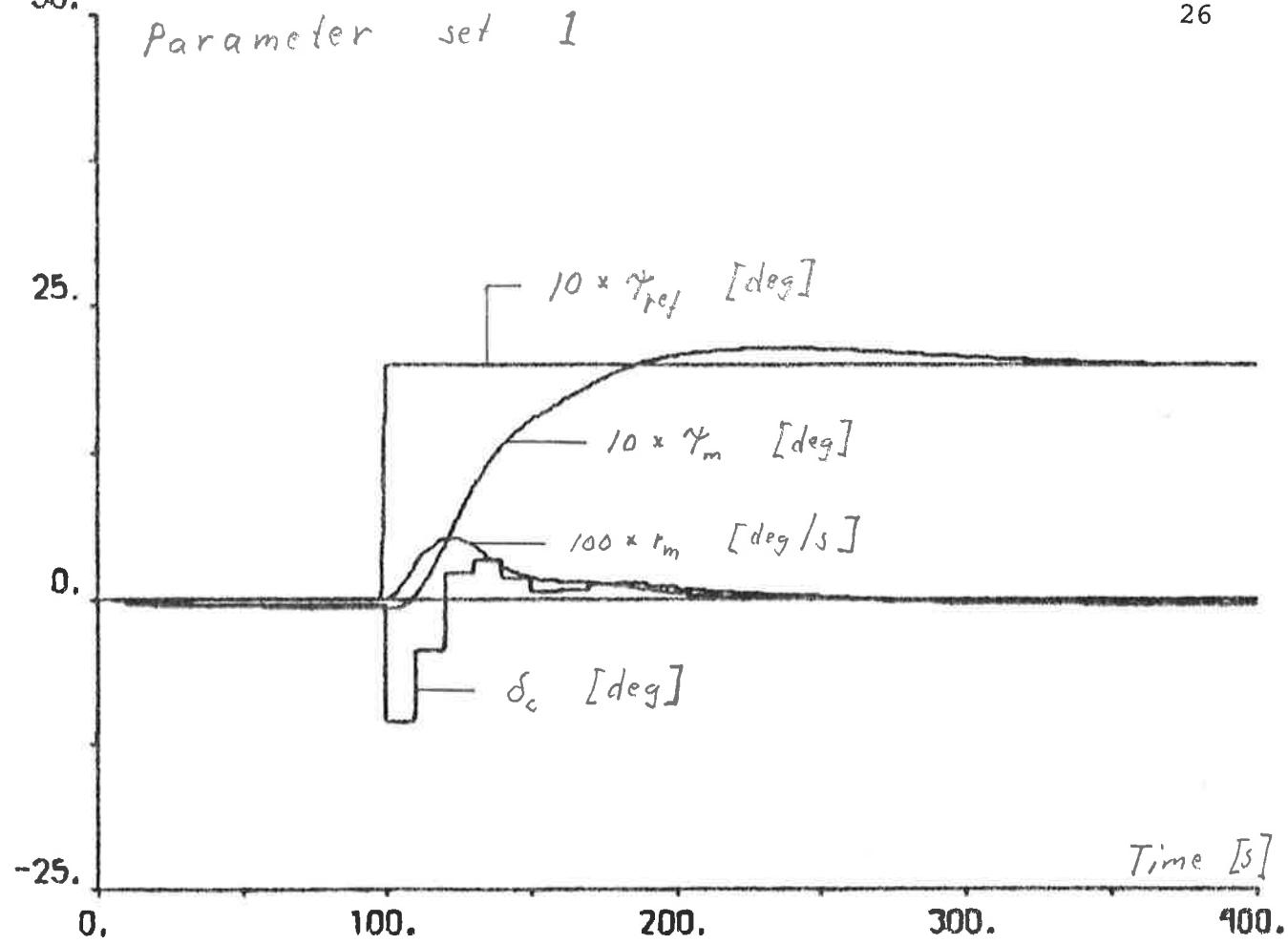
and

$$200 \times r_m, \quad 200 \times r_{ref} \quad \text{and} \quad -8 \times M_y$$

when

$$\Delta\psi_{ref} = 45 \text{ or } 120 \text{ deg.}$$

The rudder command δ_c is always unscaled. In Figs. 5.1, 5.3 and 5.7 are shown a complete description of the plots.



Parameter set 2

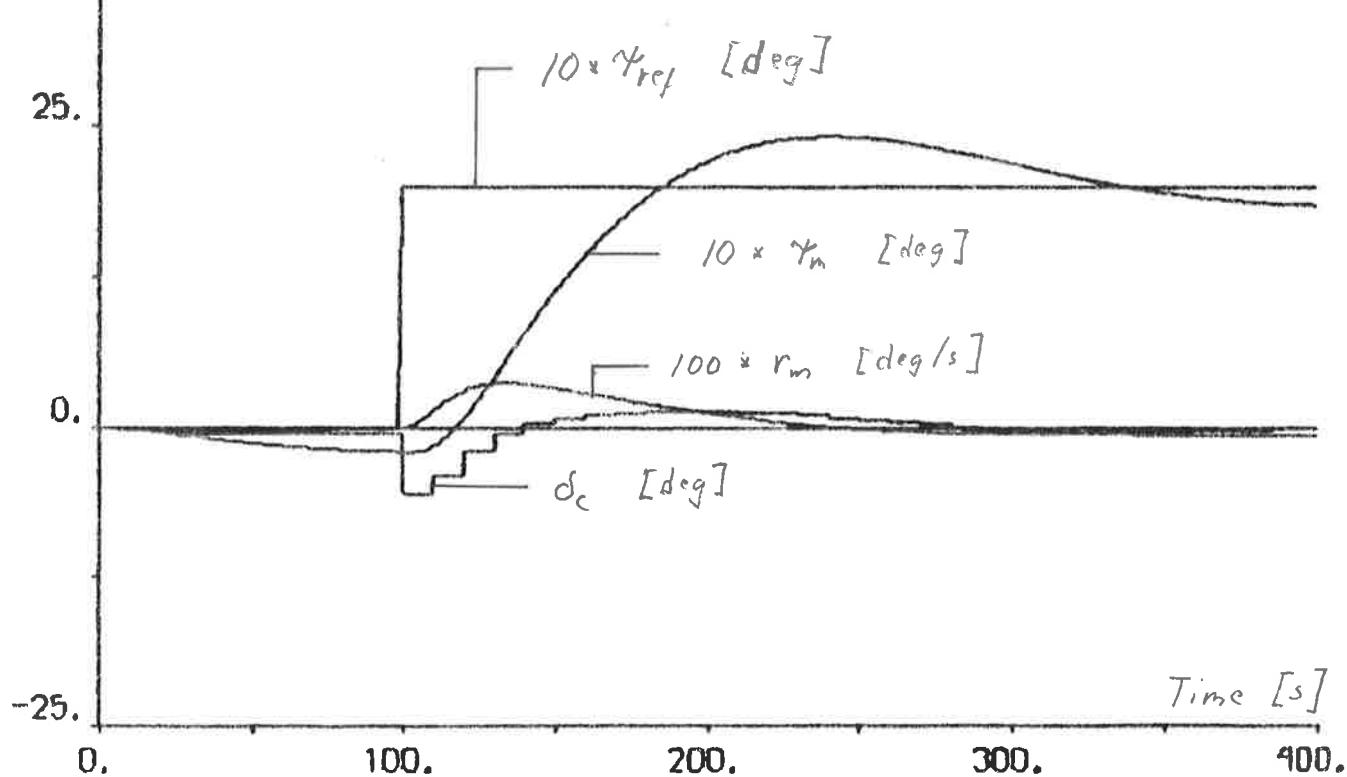


Fig. 5.1 - No disturbances: $T = 22.3$ m, $\Delta\psi_{ref} = 2$ deg.

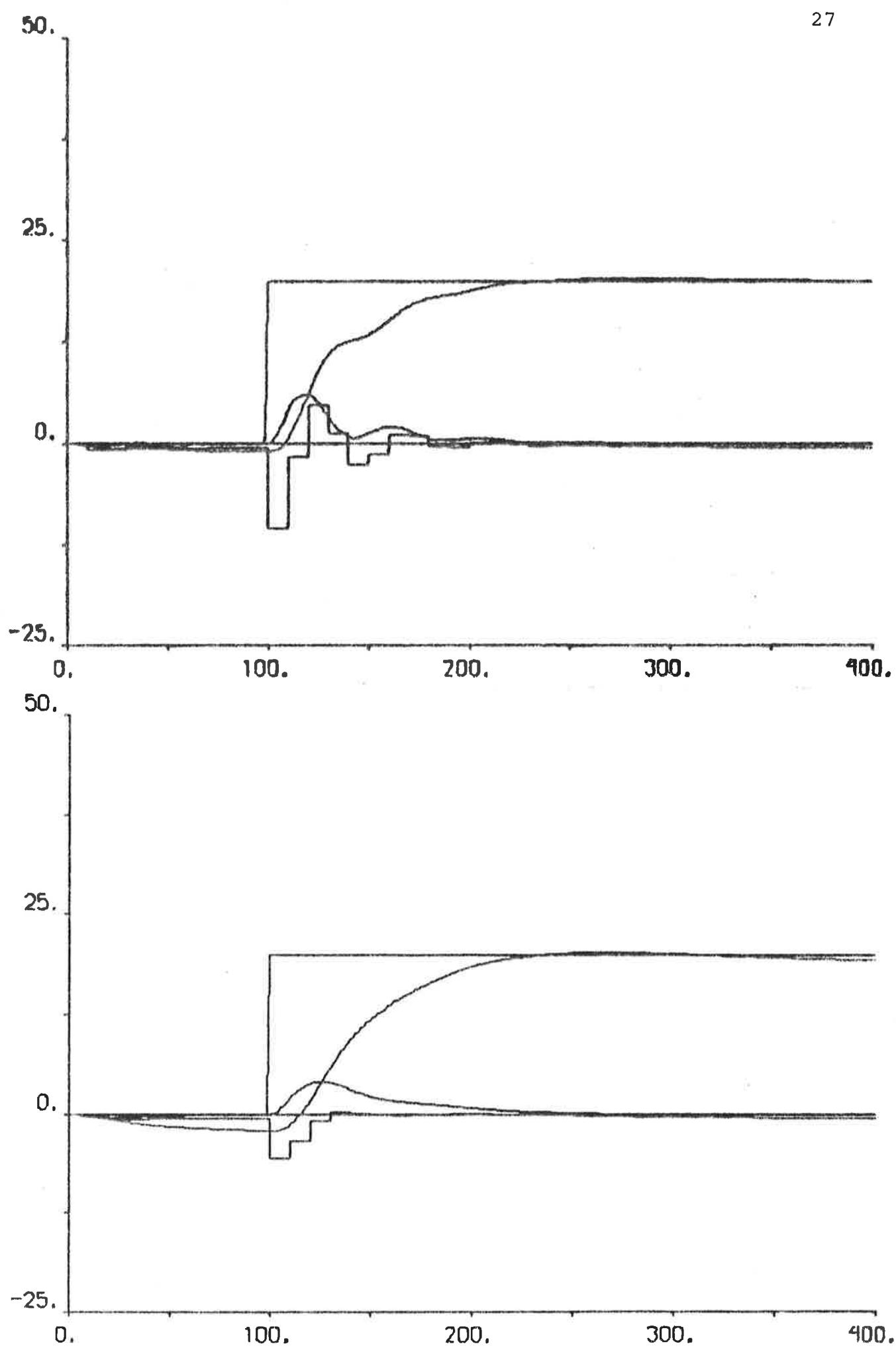
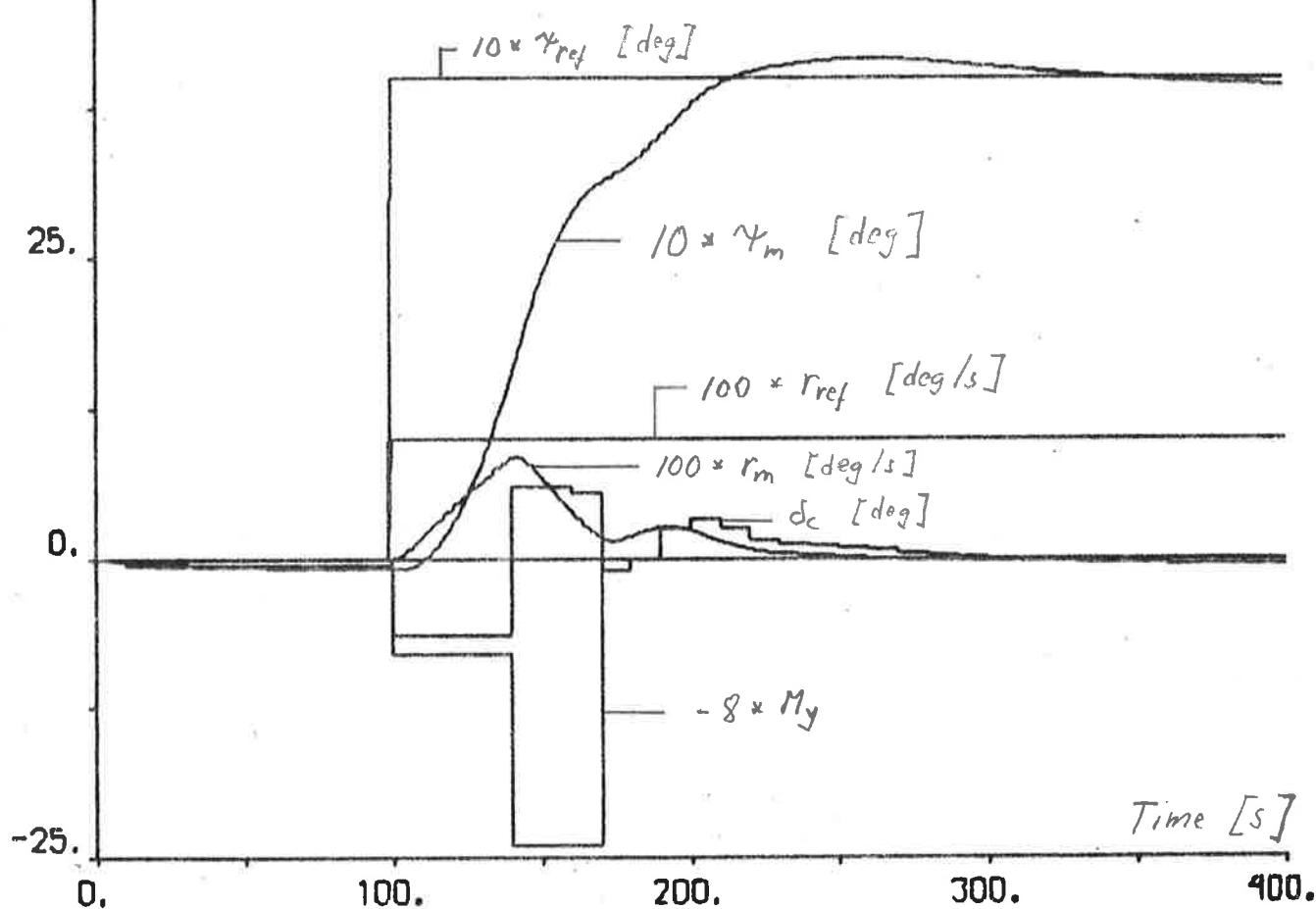


Fig. 5.2 - No disturbances: $T = 10.5$ m, $\Delta\psi_{ref} = 2$ deg.



50. Parameter set 2

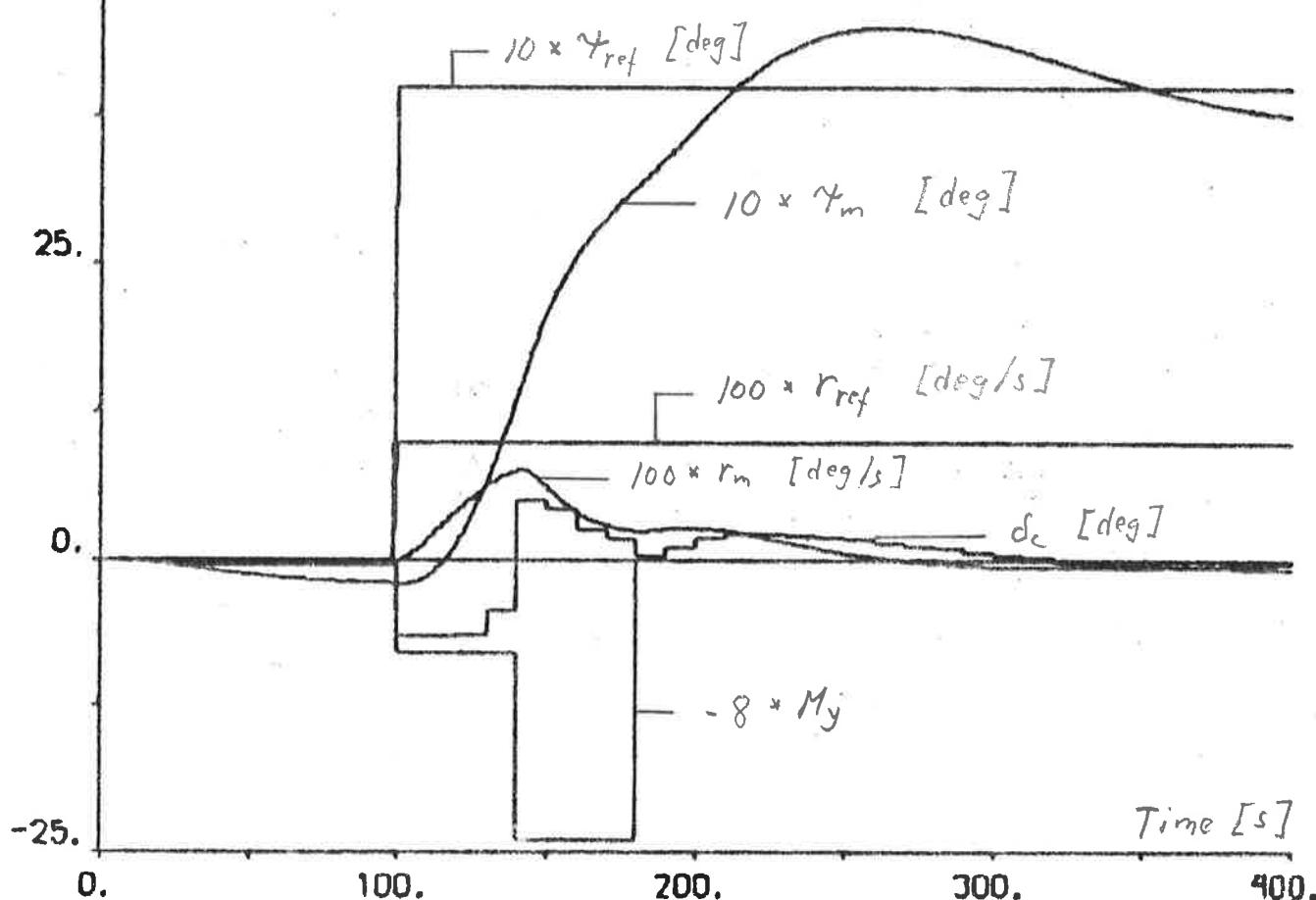


Fig. 5.3 - No disturbances: $T = 22.3$ m, $\Delta\psi_{ref} = 4$ deg,
 $r_{ref} = 0.1$ deg/s.

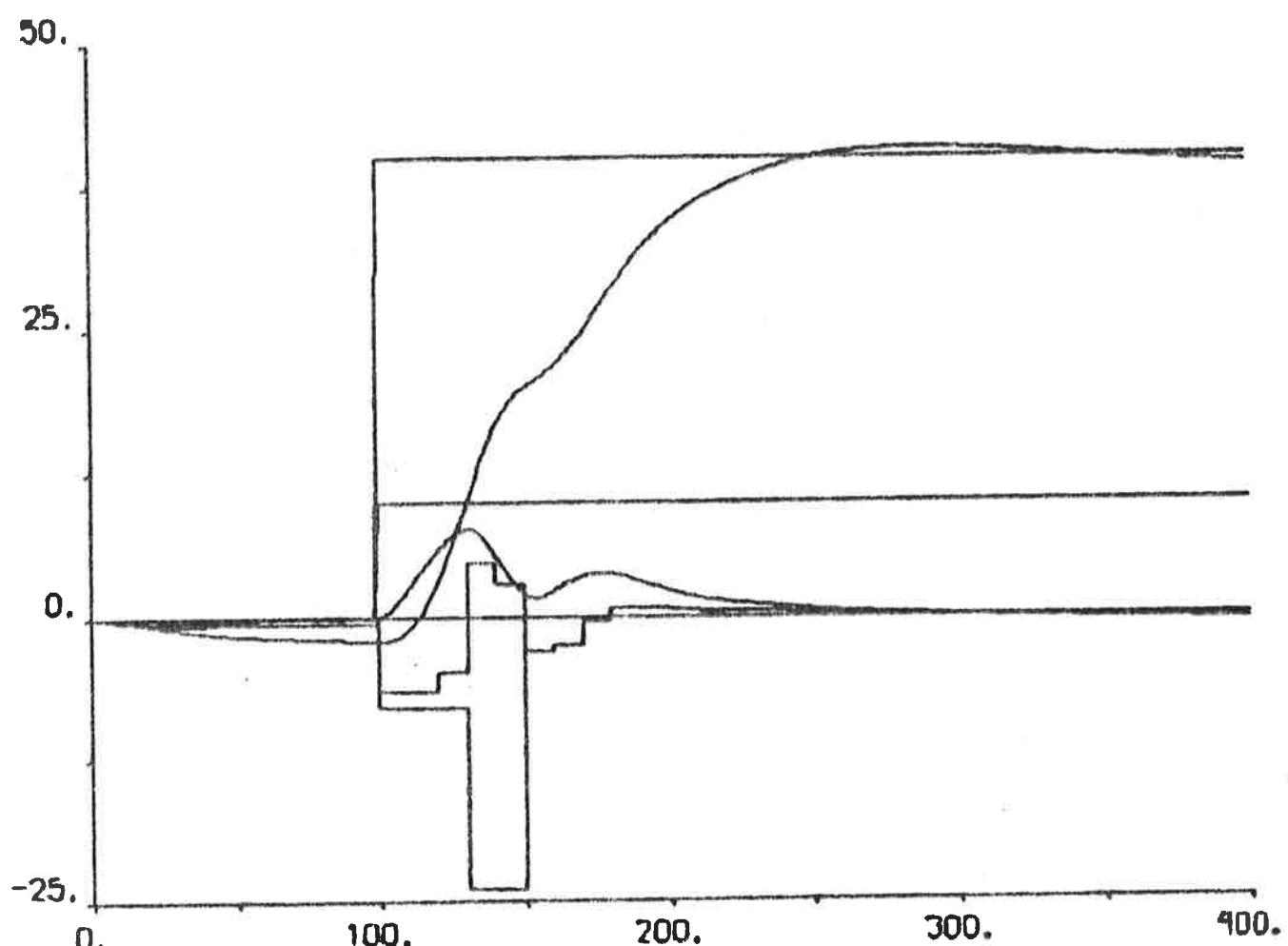
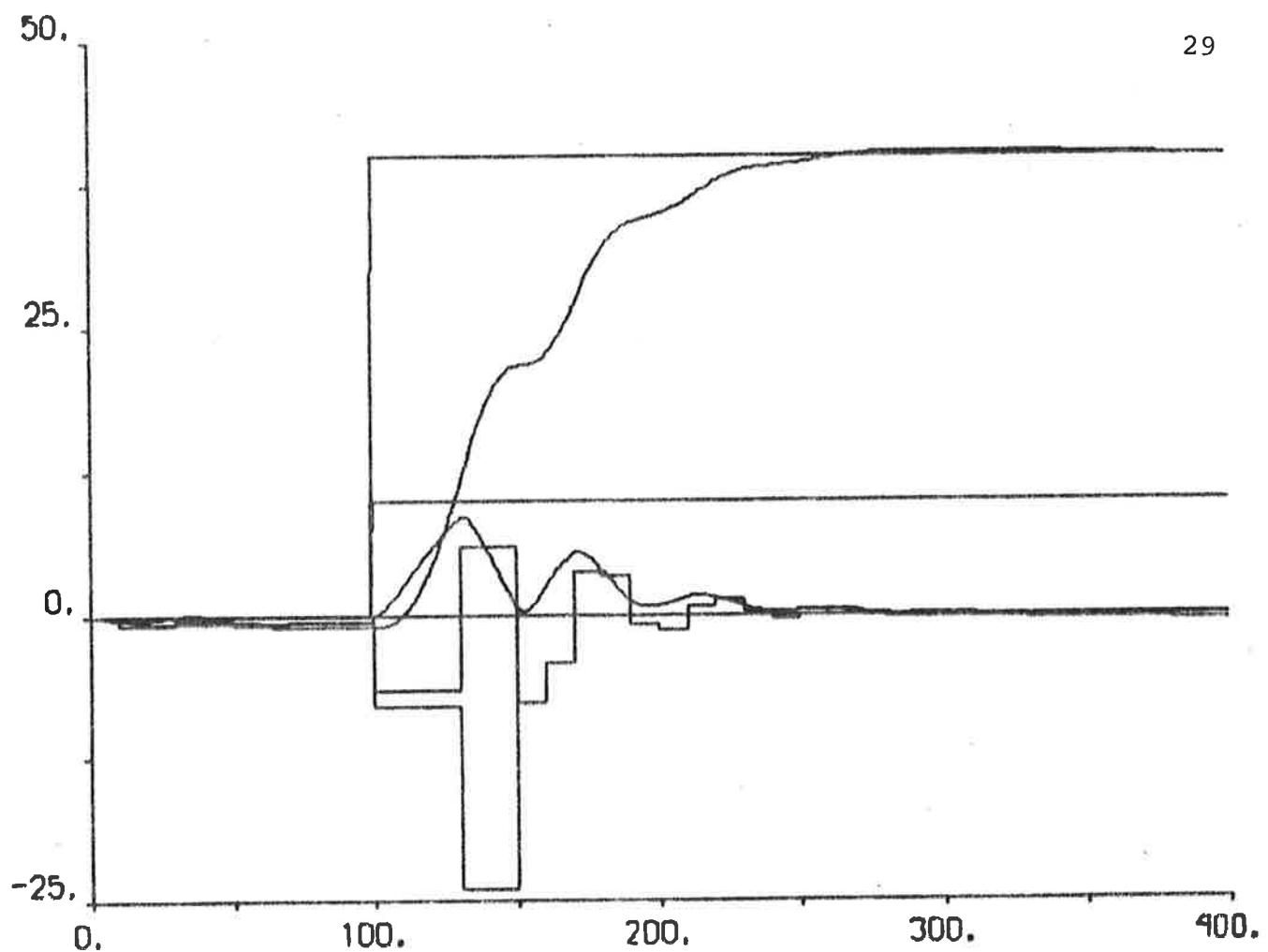


Fig. 5.4 - No dusturbances: $T = 10.5 \text{ m}$, $\Delta\psi_{\text{ref}} = 4 \text{ deg}$,
 $r_{\text{ref}} = 0.1 \text{ deg/s}$.

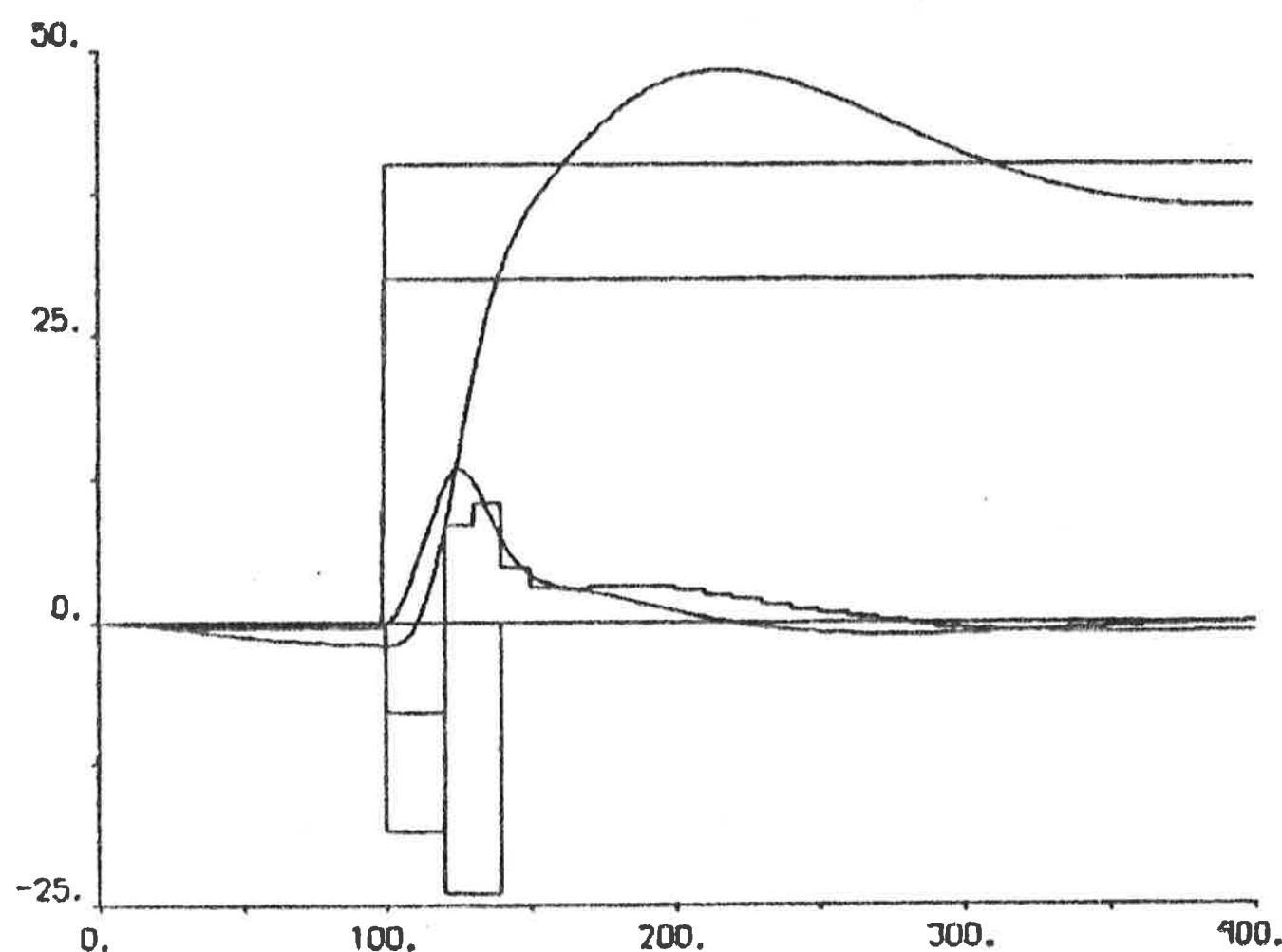
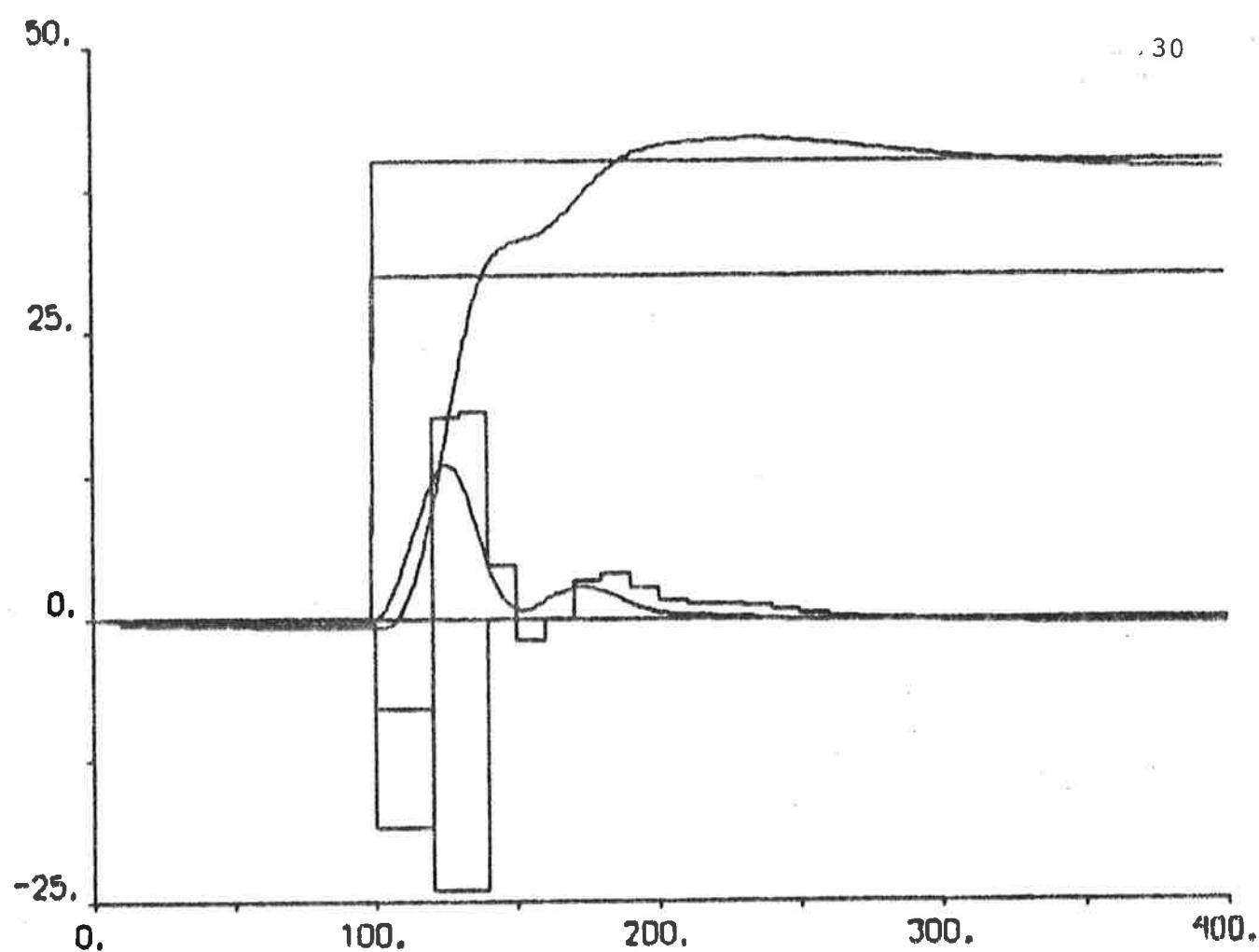


Fig. 5.5 - No disturbances: $T = 22.3$ m, $\Delta\psi_{ref} = 4$ deg,
 $r_{ref} = 0.3$ deg/s.

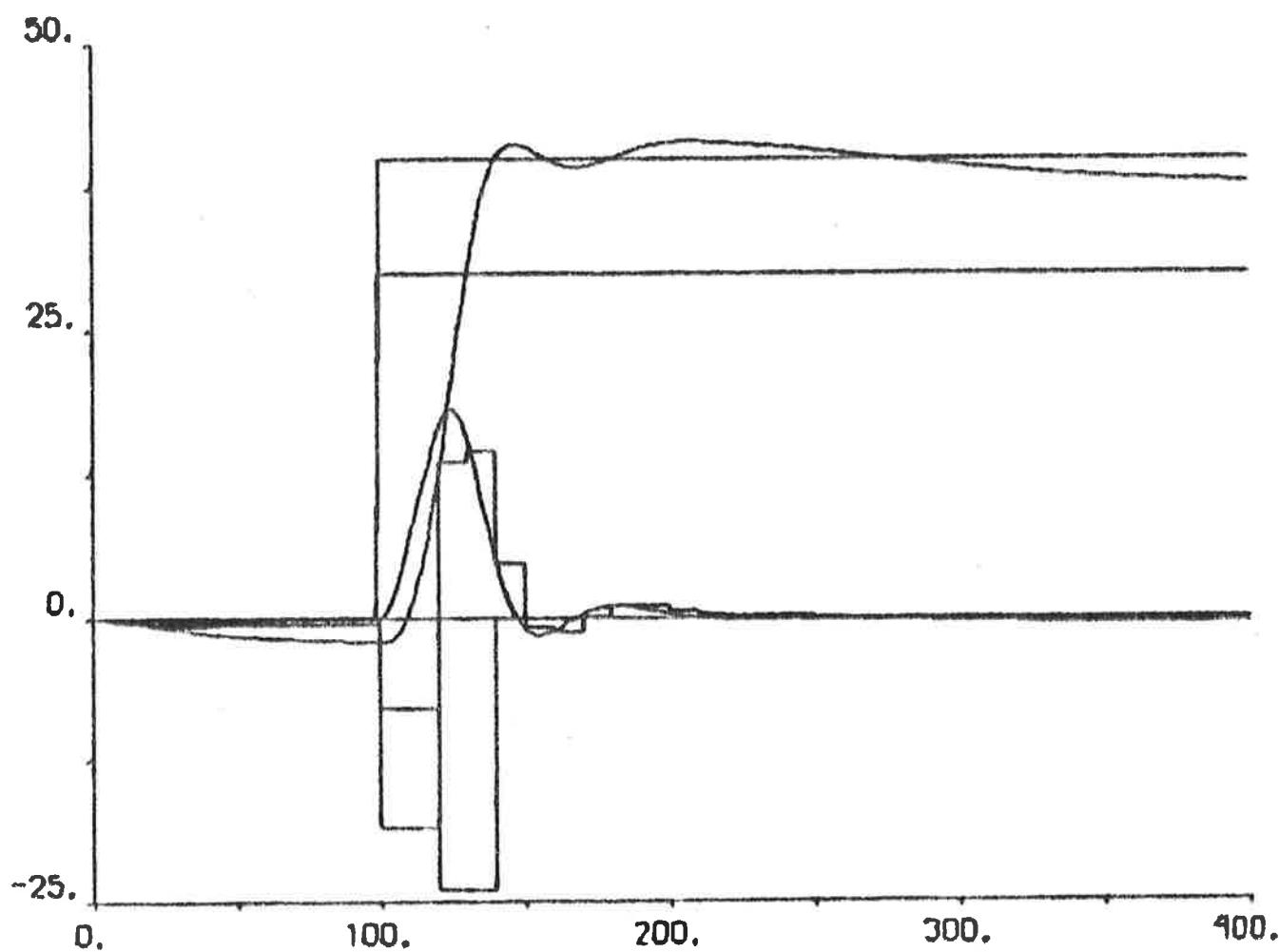
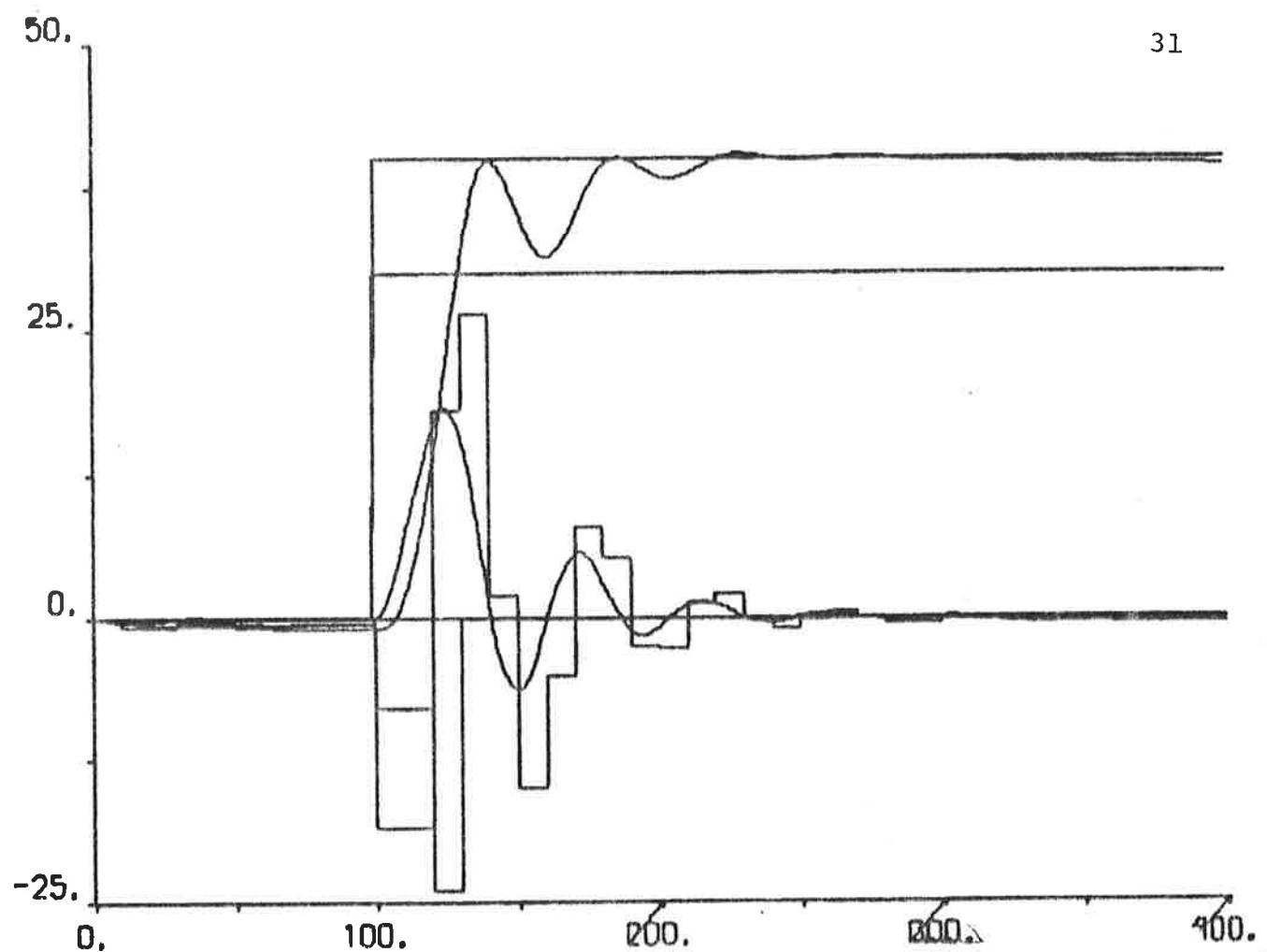
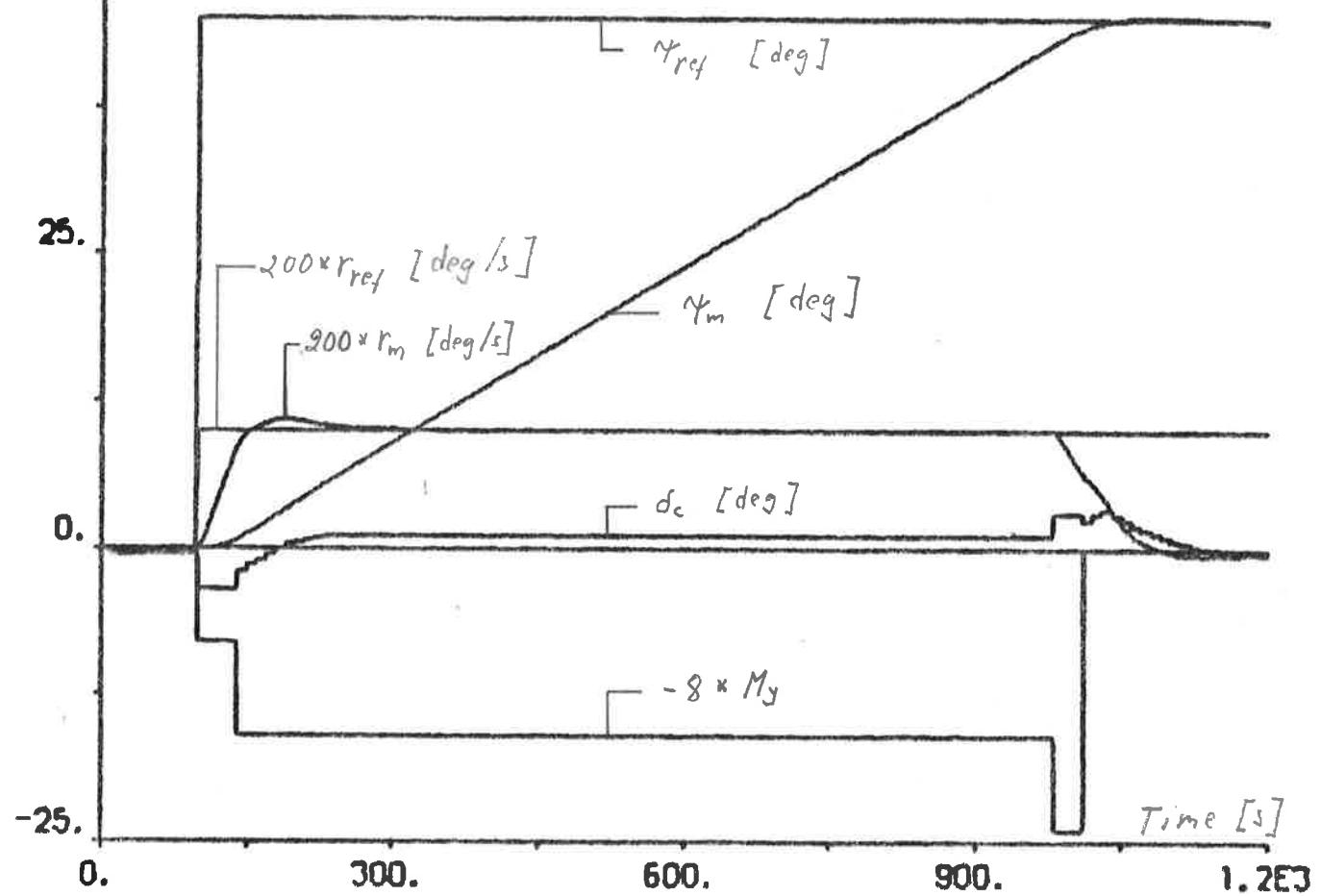


Fig. 5.6 - No disturbances: $T = 10.5 \text{ m}$, $\Delta\psi_{\text{ref}} = 4 \text{ deg}$,
 $r_{\text{ref}} = 0.3 \text{ deg/s}$.



Parameter set 2

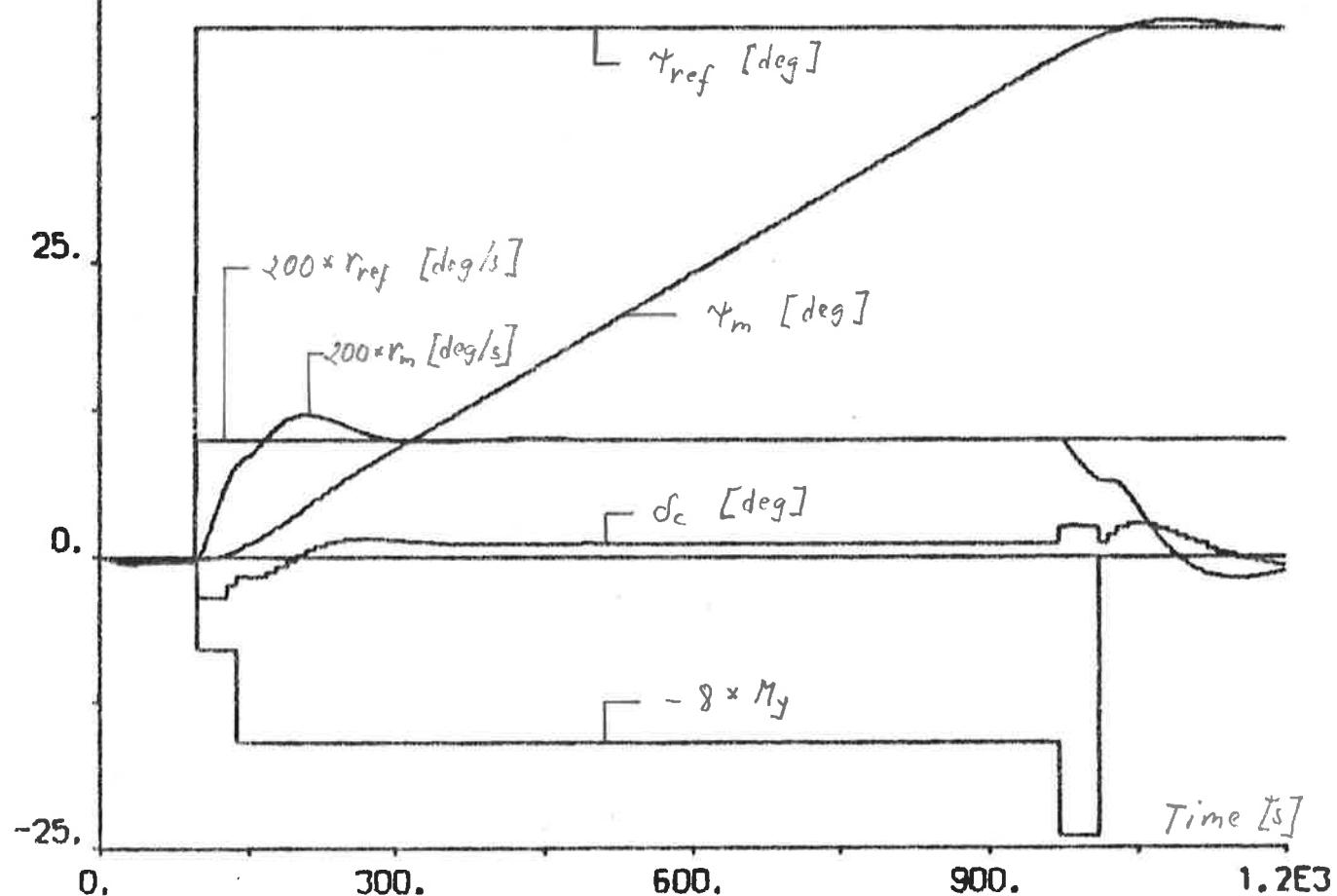


Fig. 5.7 - No disturbances: $T = 22.3$ m, $\Delta\psi_{ref} = 45$ deg,
 $r_{ref} = 0.05$ deg/s.

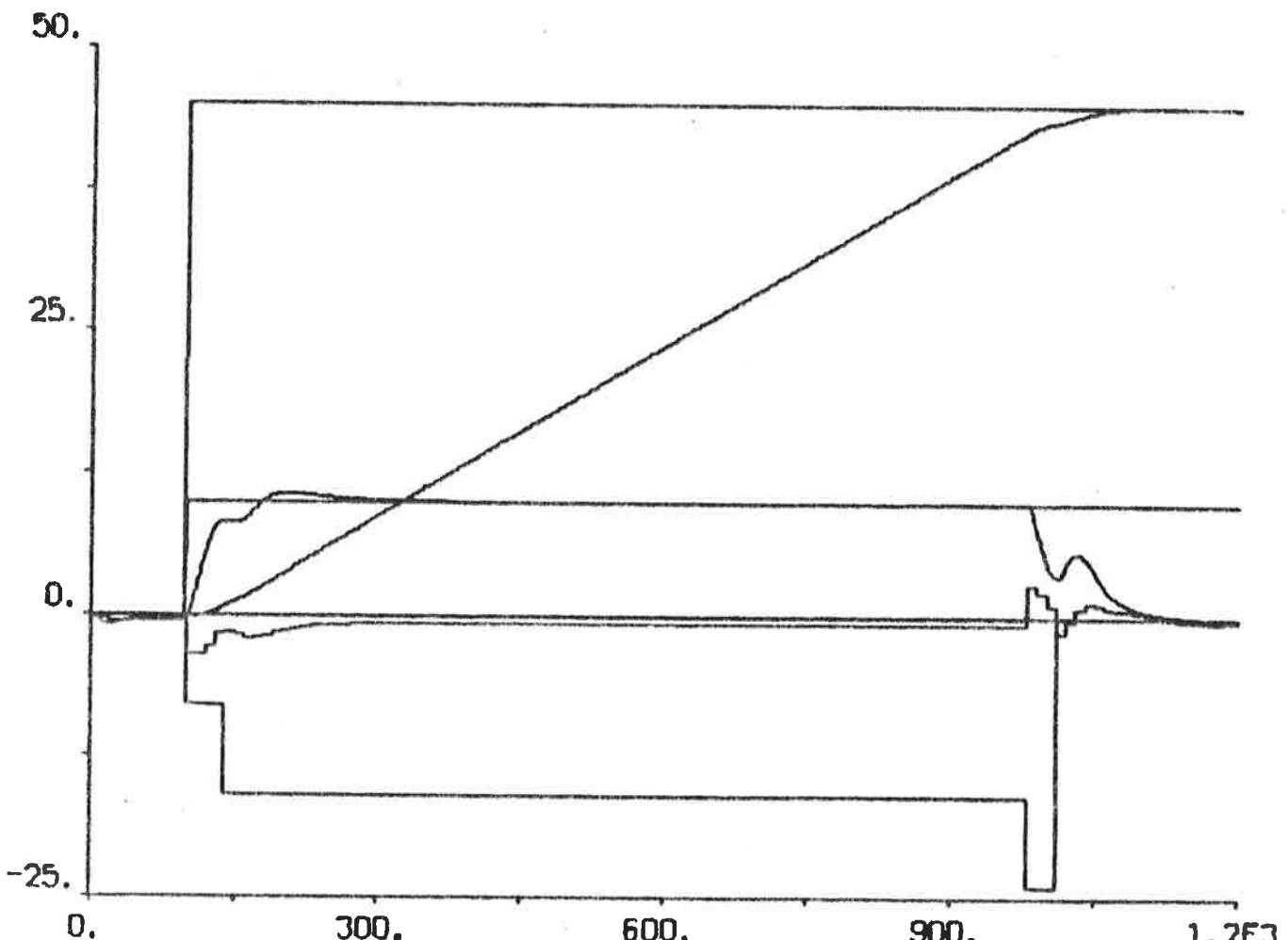
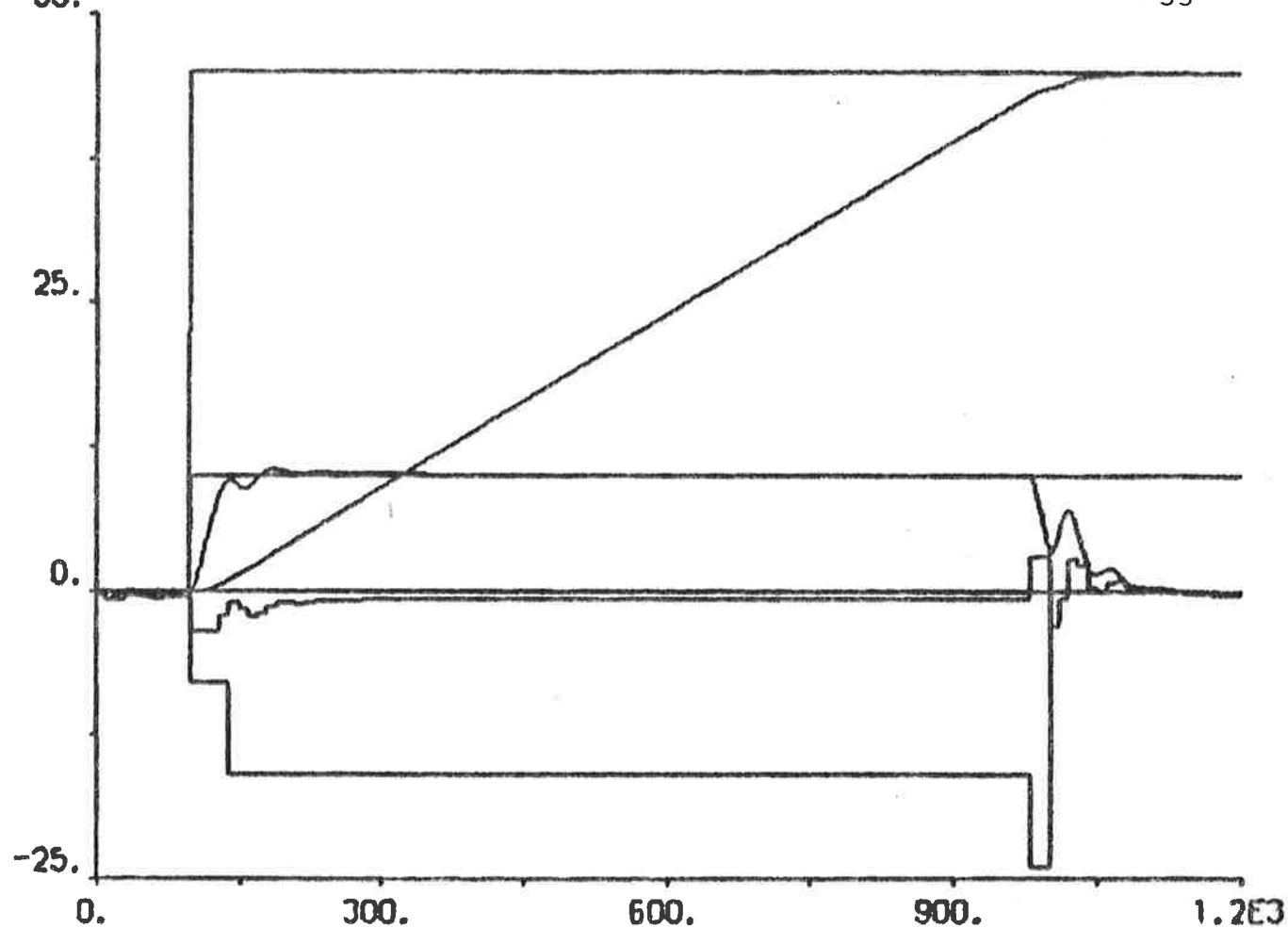


Fig. 5.8 - No disturbances: $T = 10.5$ m, $\Delta\psi_{ref} = 45$ deg,
 $r_{ref} = 0.05$ deg/s.

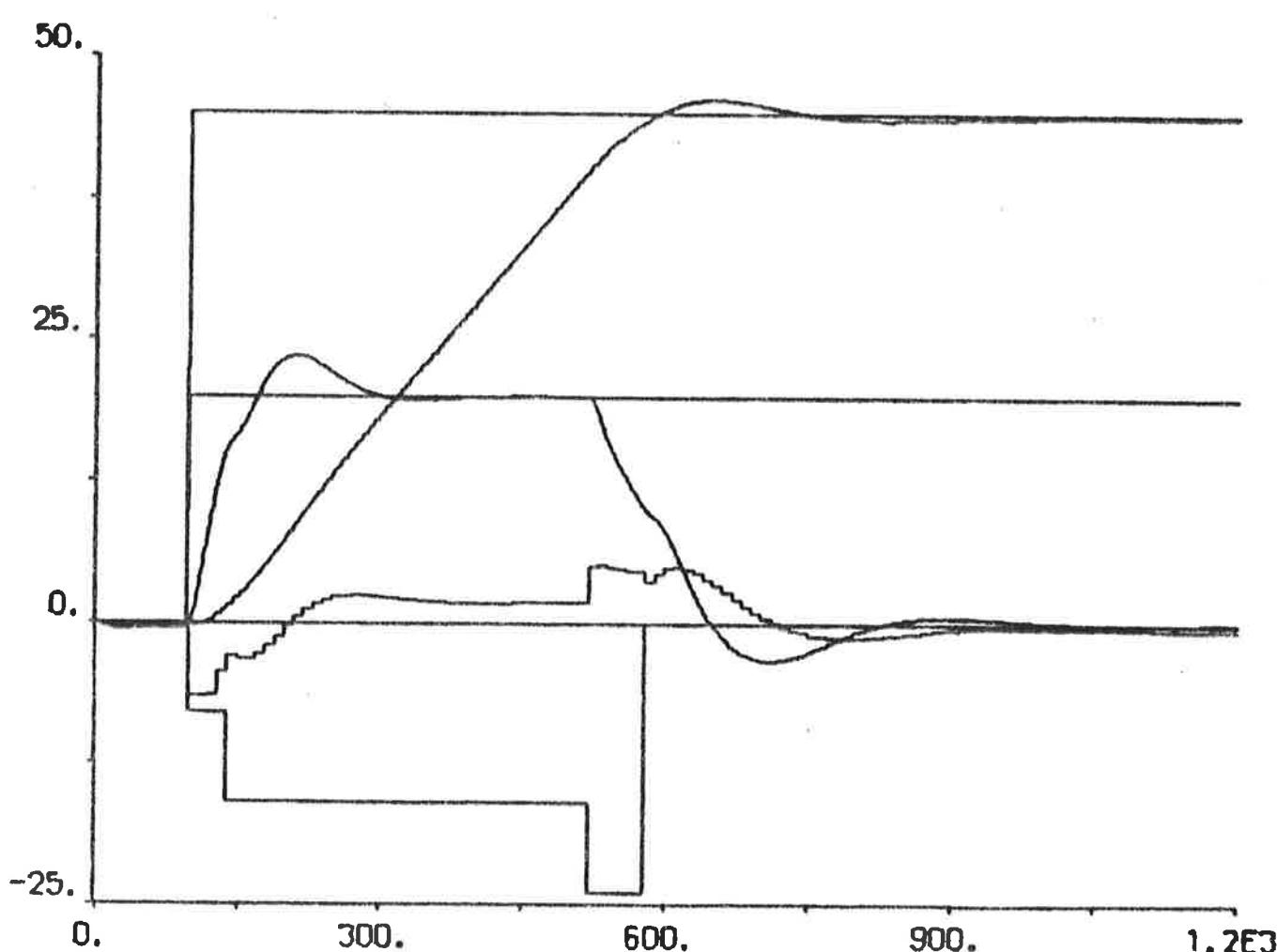
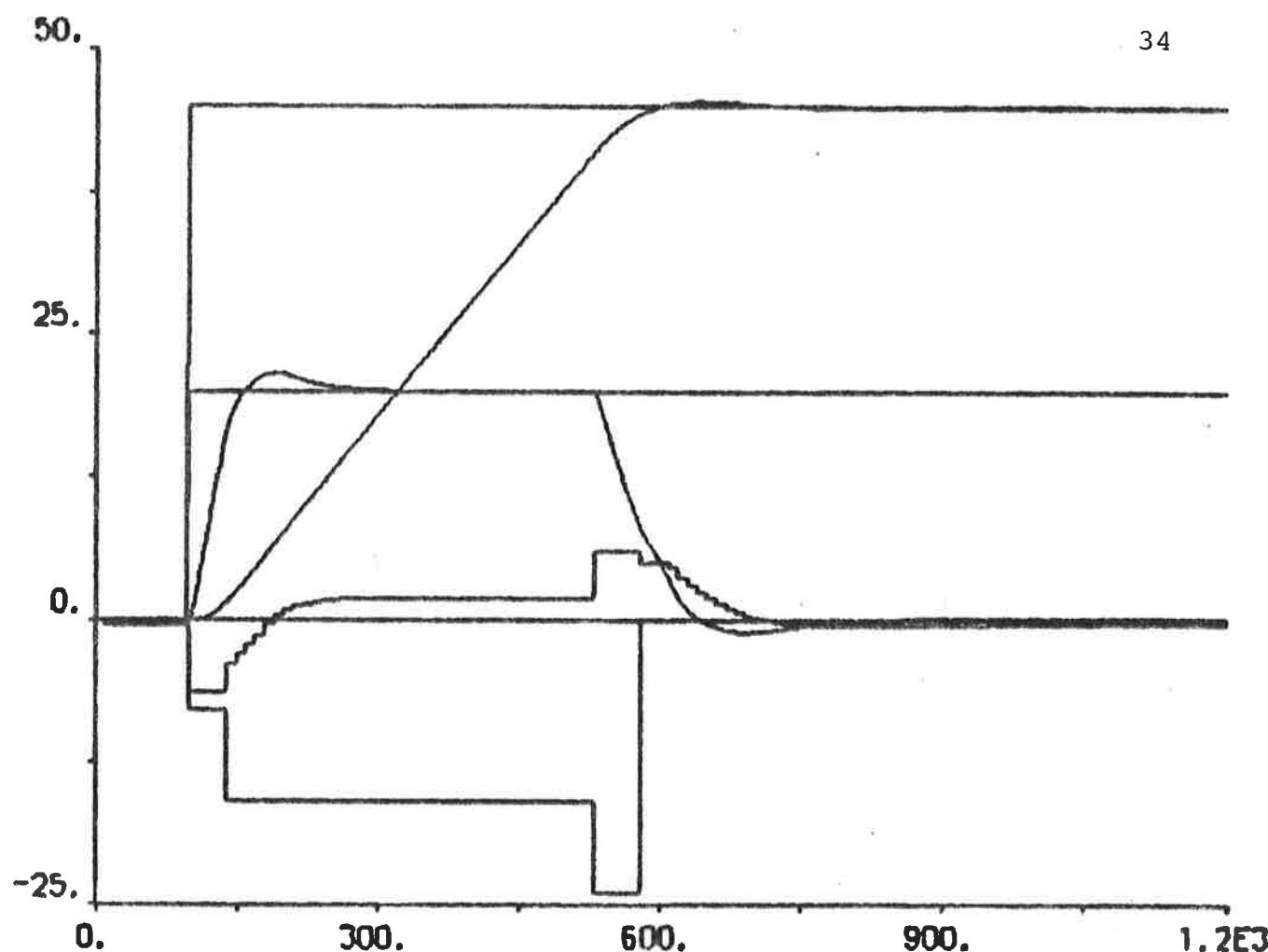


Fig. 5.9 - No disturbances: $T = 22.3$ m, $\Delta\psi_{ref} = 45$ deg,
 $r_{ref} = 0.1$ deg/s.

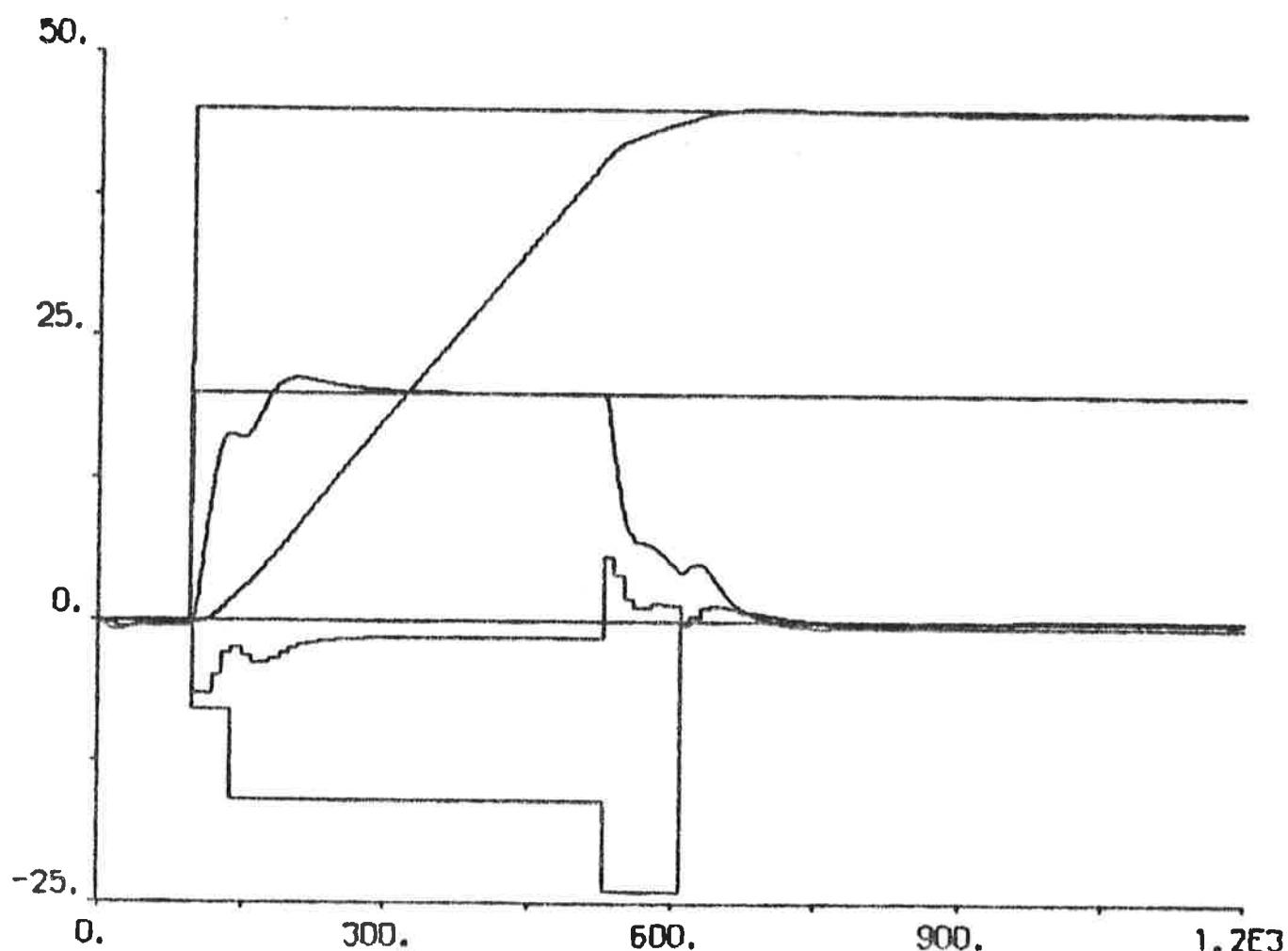
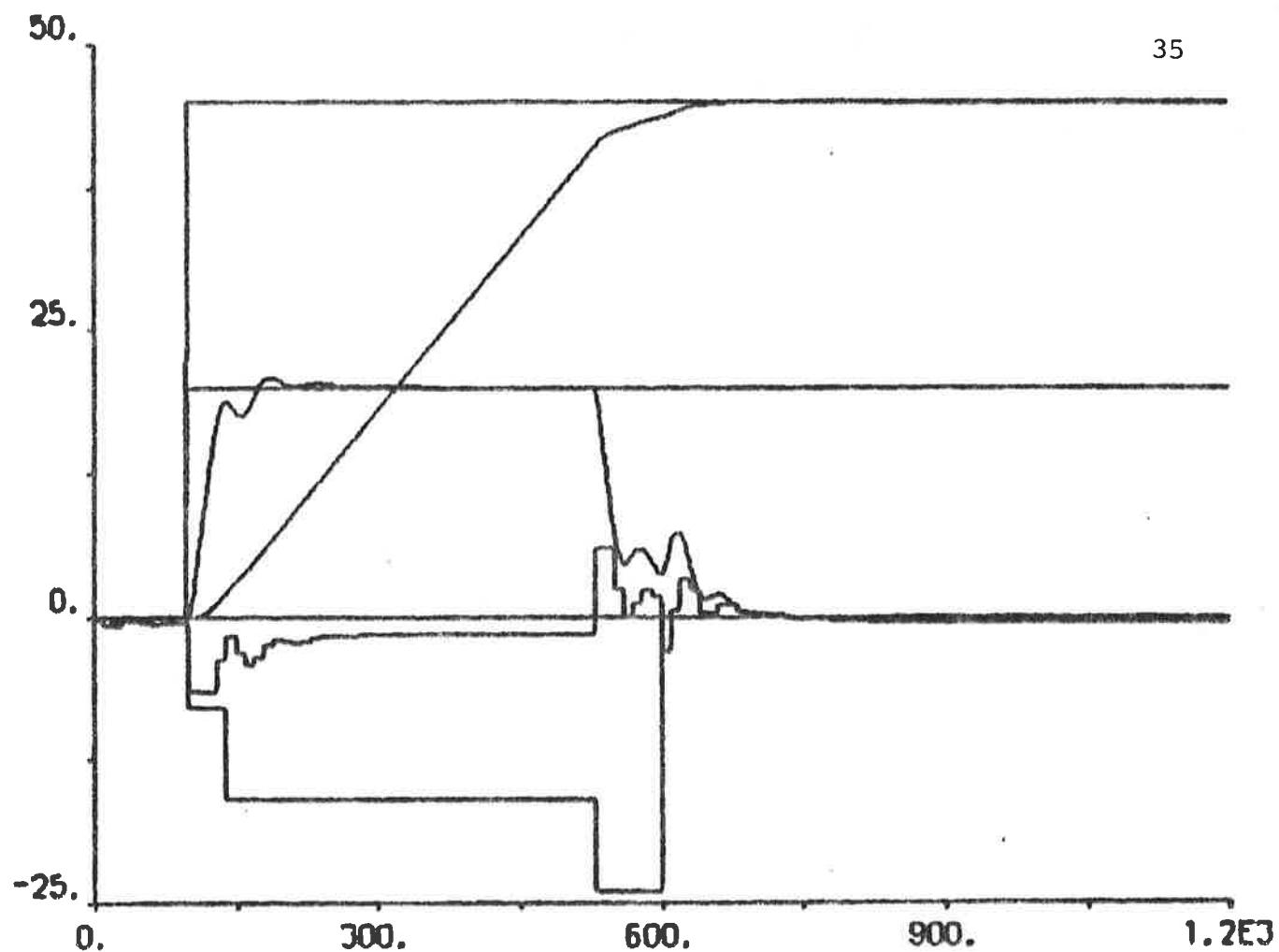


Fig. 5.10 - No disturbances: $T = 10.5 \text{ m}$, $\Delta\psi_{\text{ref}} = 45 \text{ deg}$,
 $r_{\text{ref}} = 0.1 \text{ deg/s}$.

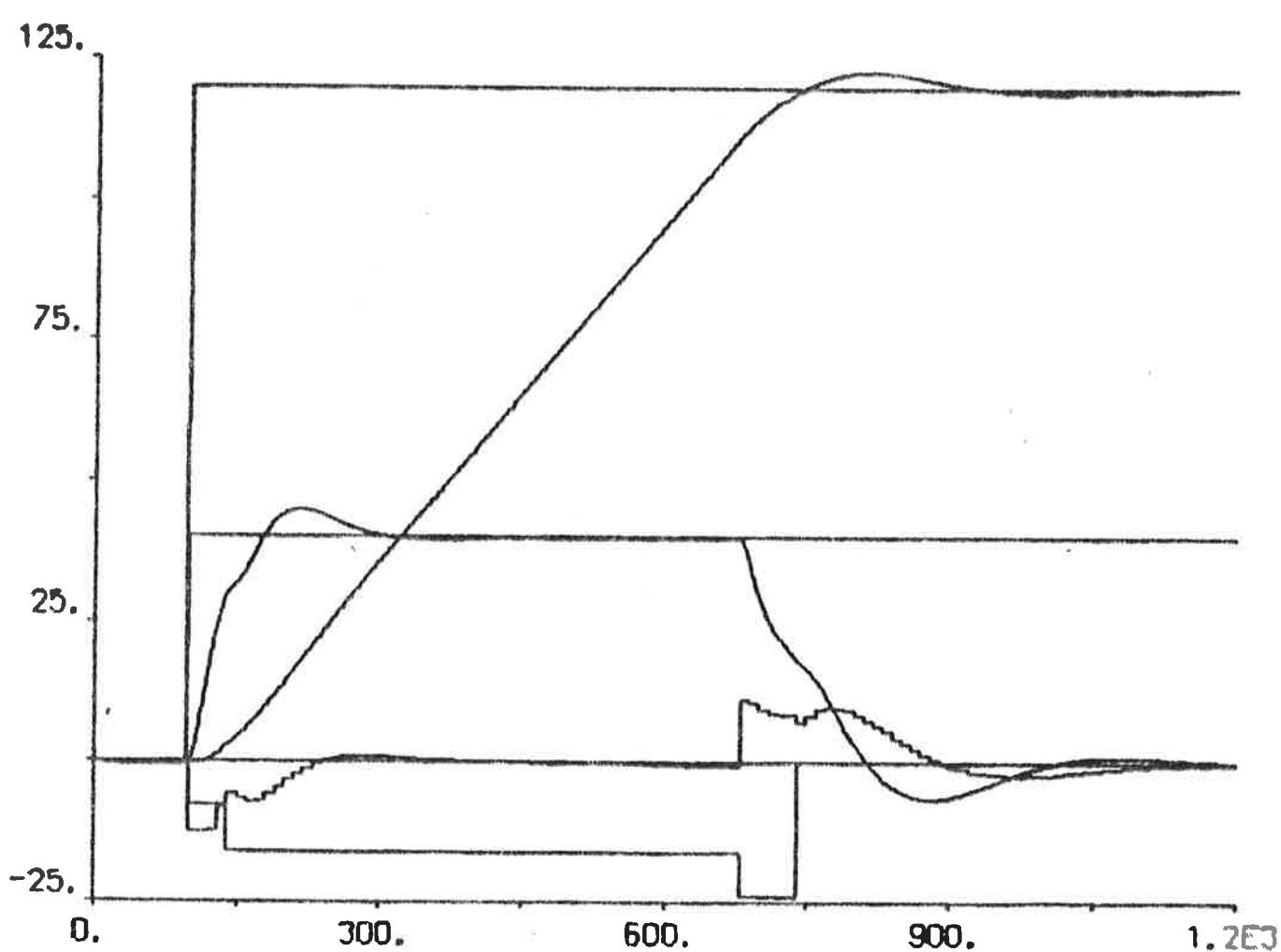
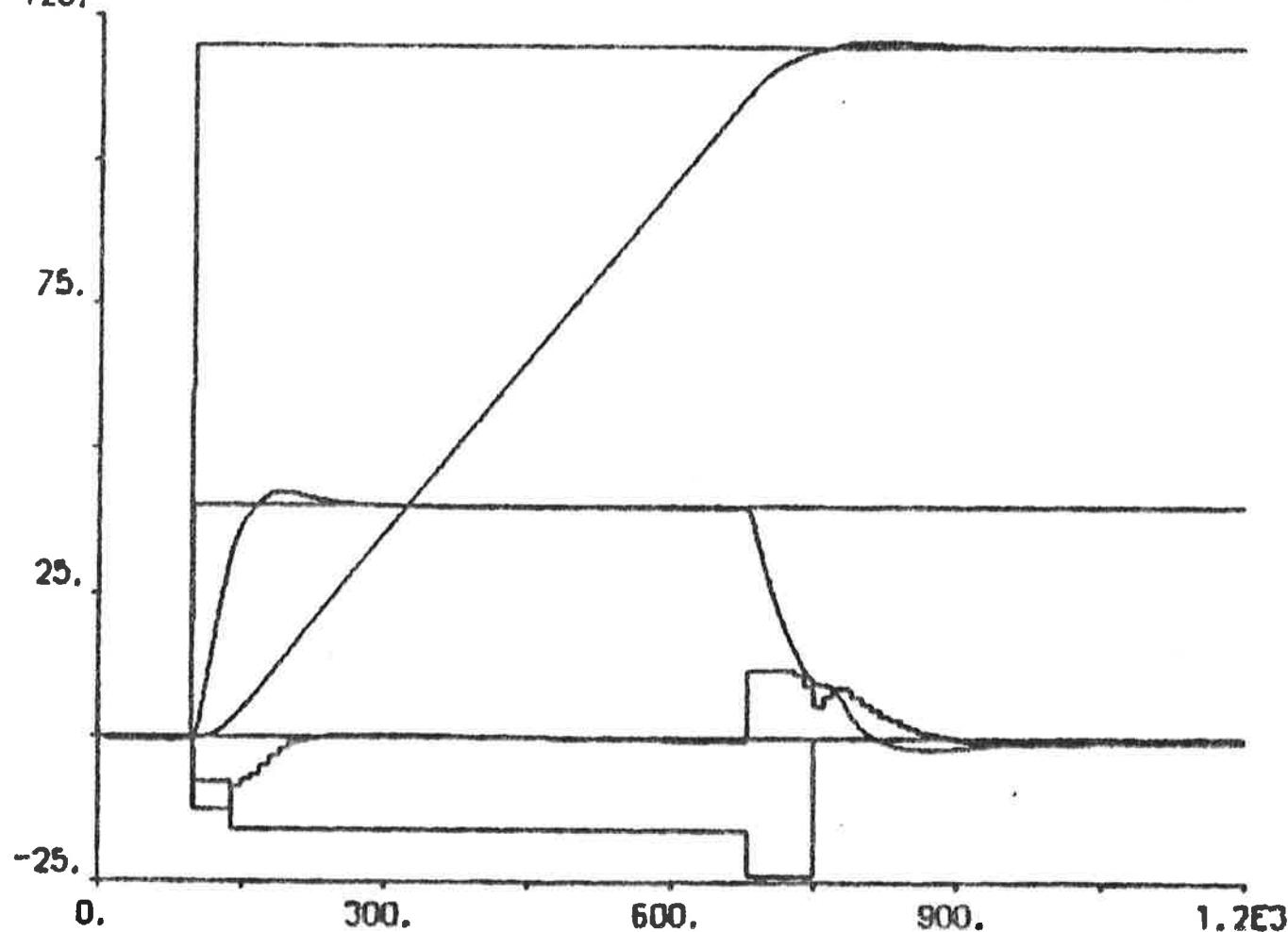


Fig. 5.11 - No disturbances: $T = 22.3$ m, $\Delta\psi_{ref} = 120$ deg,
 $r_{ref} = 0.2$ deg/s.

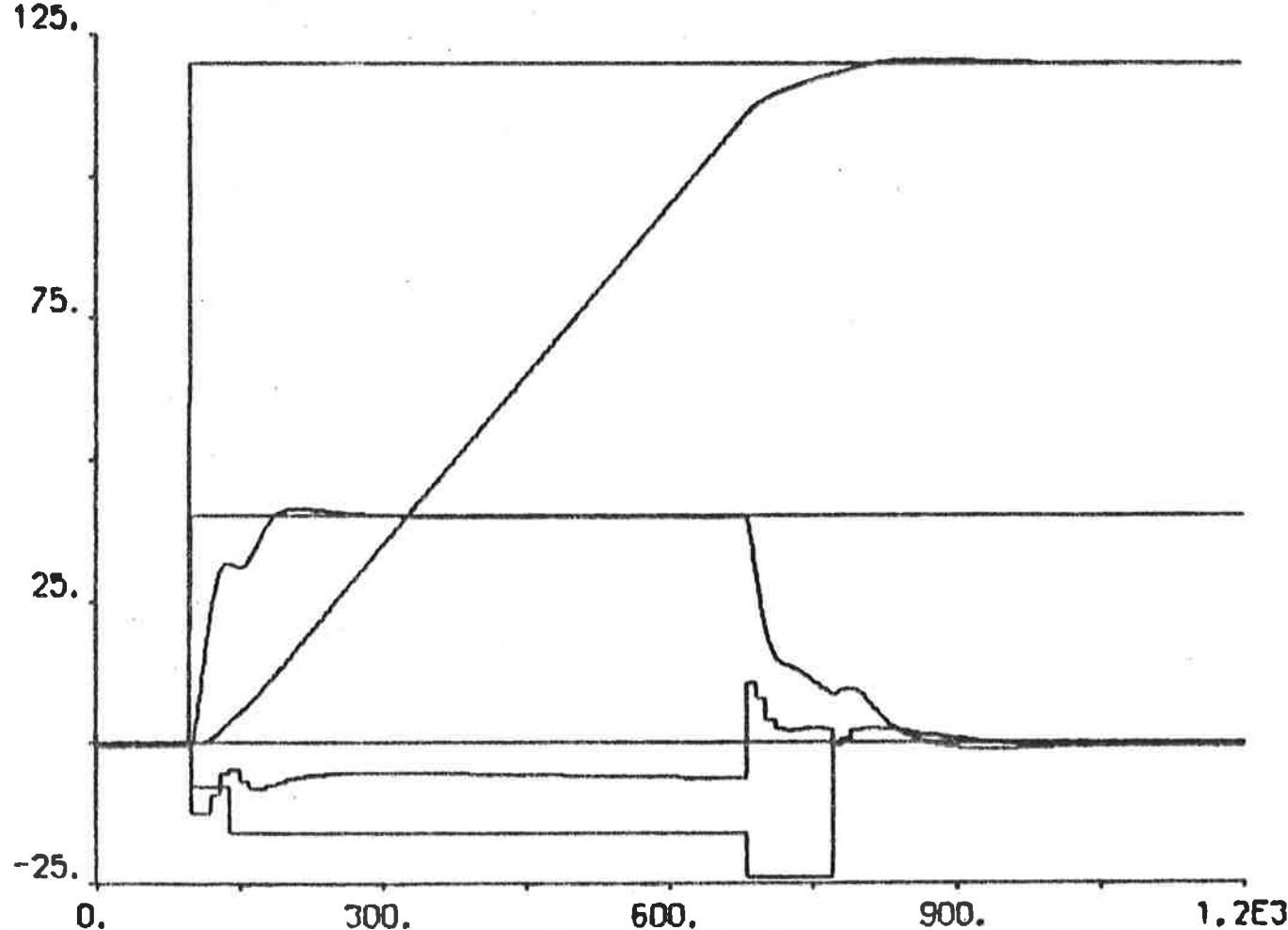
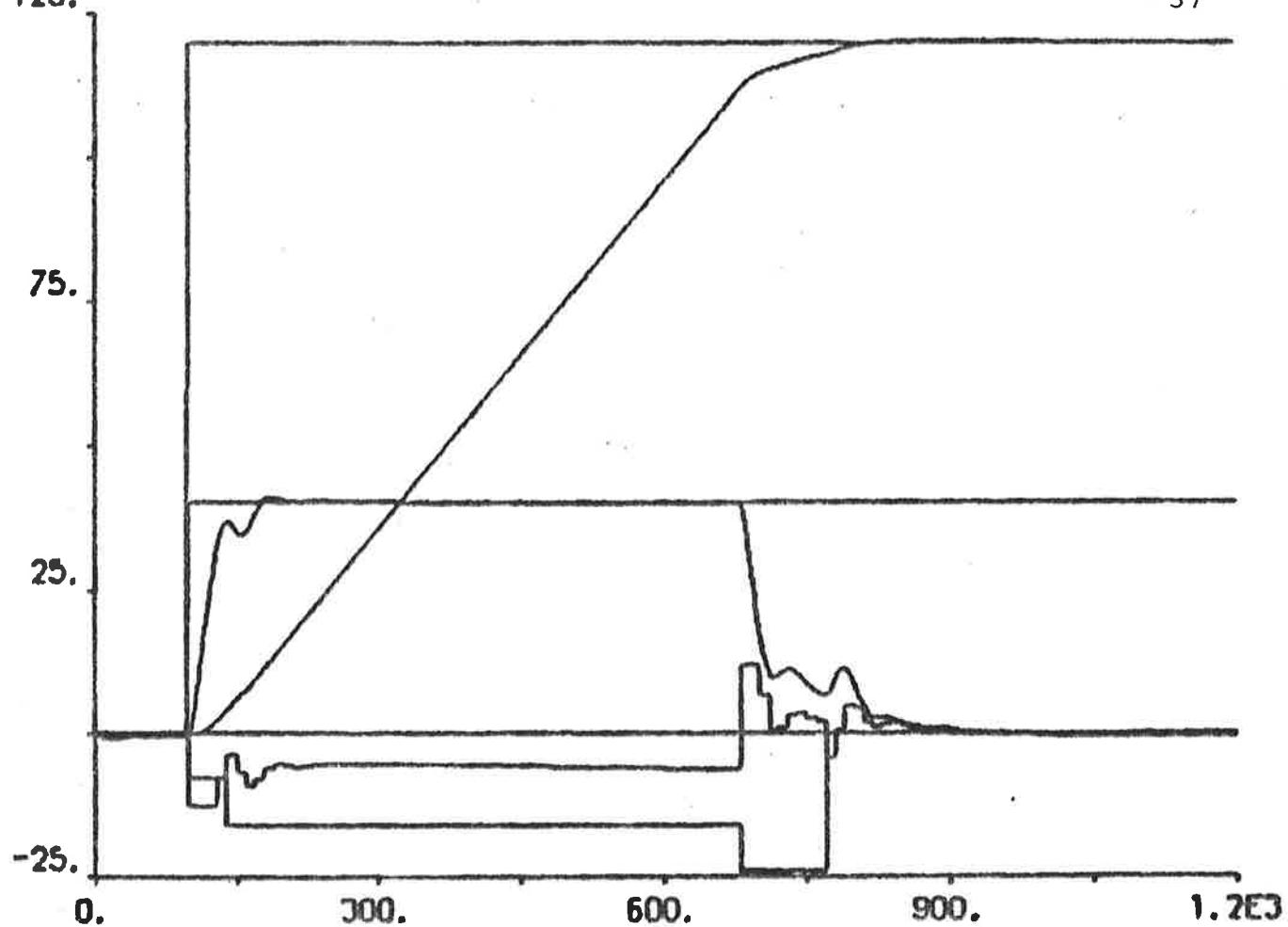


Fig. 5.12 - No disturbances: $T = 10.5 \text{ m}$, $\Delta\psi_{\text{ref}} = 120 \text{ deg}$,
 $r_{\text{ref}} = 0.2 \text{ deg/s}$.

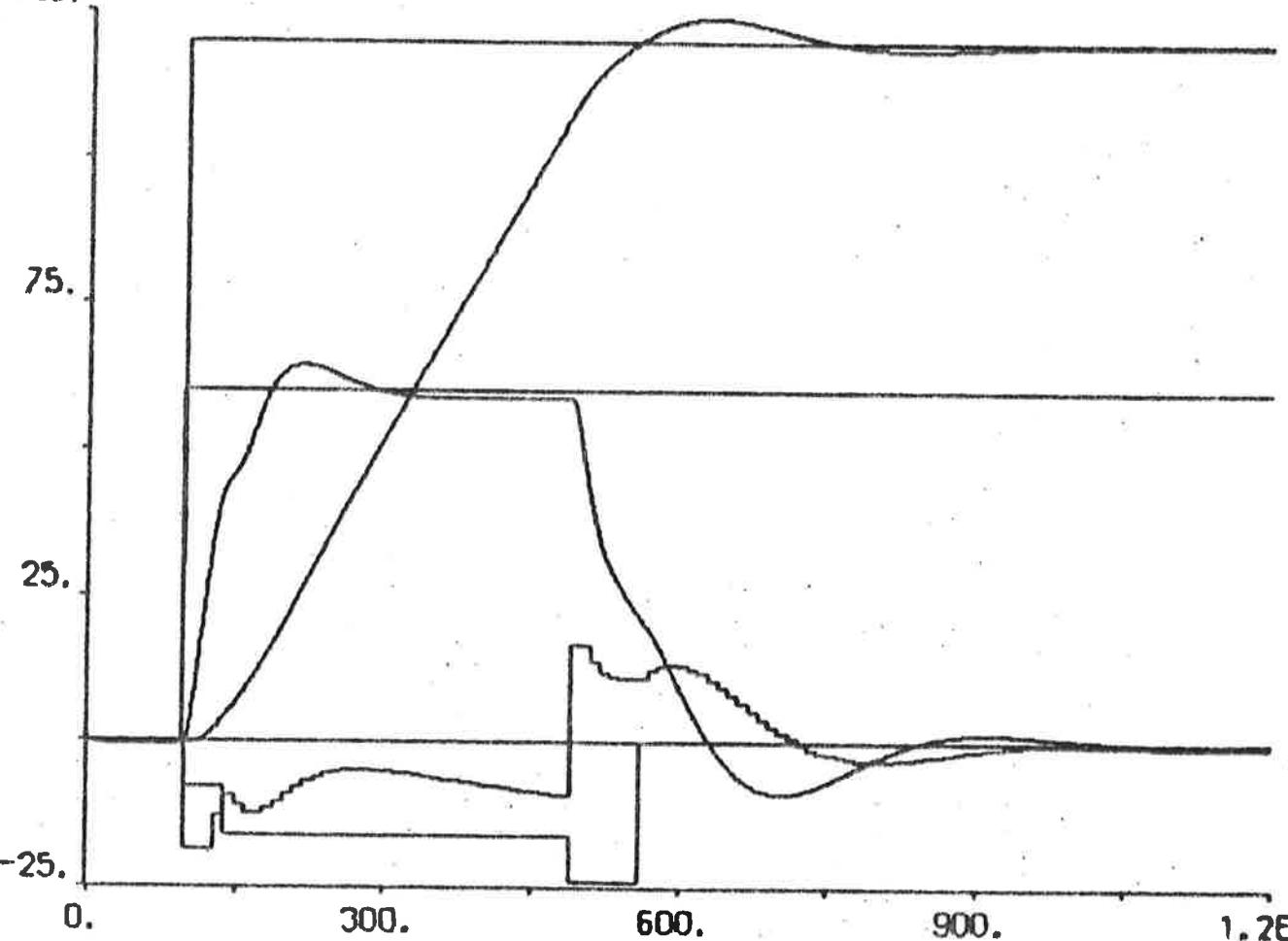
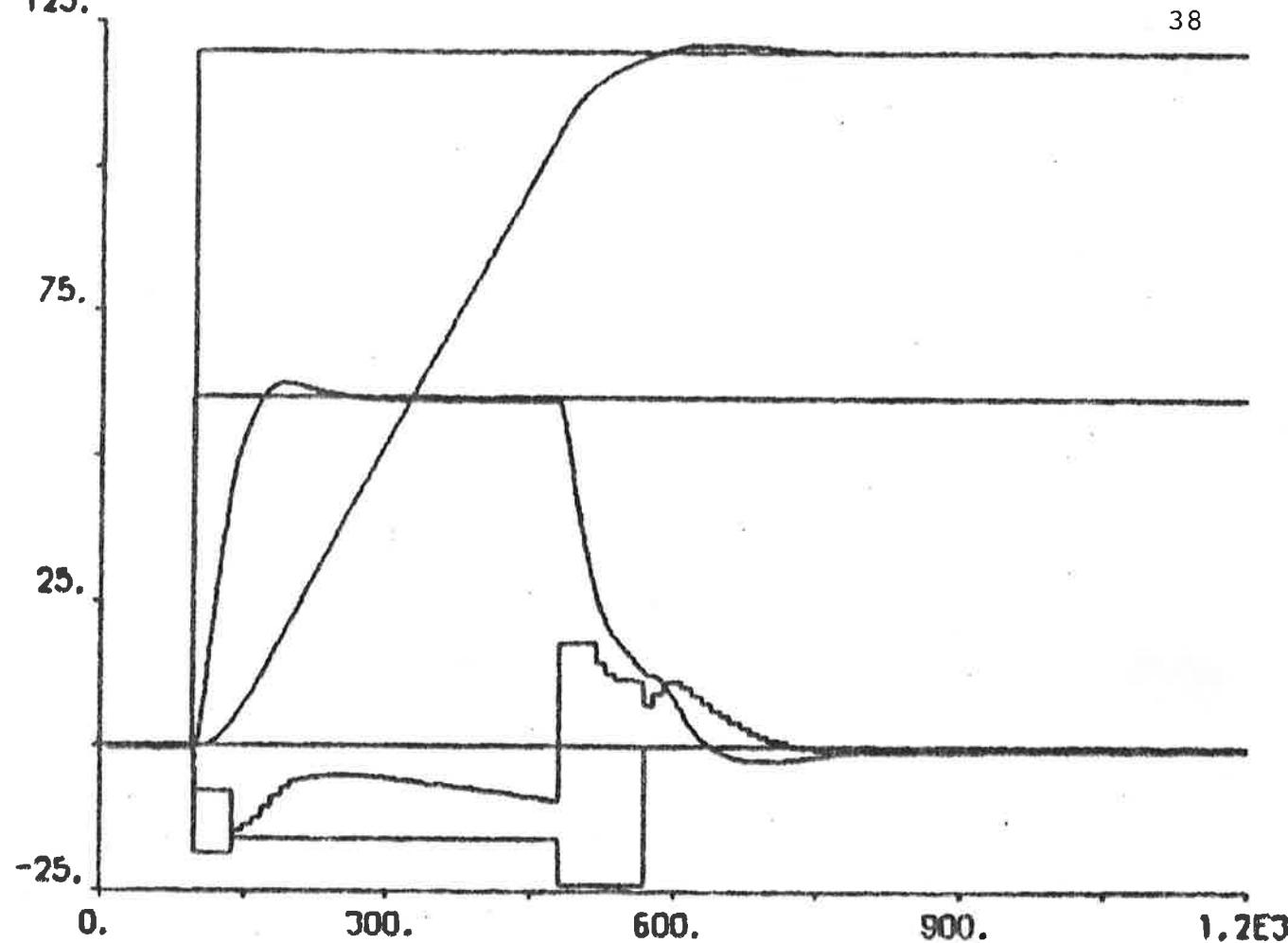


Fig. 5.13 - No disturbances: $T = 22.3$ m, $\Delta\psi_{ref} = 120$ deg,
 $r_{ref} = 0.3$ deg/s.

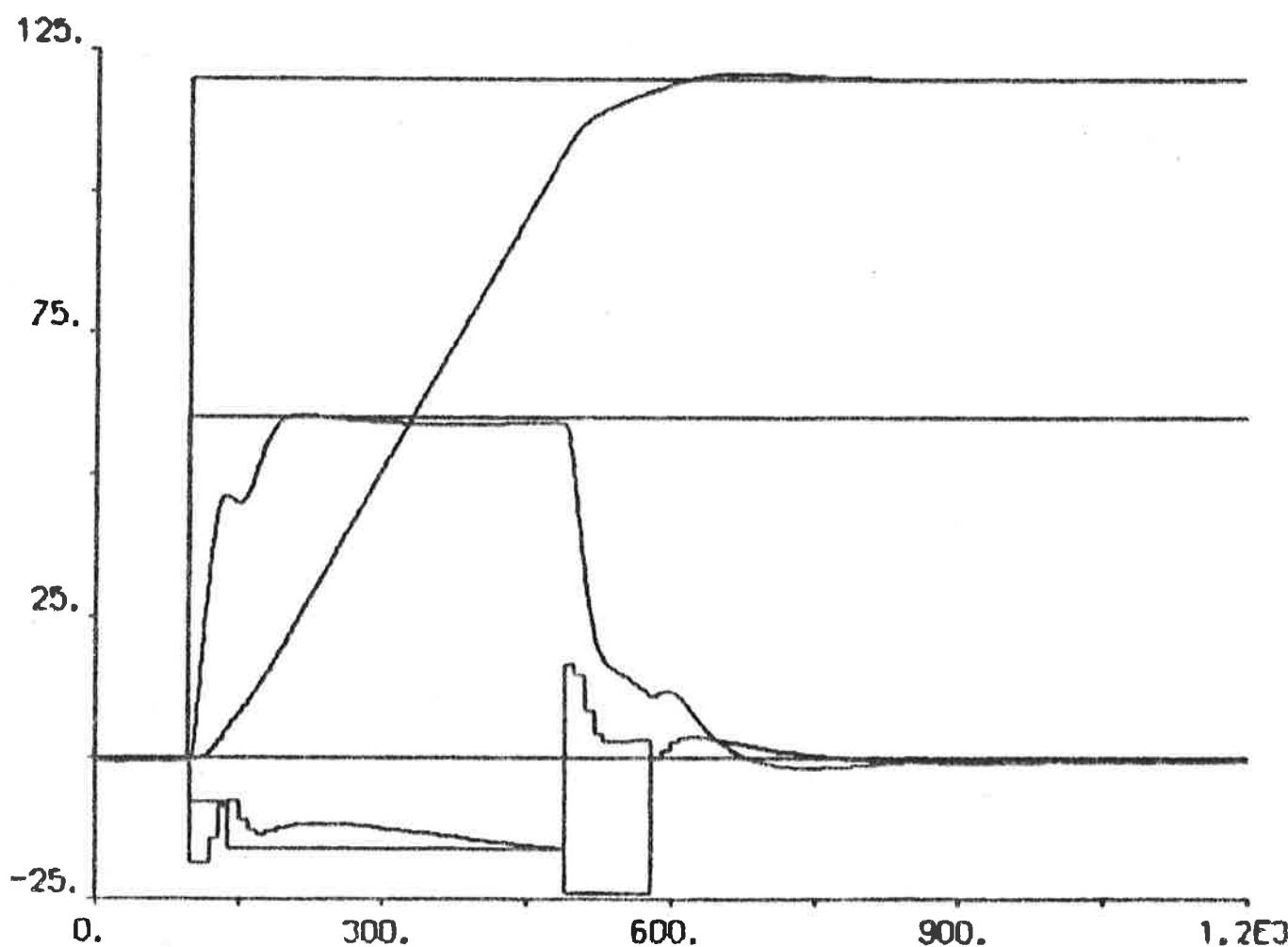
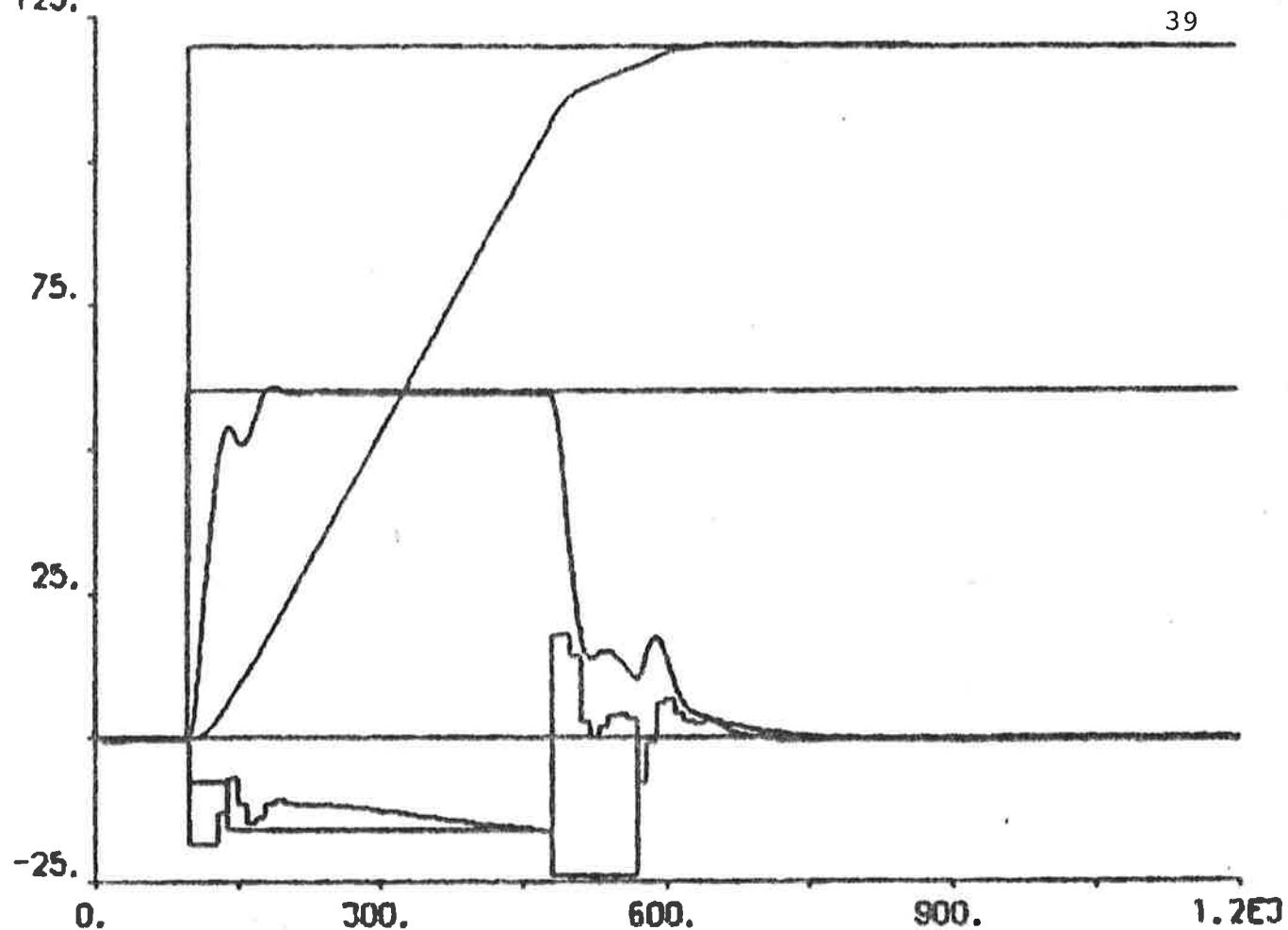


Fig. 5.14 - No disturbances: $T = 10.5$ m, $\Delta\psi_{ref} = 120$ deg,
 $r_{ref} = 0.3$ deg/s.

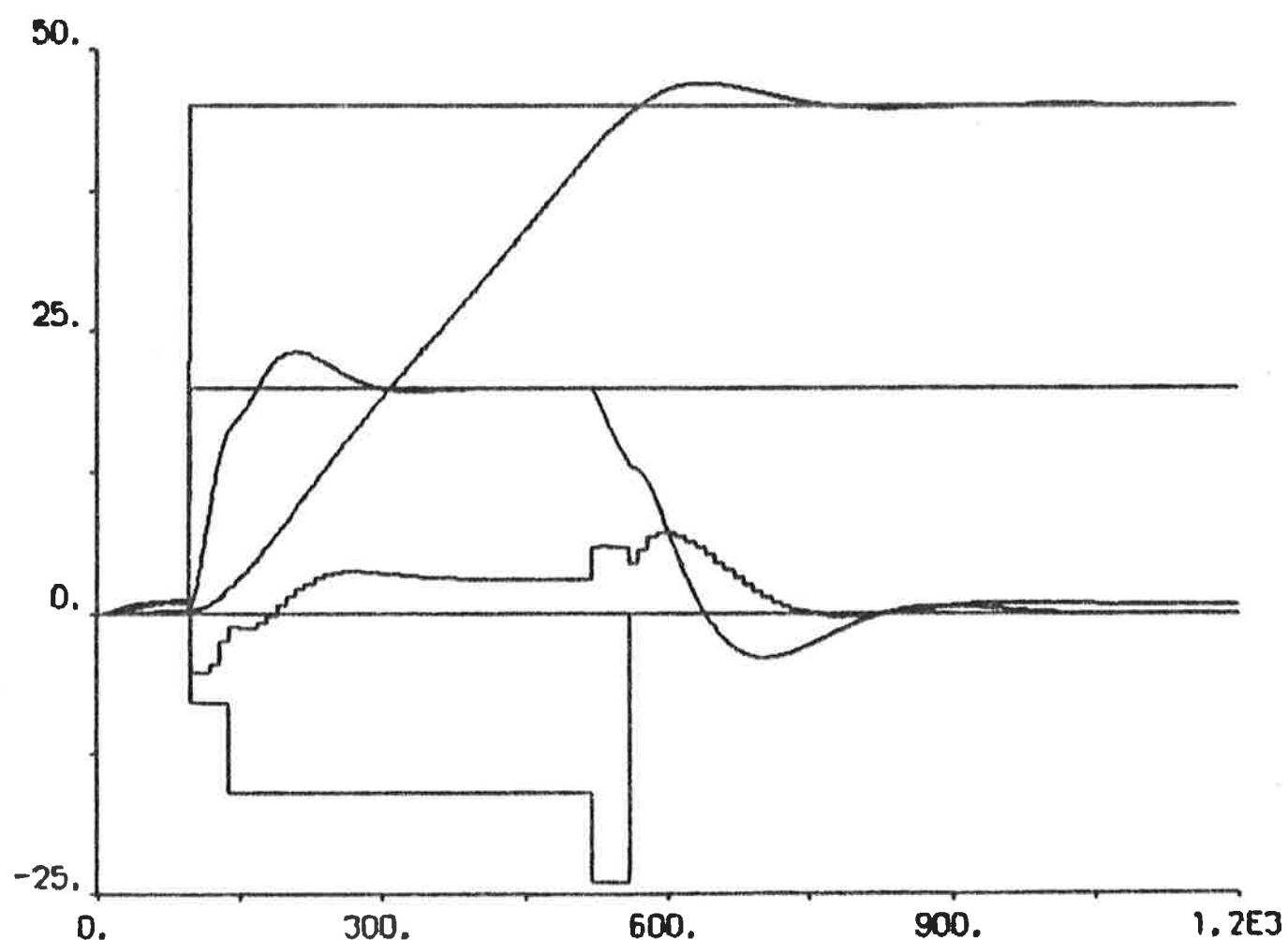
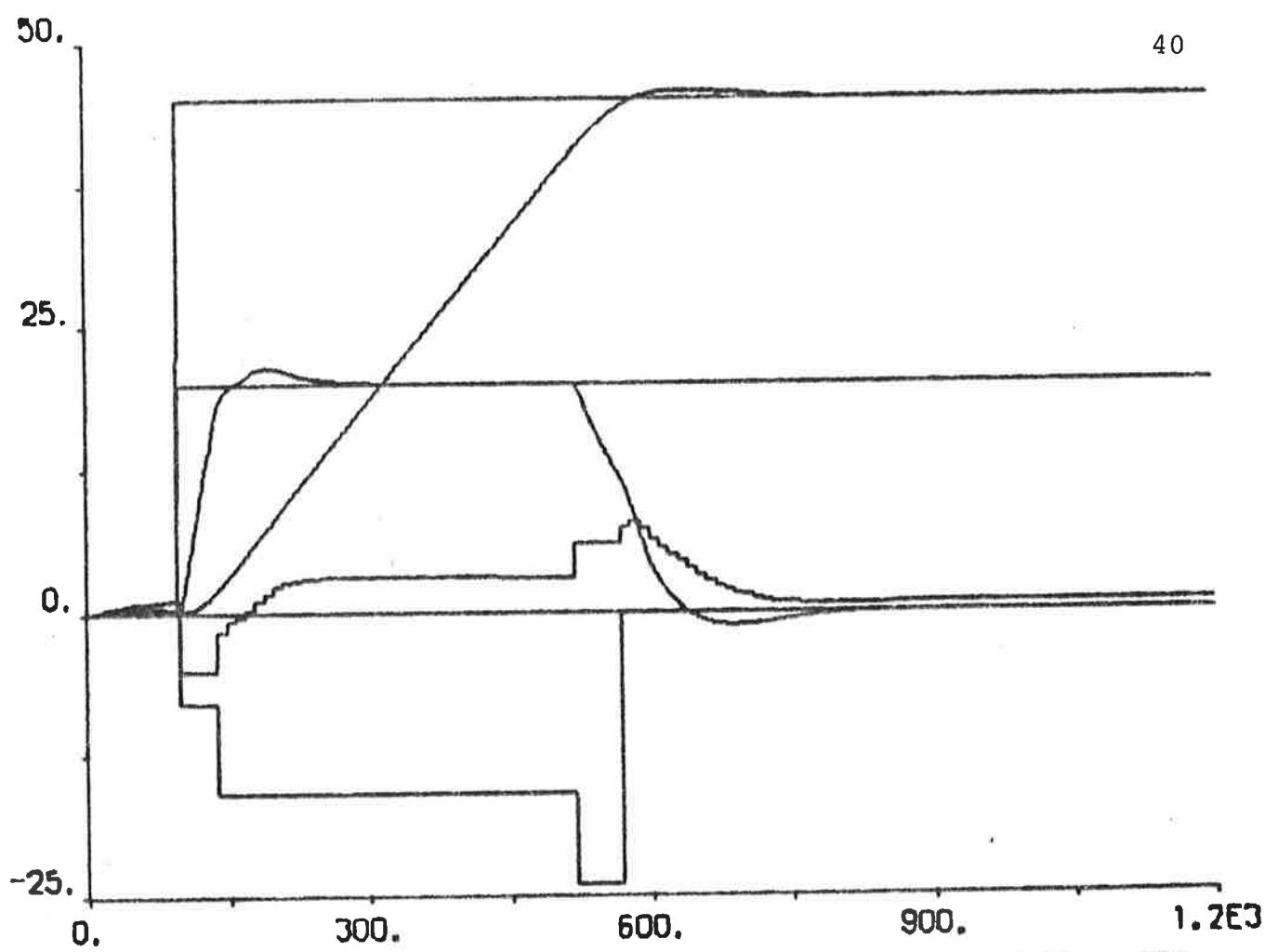


Fig. 5.15 - Constant wind force disturbance: $T = 22.3$ m,
 $\alpha = 90$ deg, $\Delta\psi_{ref} = 45$ deg, $r_{ref} = 0.1$ deg/s.

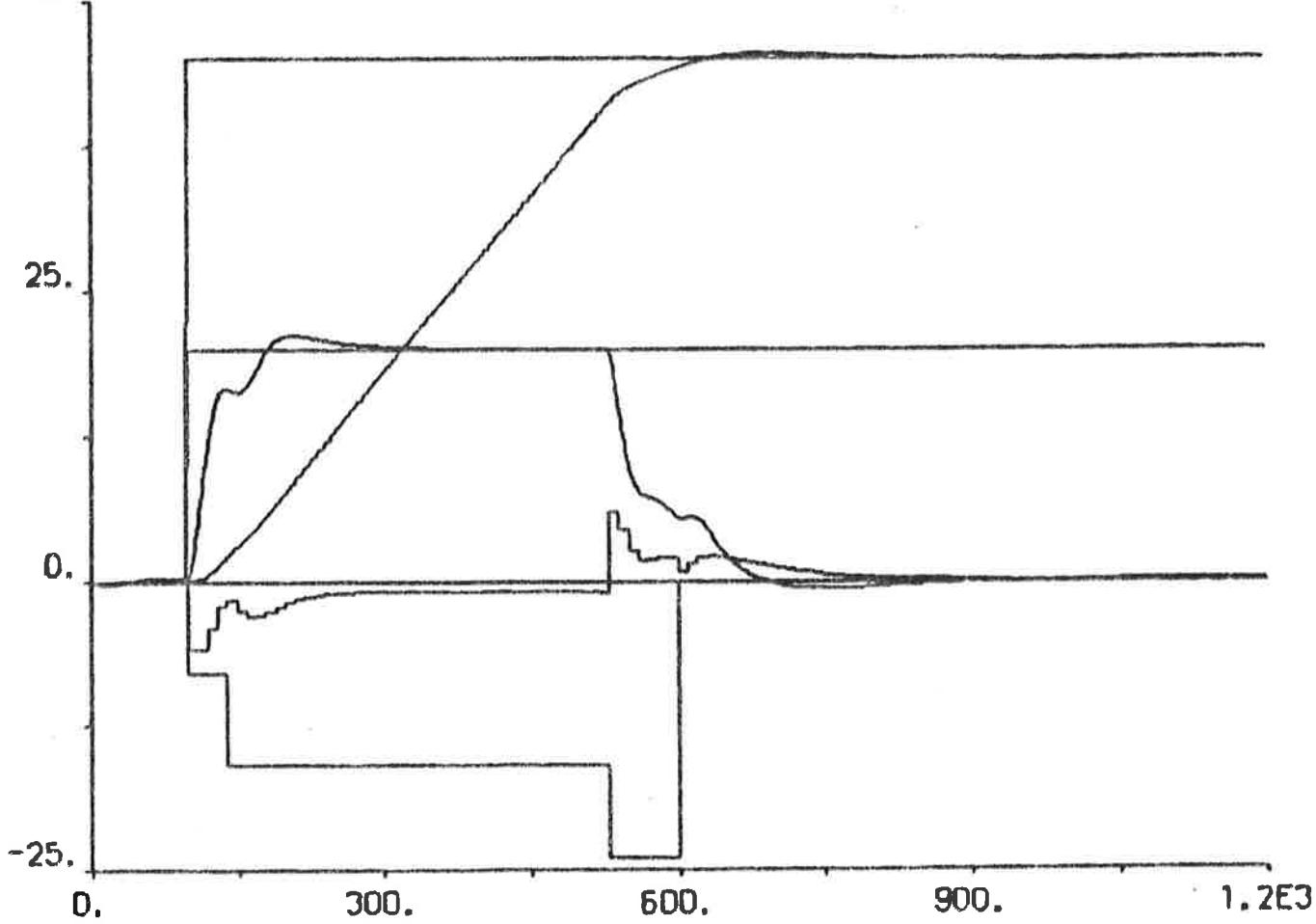
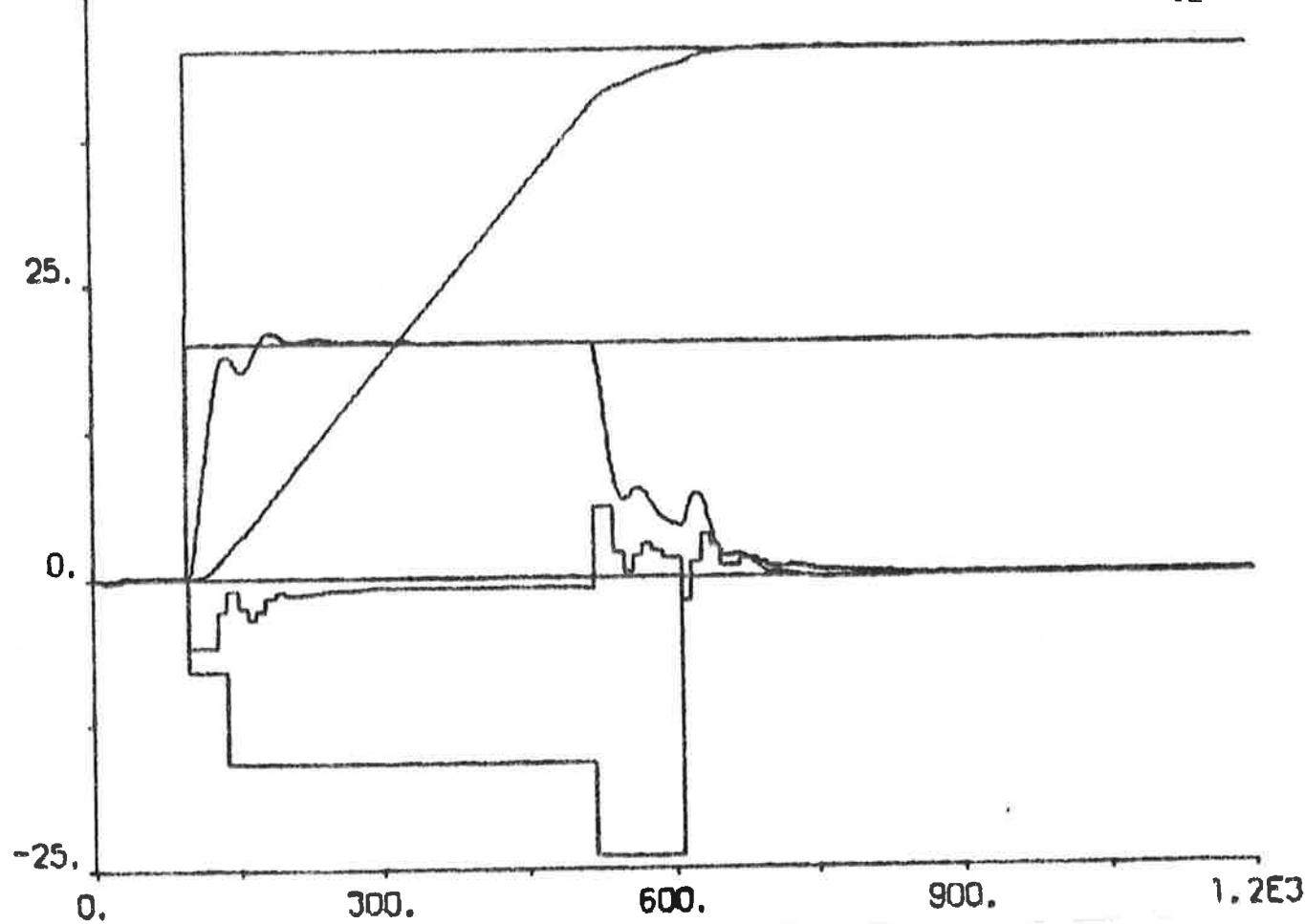


Fig. 5.16 - Constant wind force disturbance: $T = 10.5 \text{ m}$,
 $\alpha = 90 \text{ deg}$, $\Delta\psi_{\text{ref}} = 45 \text{ deg}$, $r_{\text{ref}} = 0.1 \text{ deg/s}$.

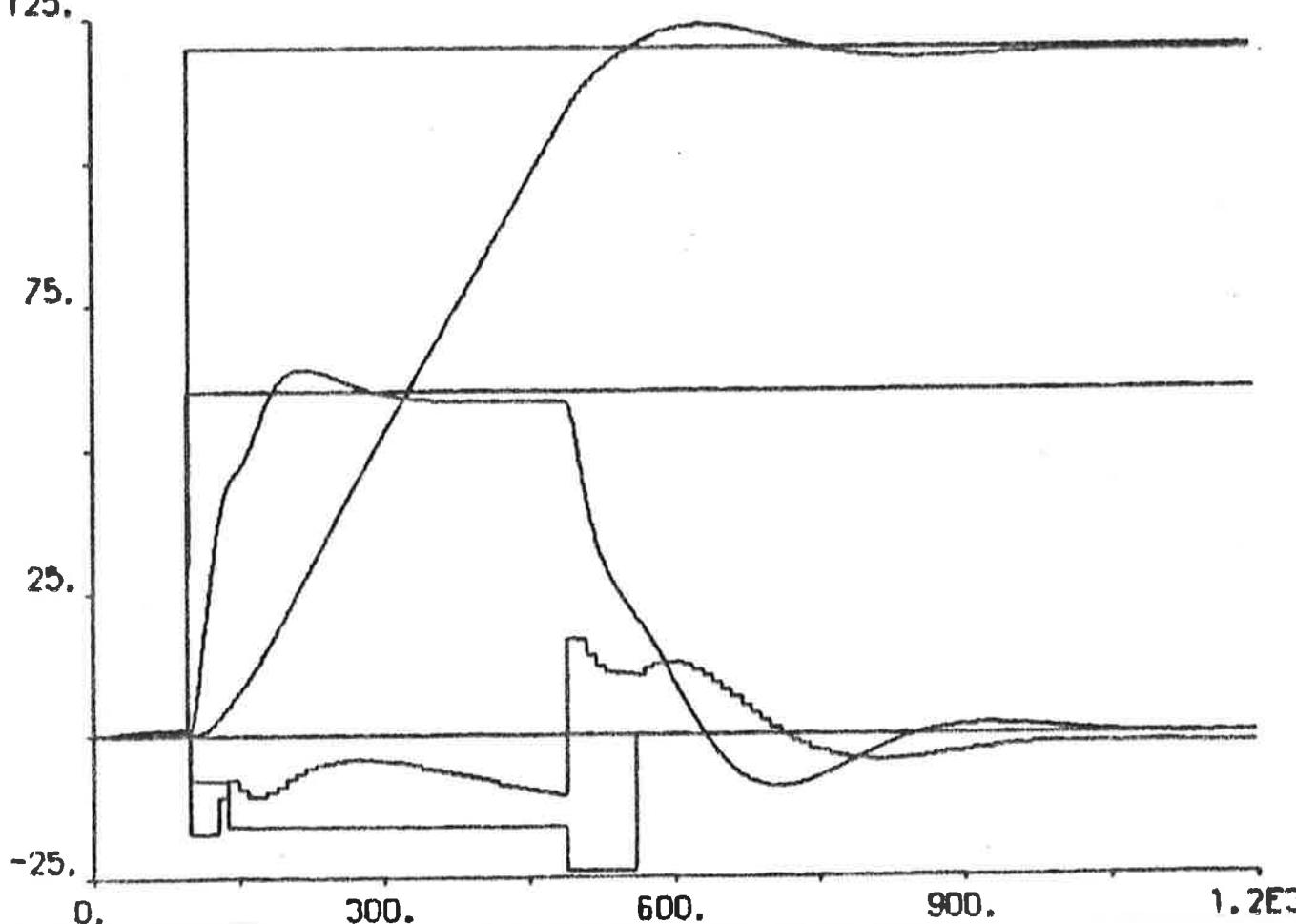
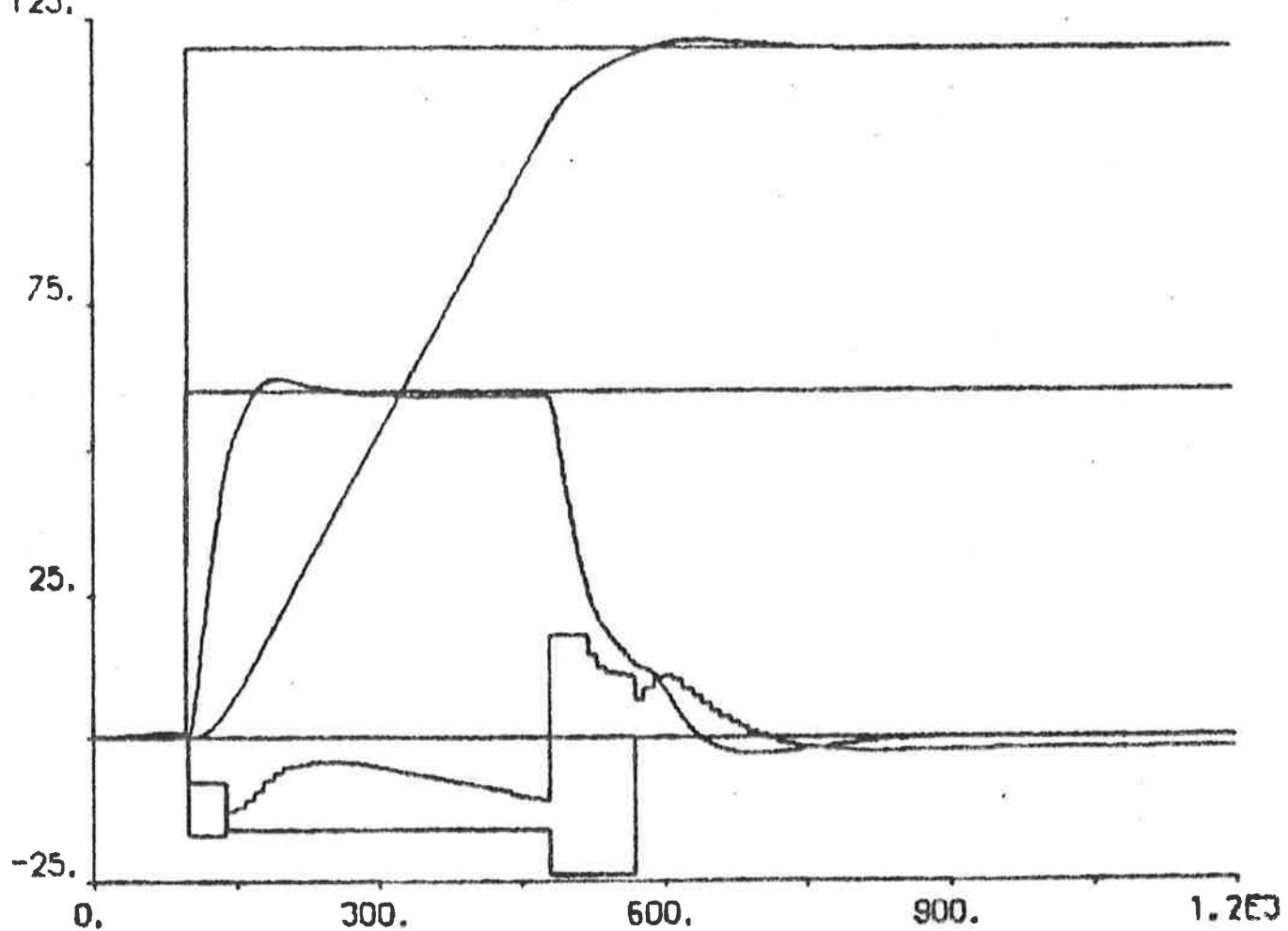


Fig. 5.17 - Constant wind force disturbance: $T = 22.3$ m,
 $\alpha = 90$ deg, $\Delta\psi_{ref} = 120$ deg, $r_{ref} = 0.3$ deg/s.

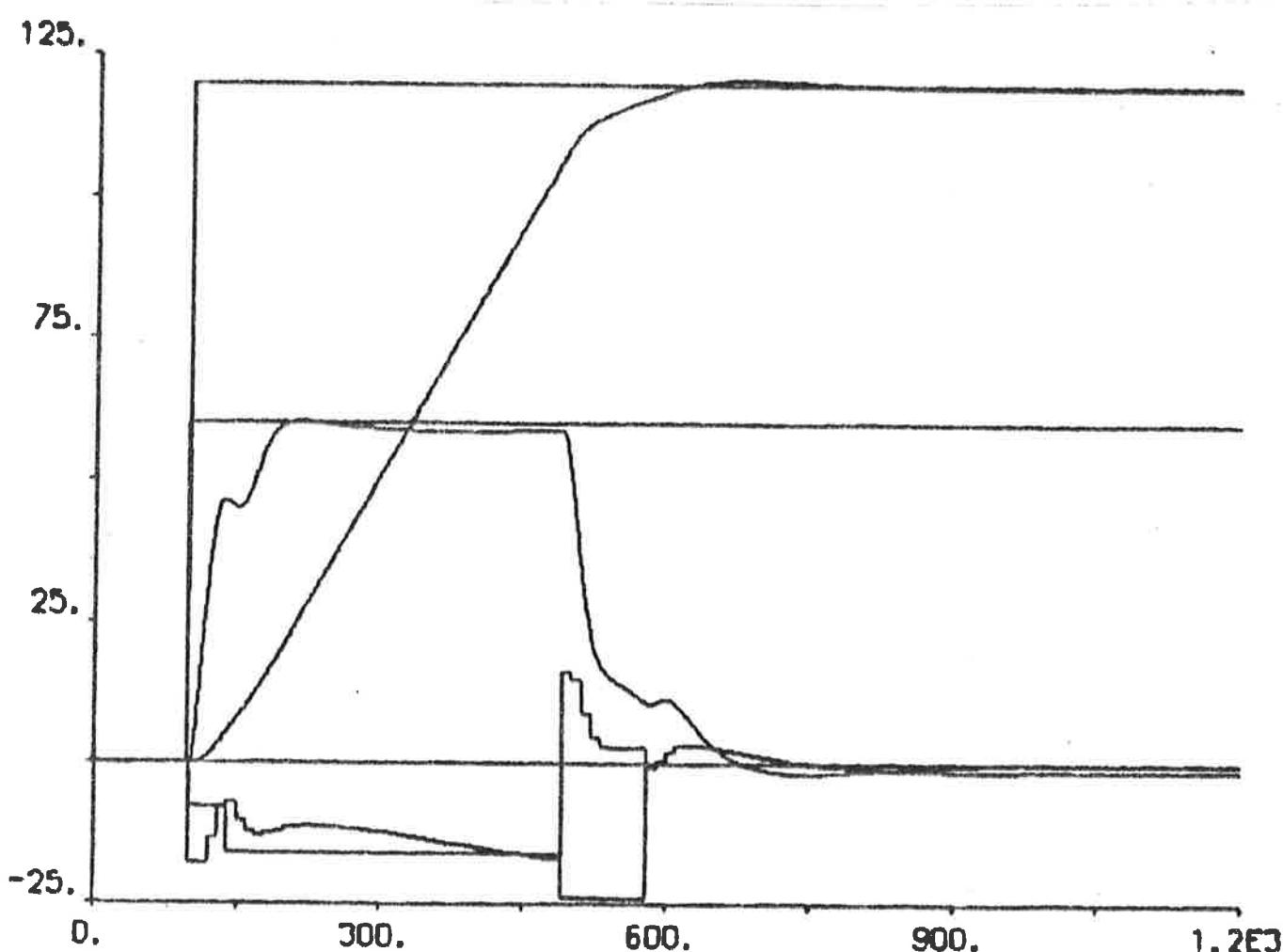
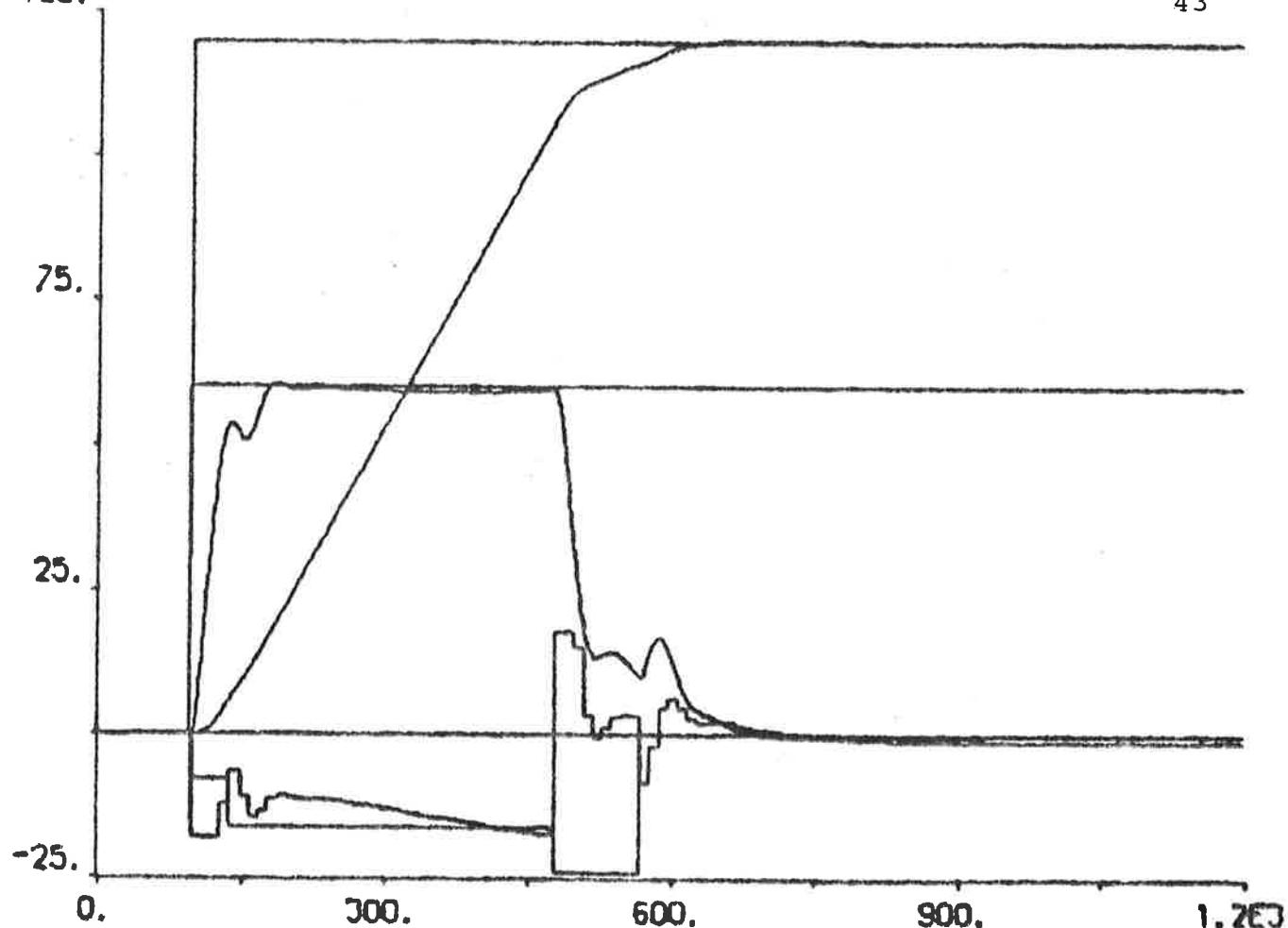


Fig. 5.18 - Constant wind force disturbance: $T = 10.5 \text{ m}$, $\alpha = 90 \text{ deg}$, $\Delta\psi_{\text{ref}} = 120 \text{ deg}$, $r_{\text{ref}} = 0.3 \text{ deg/s}$.

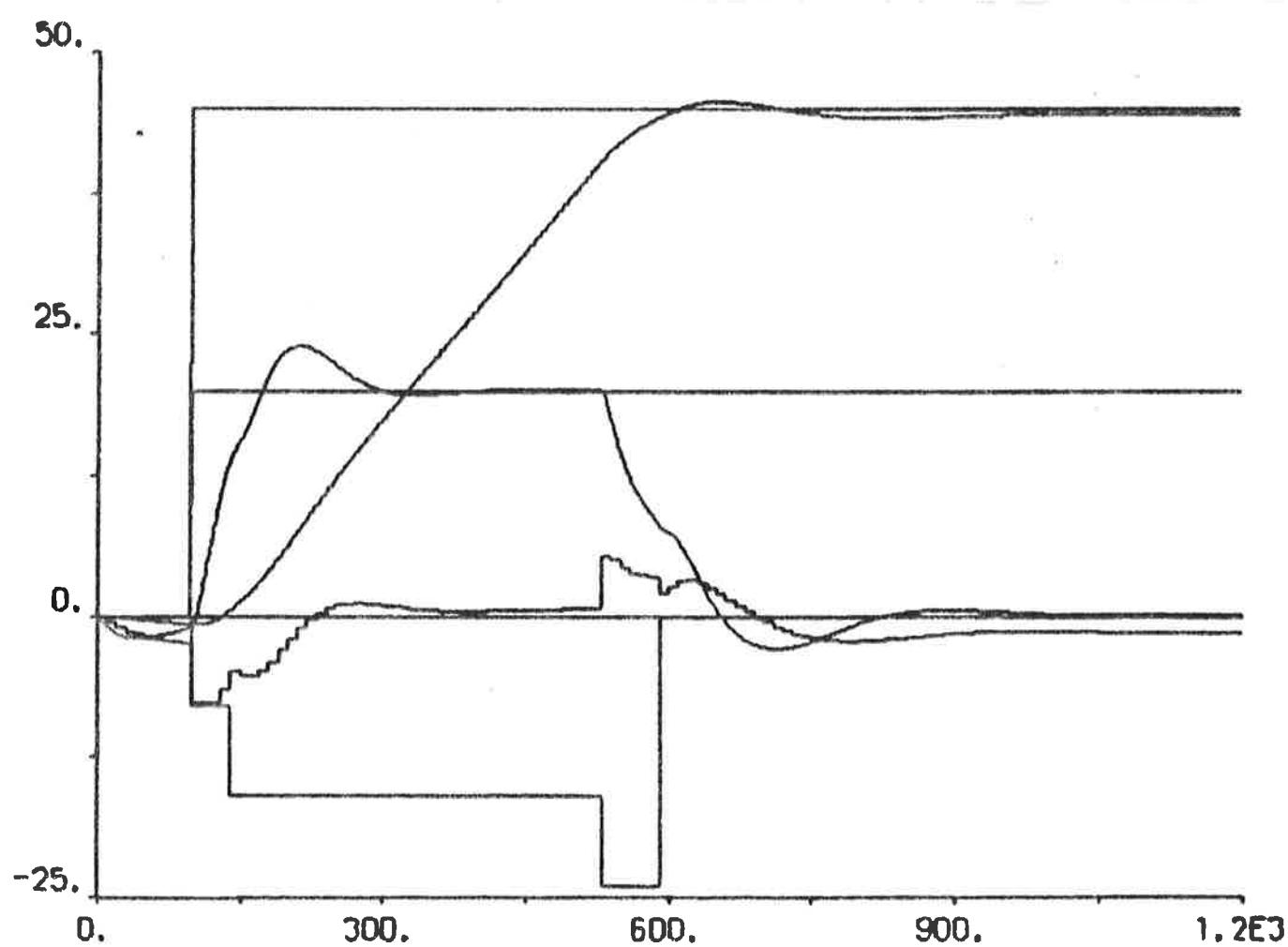
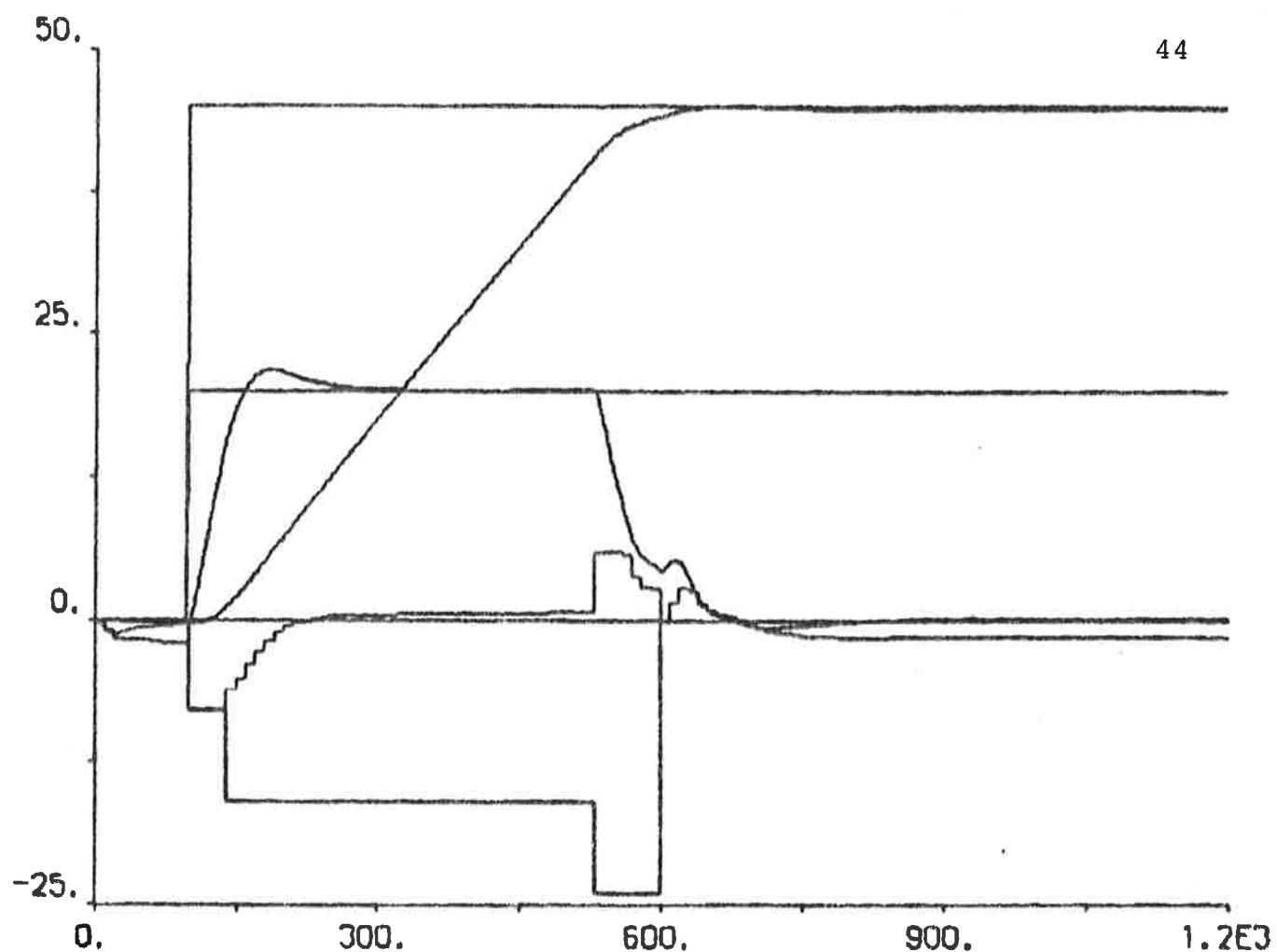
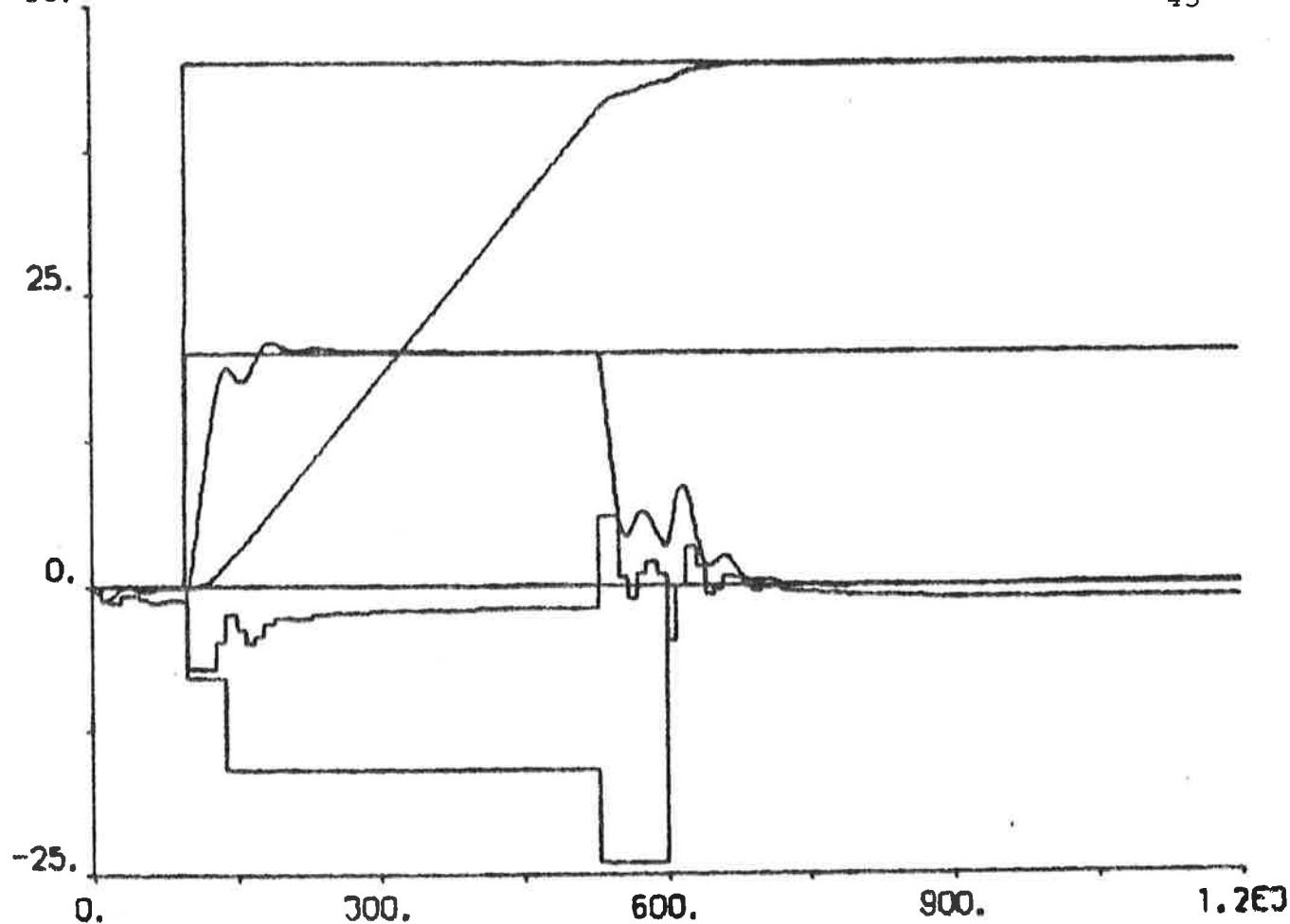


Fig. 5.19 - Constant wind force disturbance: $T = 22.3$ m,
 $\alpha = 270$ deg, $\Delta\psi_{ref} = 45$ deg, $r_{ref} = 0.1$ deg/s.



50.

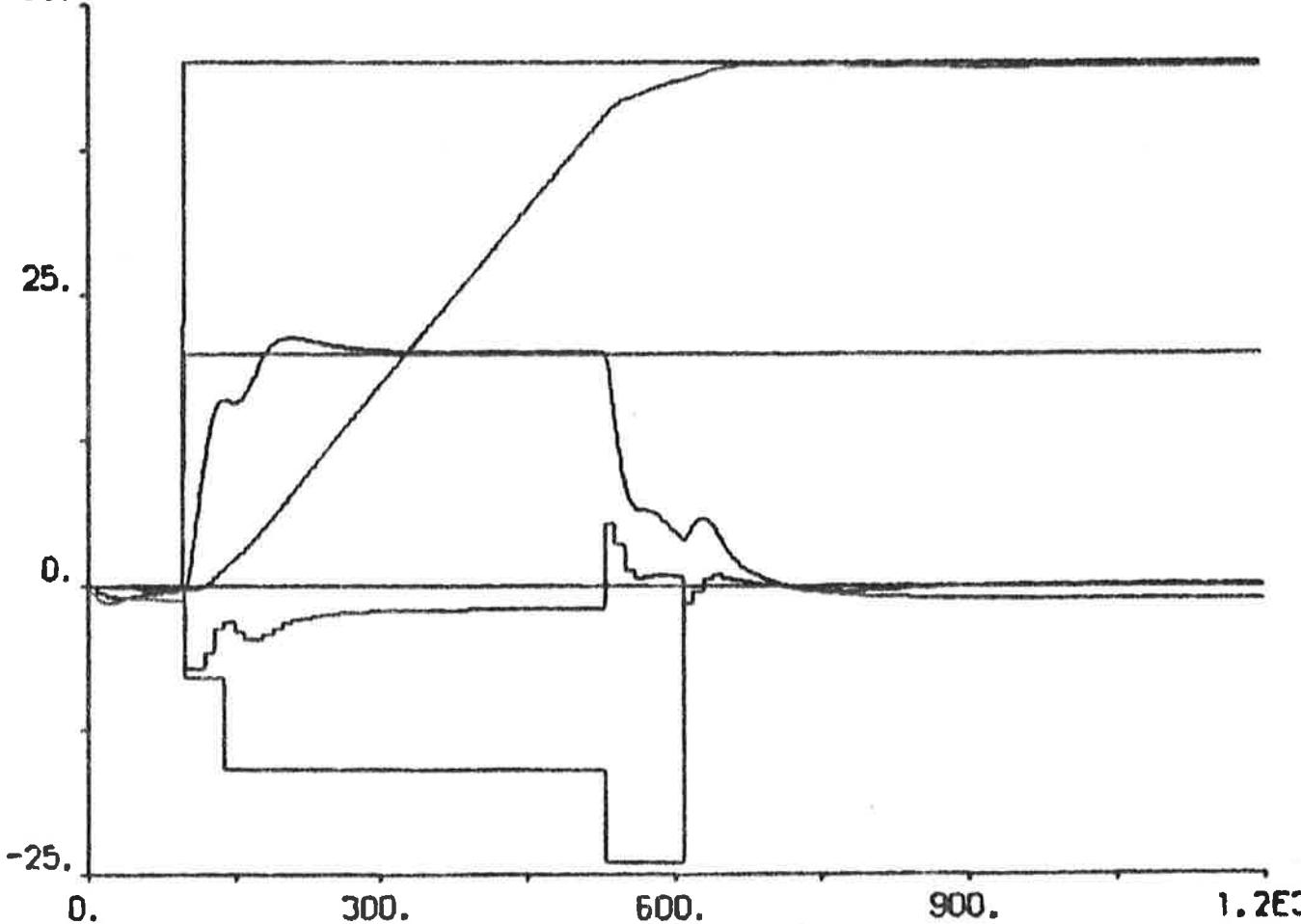
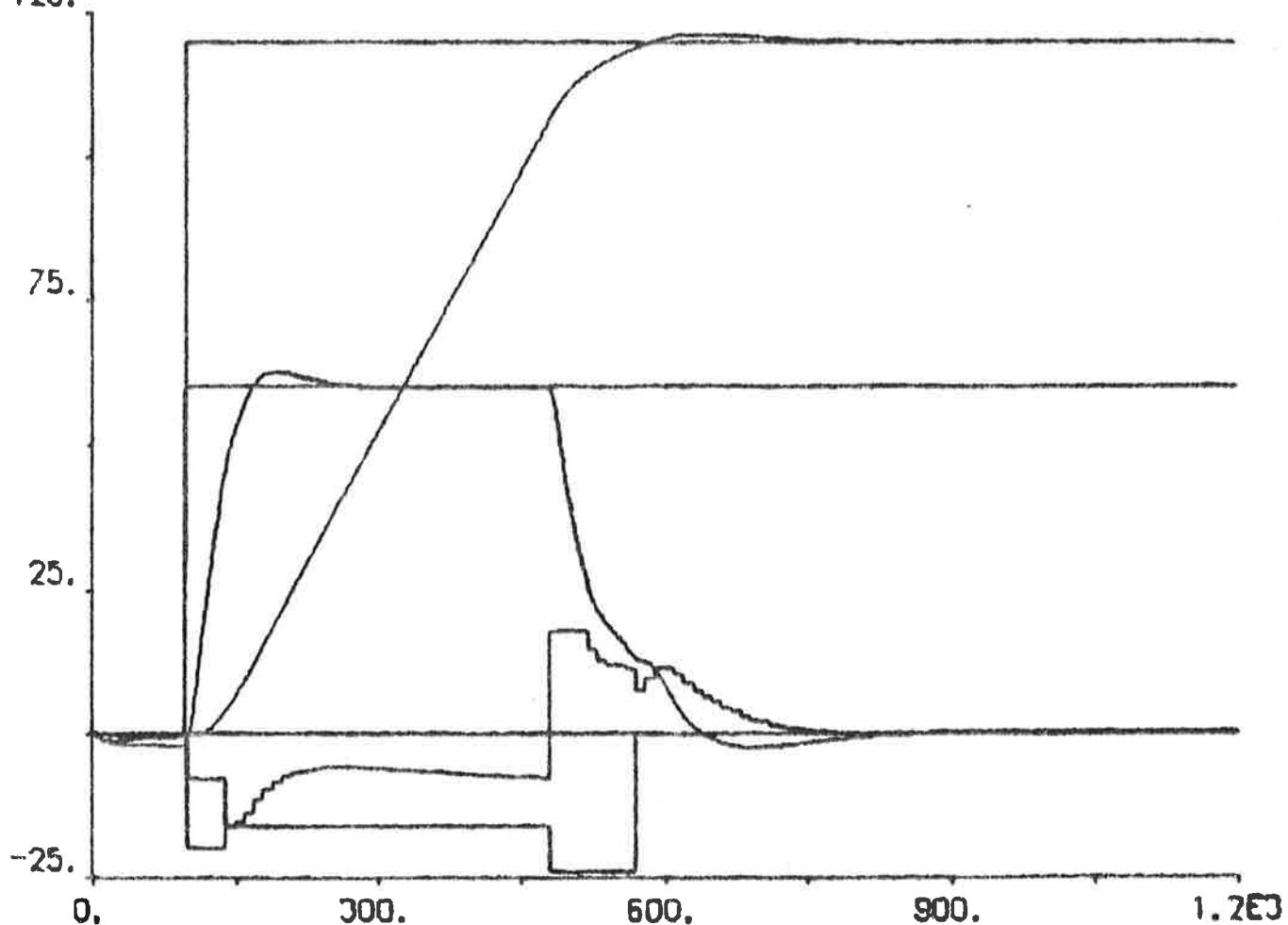


Fig. 5.20 - Constant wind force disturbance: $T = 10.5 \text{ m}$,
 $\alpha = 270 \text{ deg}$, $\Delta\psi_{\text{ref}} = 45 \text{ deg}$, $r_{\text{ref}} = 0.1 \text{ deg/s}$.



125.

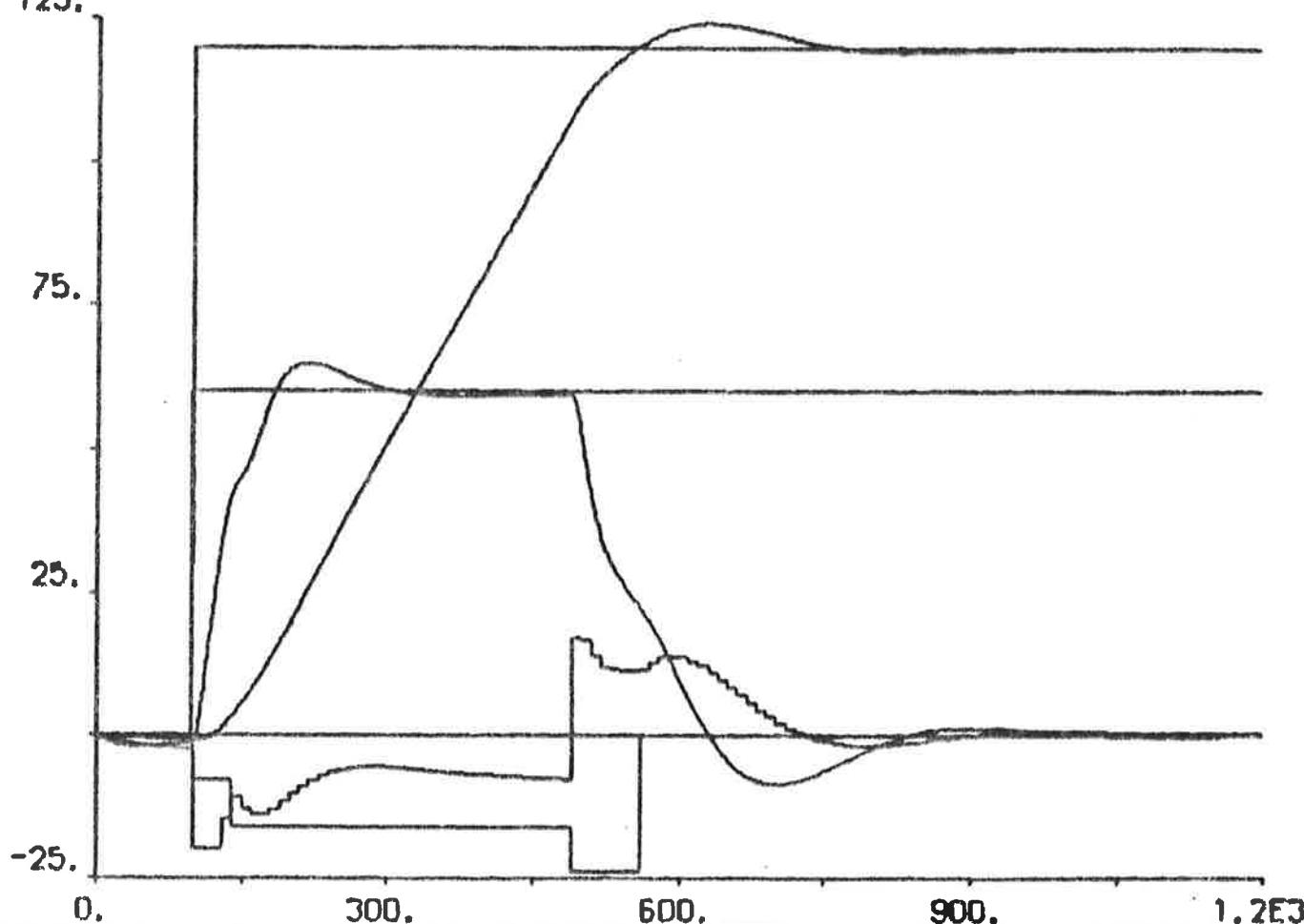


Fig. 5.21 - Constant wind force disturbance: $T = 22.3 \text{ m}$,
 $\alpha = 270 \text{ deg}$, $\Delta\psi_{\text{ref}} = 120 \text{ deg}$, $r_{\text{ref}} = 0.3 \text{ deg/s}$.

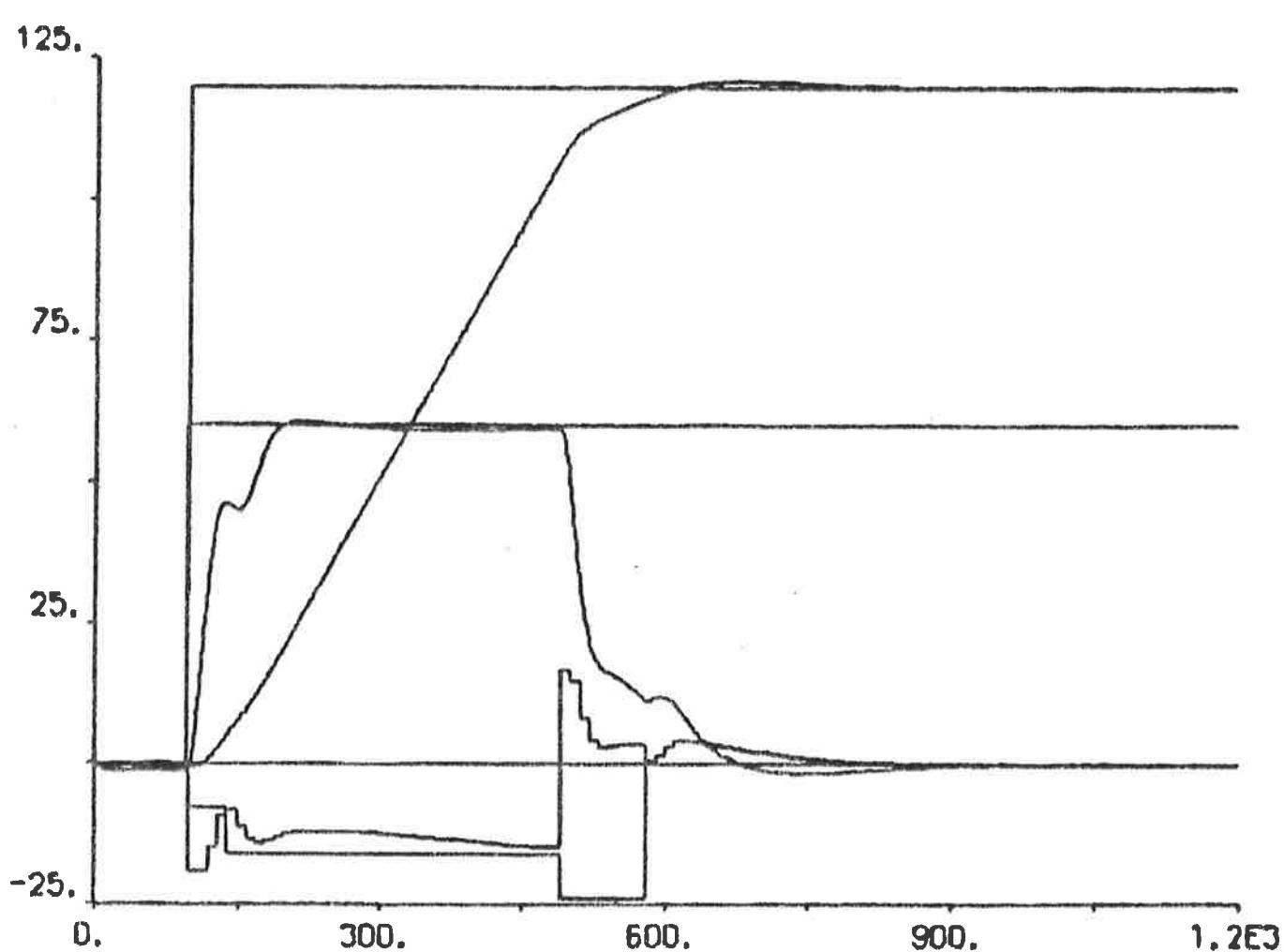
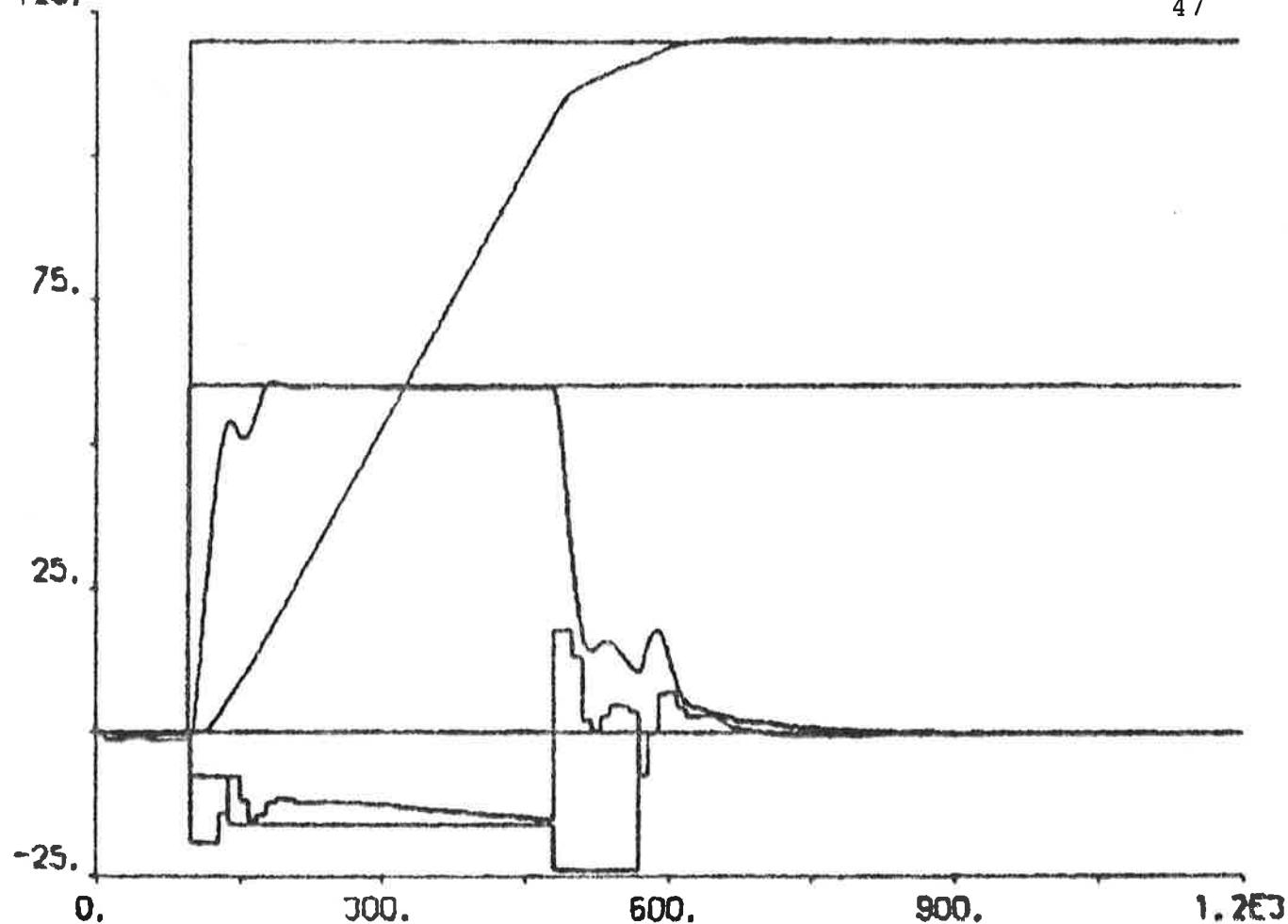


Fig. 5.22 - Constant wind force disturbance: $T = 10.5 \text{ m}$, $\alpha = 270 \text{ deg}$, $\Delta\psi_{\text{ref}} = 120 \text{ deg}$, $r_{\text{ref}} = 0.3 \text{ deg/s}$.

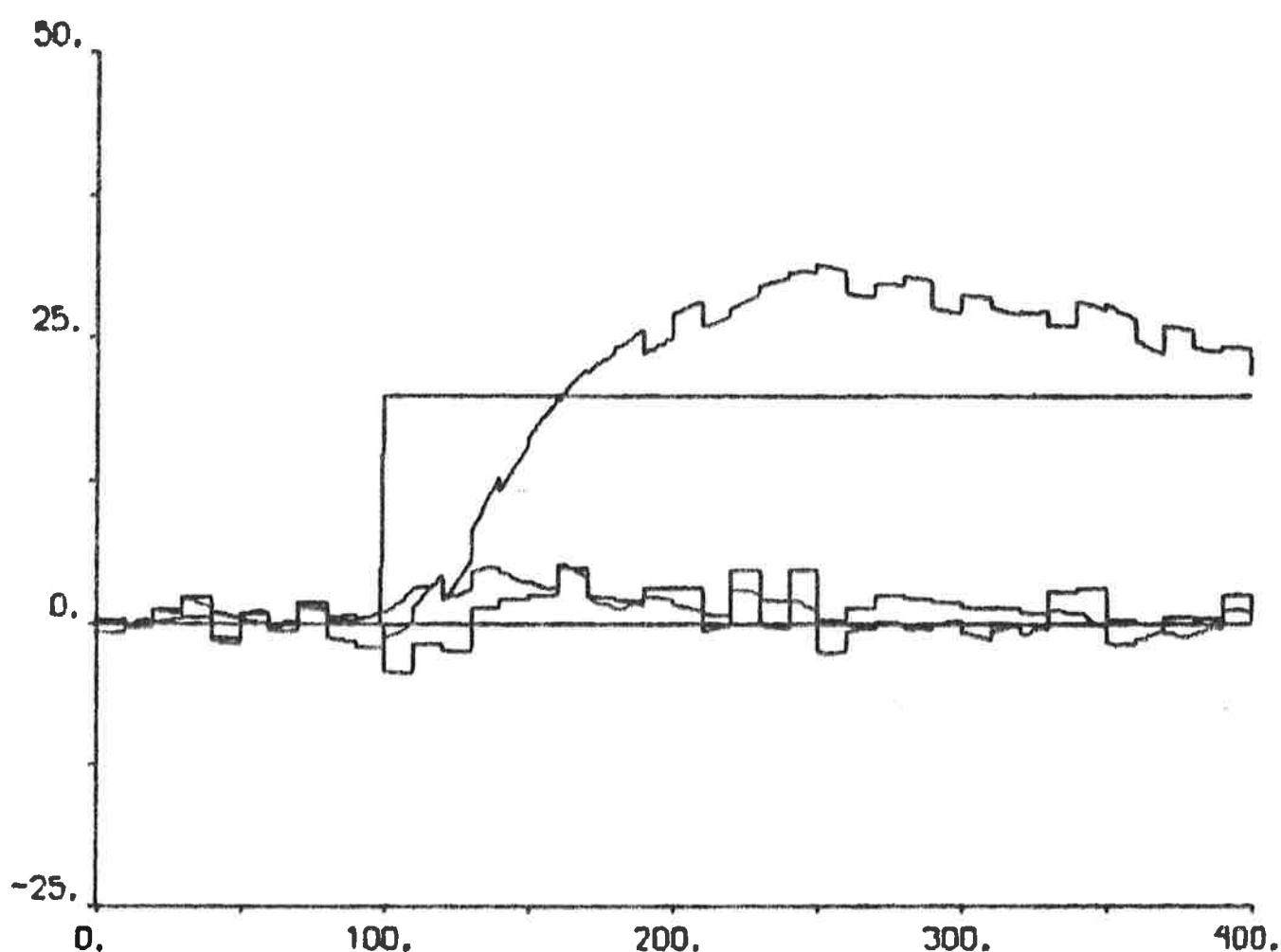
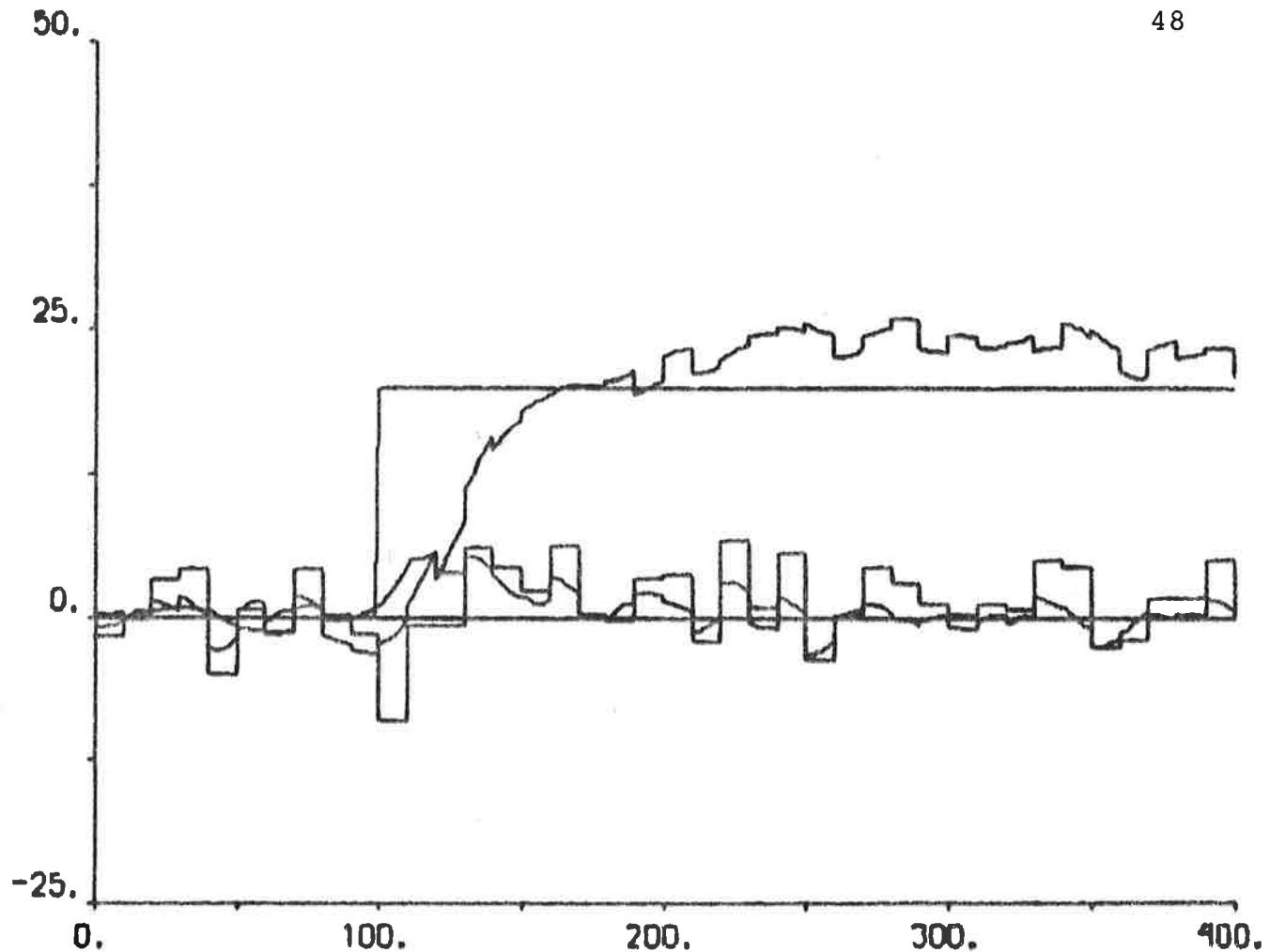


Fig. 5.23 - Stochastic disturbances: $T = 22.3$ m, $\alpha = 90$ deg,
 $\sigma_r = 0.01$ deg/s, $\Delta\psi_{ref} = 2$ deg.

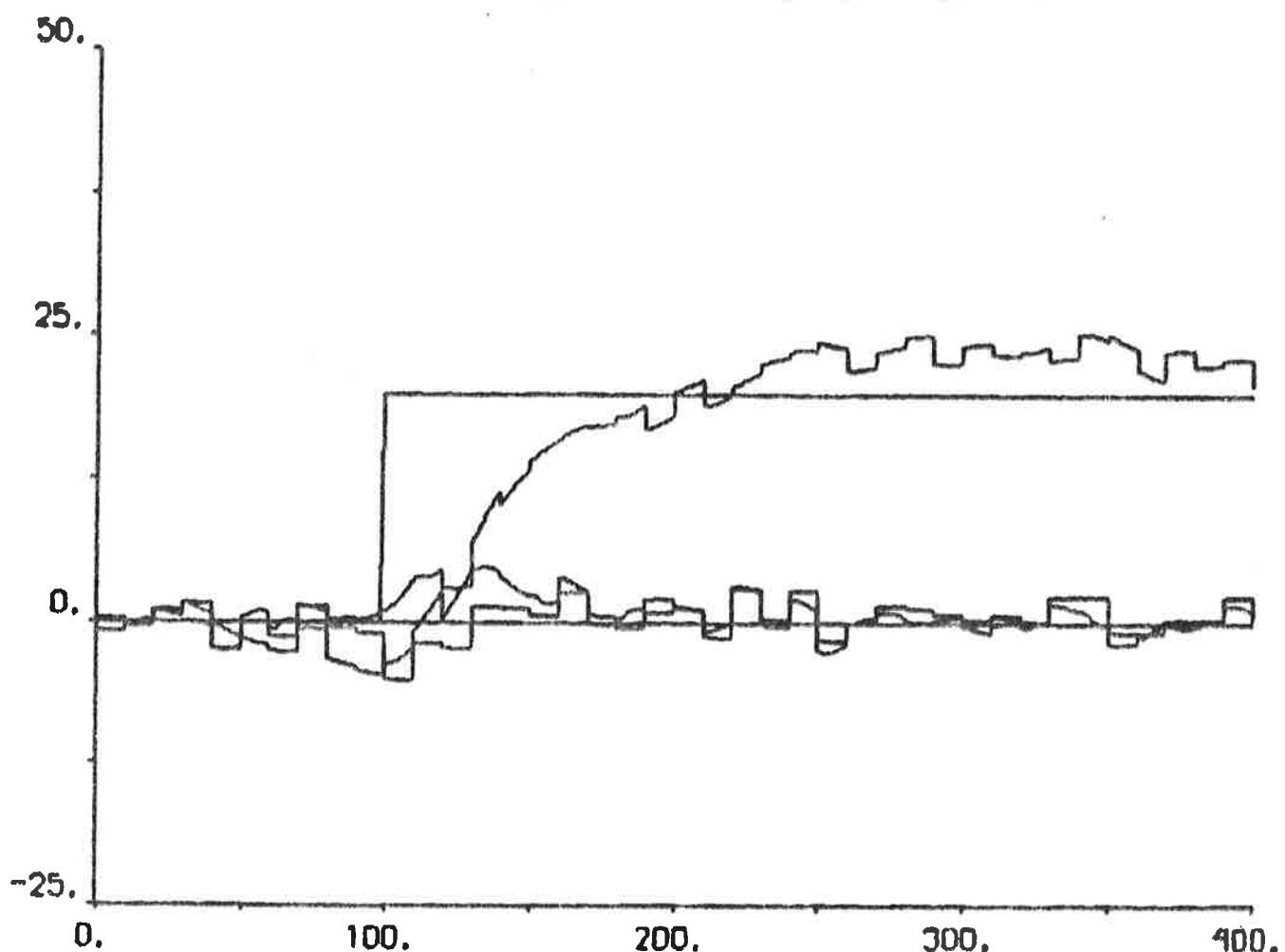
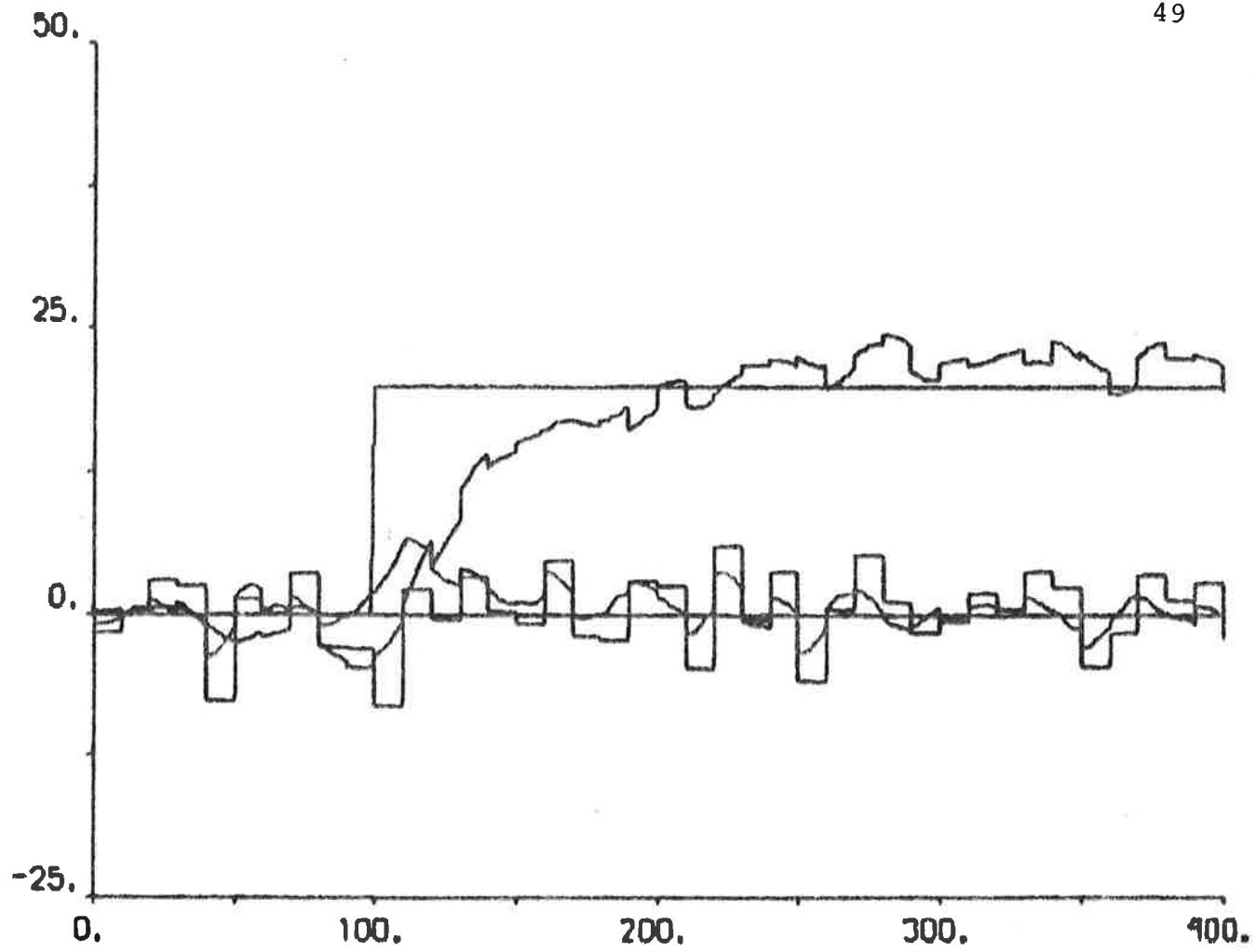


Fig. 5.24 - Stochastic disturbances: $T = 10.5 \text{ m}$, $\alpha = 90 \text{ deg}$,
 $\sigma_r = 0.01 \text{ deg/s}$, $\Delta\psi_{\text{ref}} = 2 \text{ deg}$.

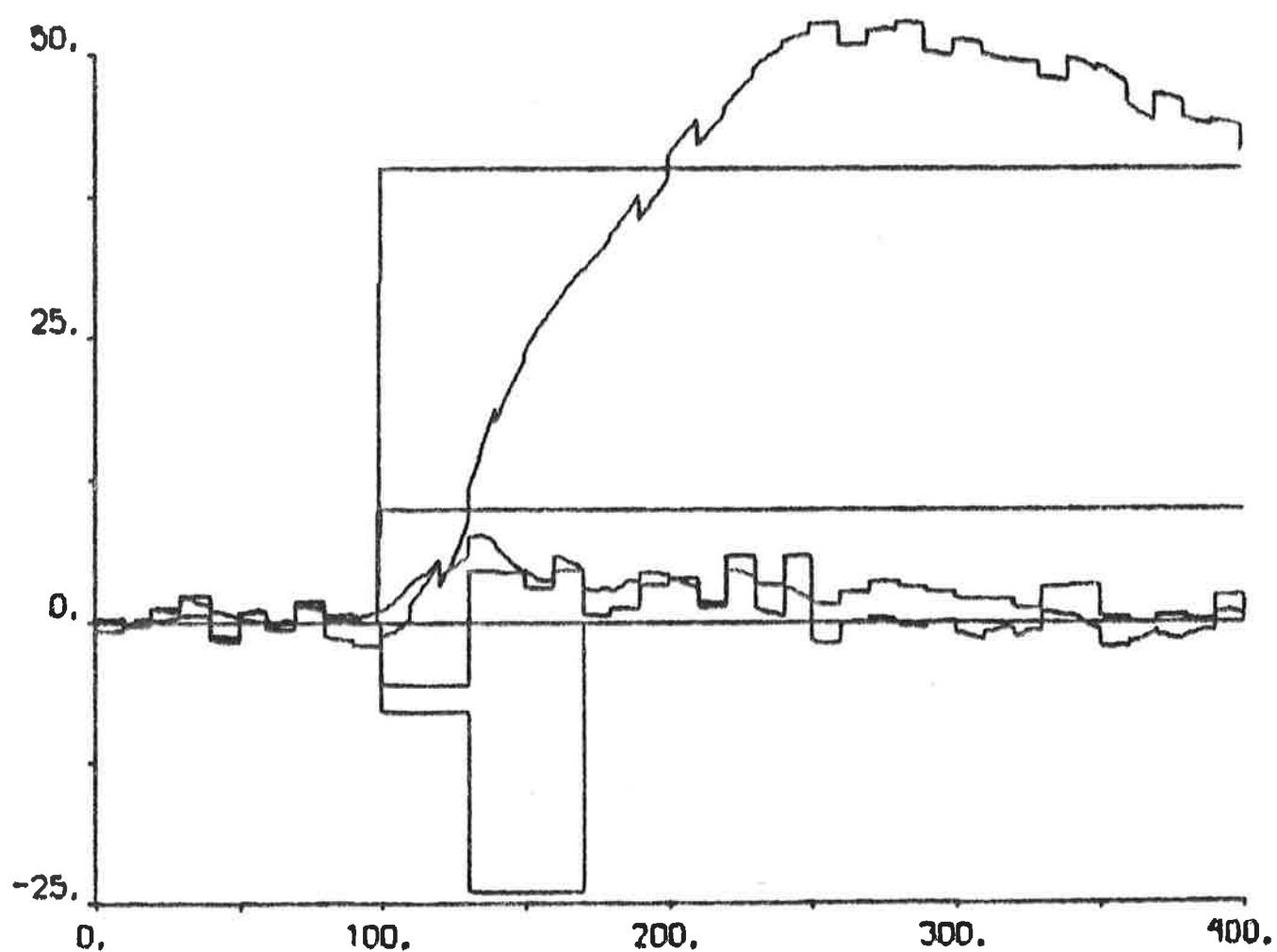
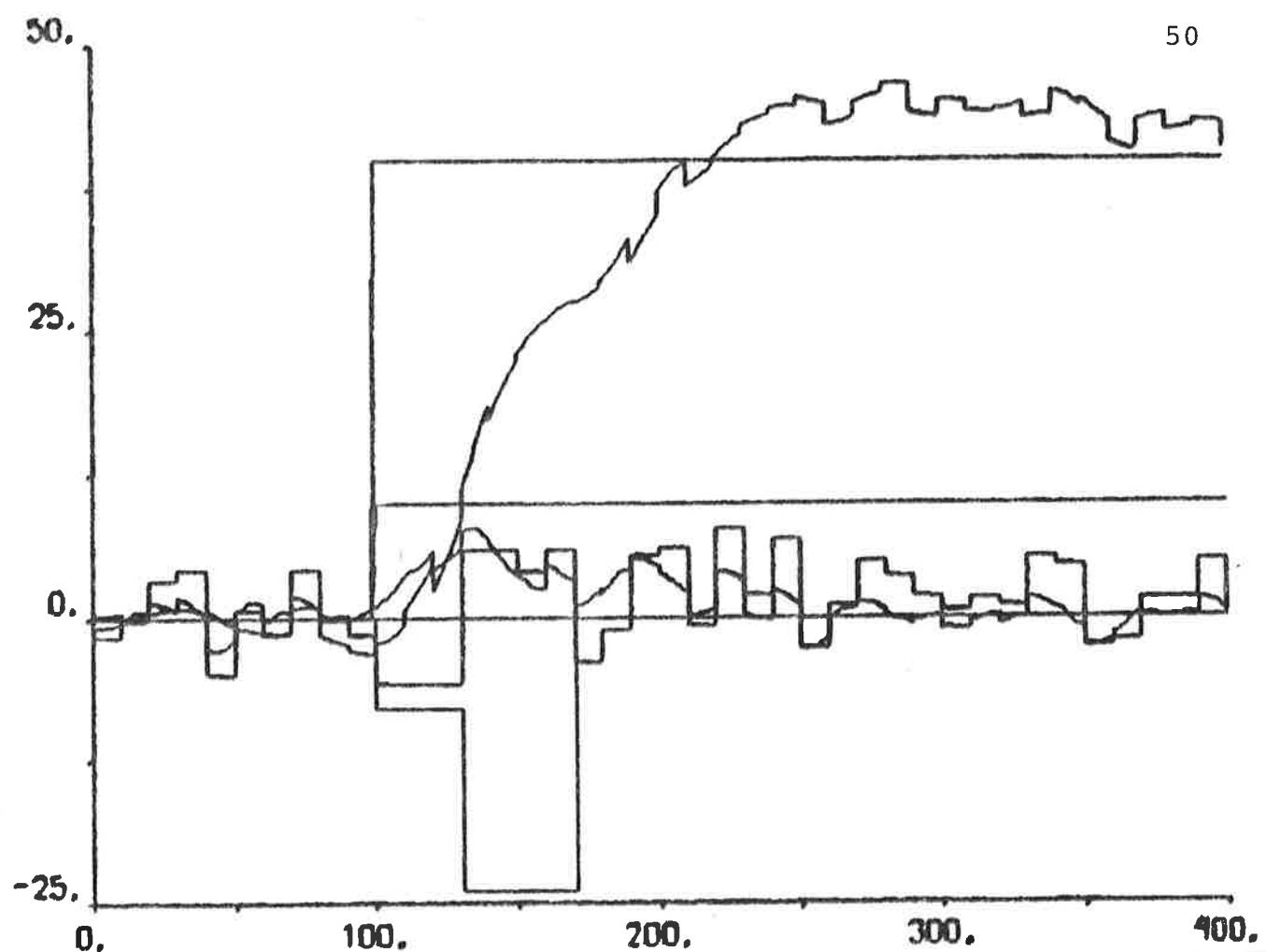


Fig. 5.25 - Stochastic disturbances: $T = 22.3$ m, $\alpha = 90$ deg,
 $\sigma_r = 0.01$ deg/s, $\Delta\psi_{ref} = 4$ deg, $r_{ref} = 0.1$ deg/s.

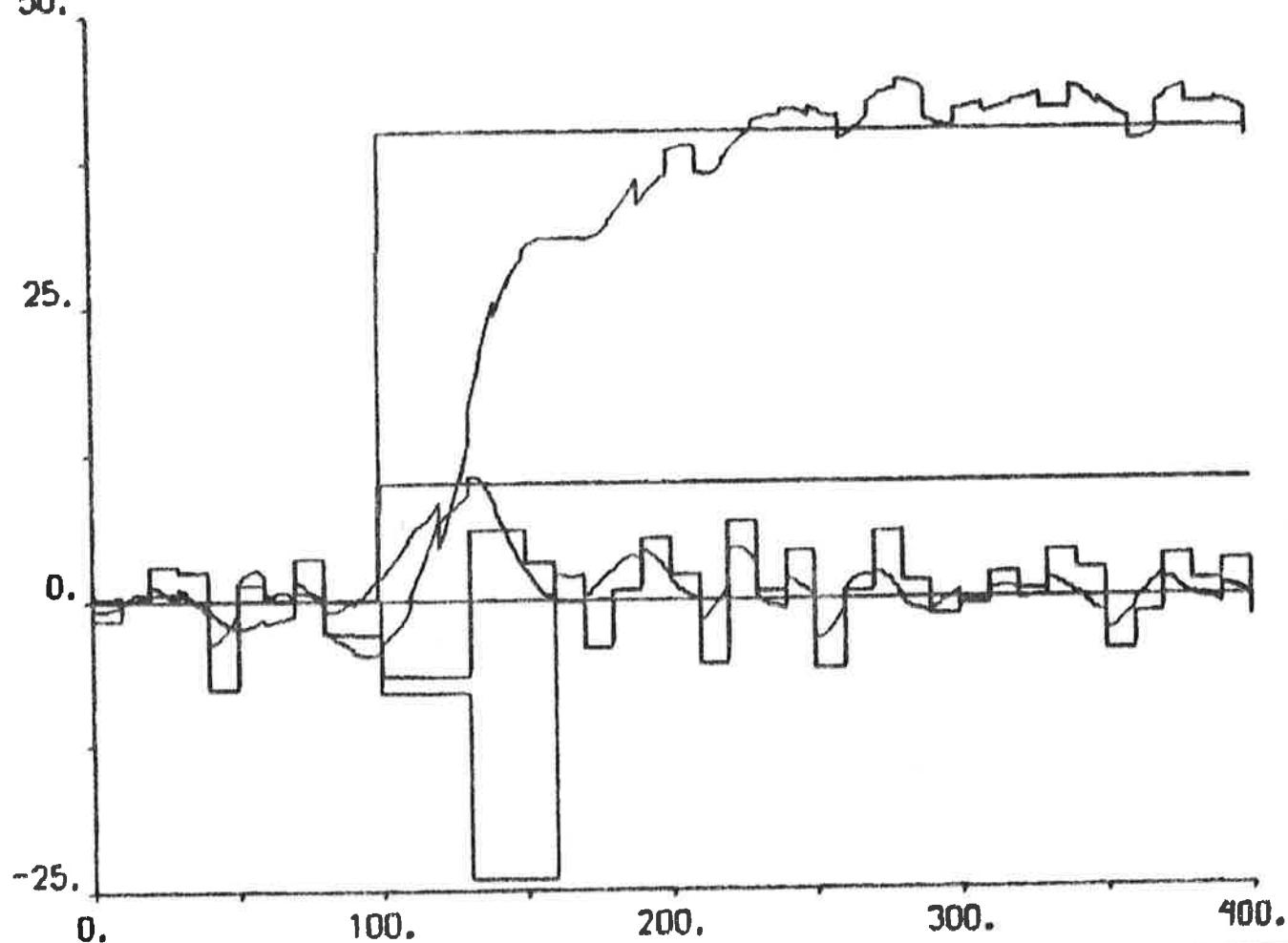


Fig. 5.26 - Stochastic disturbances: $T = 10.5 \text{ m}$, $\alpha = 90 \text{ deg}$,
 $\sigma_r = 0.01 \text{ deg/s}$, $\Delta\psi_{\text{ref}} = 4 \text{ deg}$, $r_{\text{ref}} = 0.1 \text{ deg/s}$.

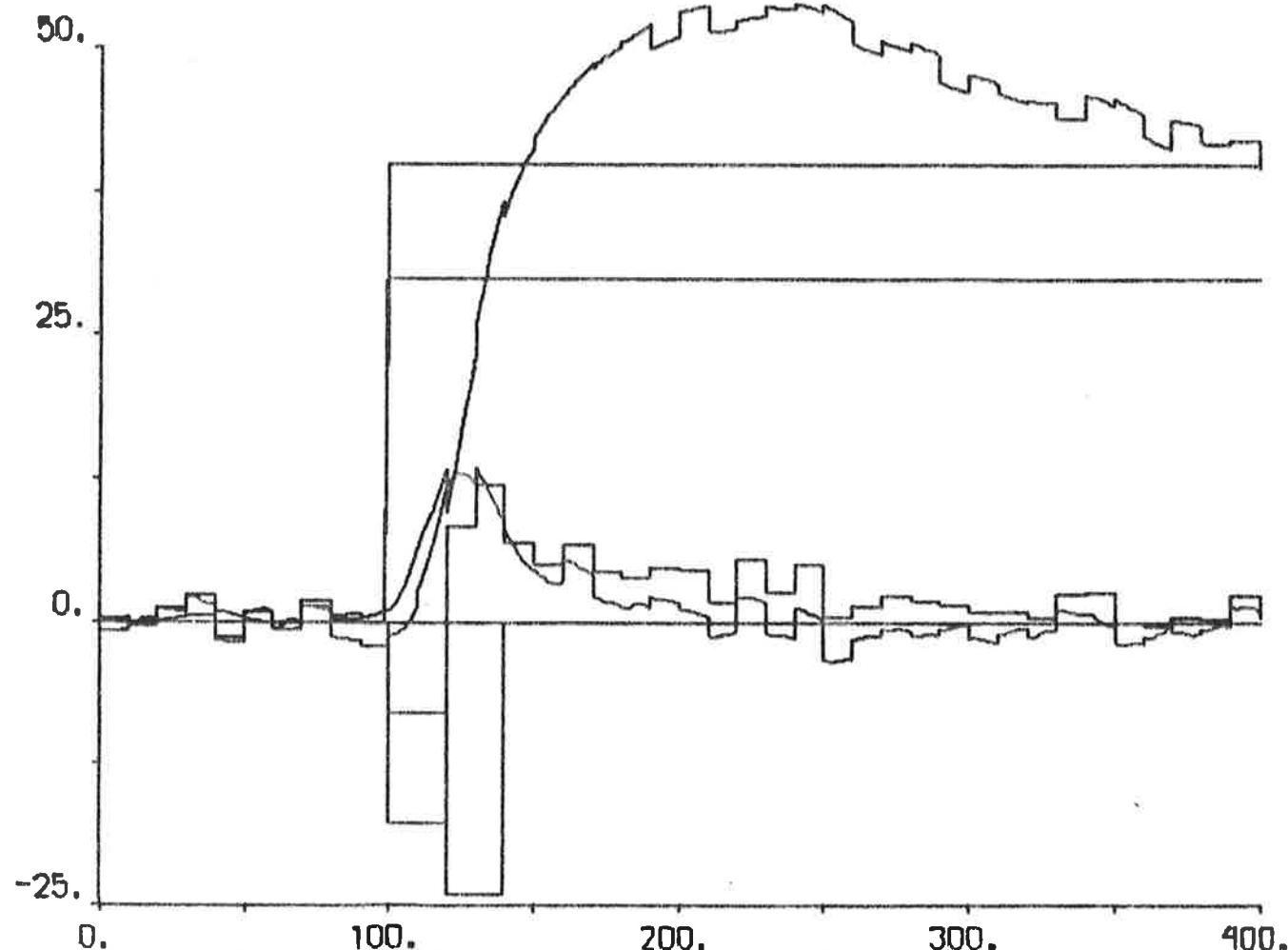
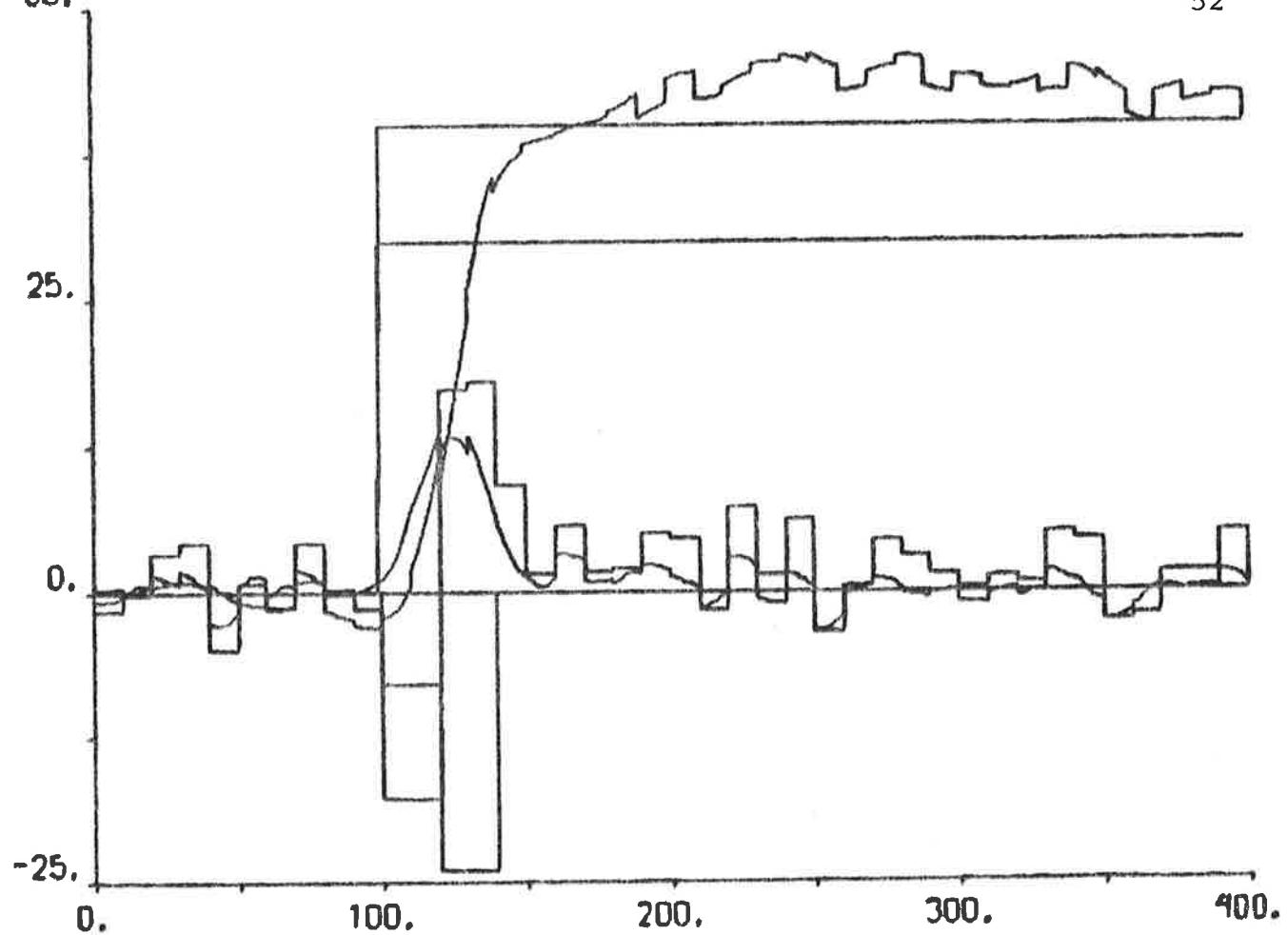
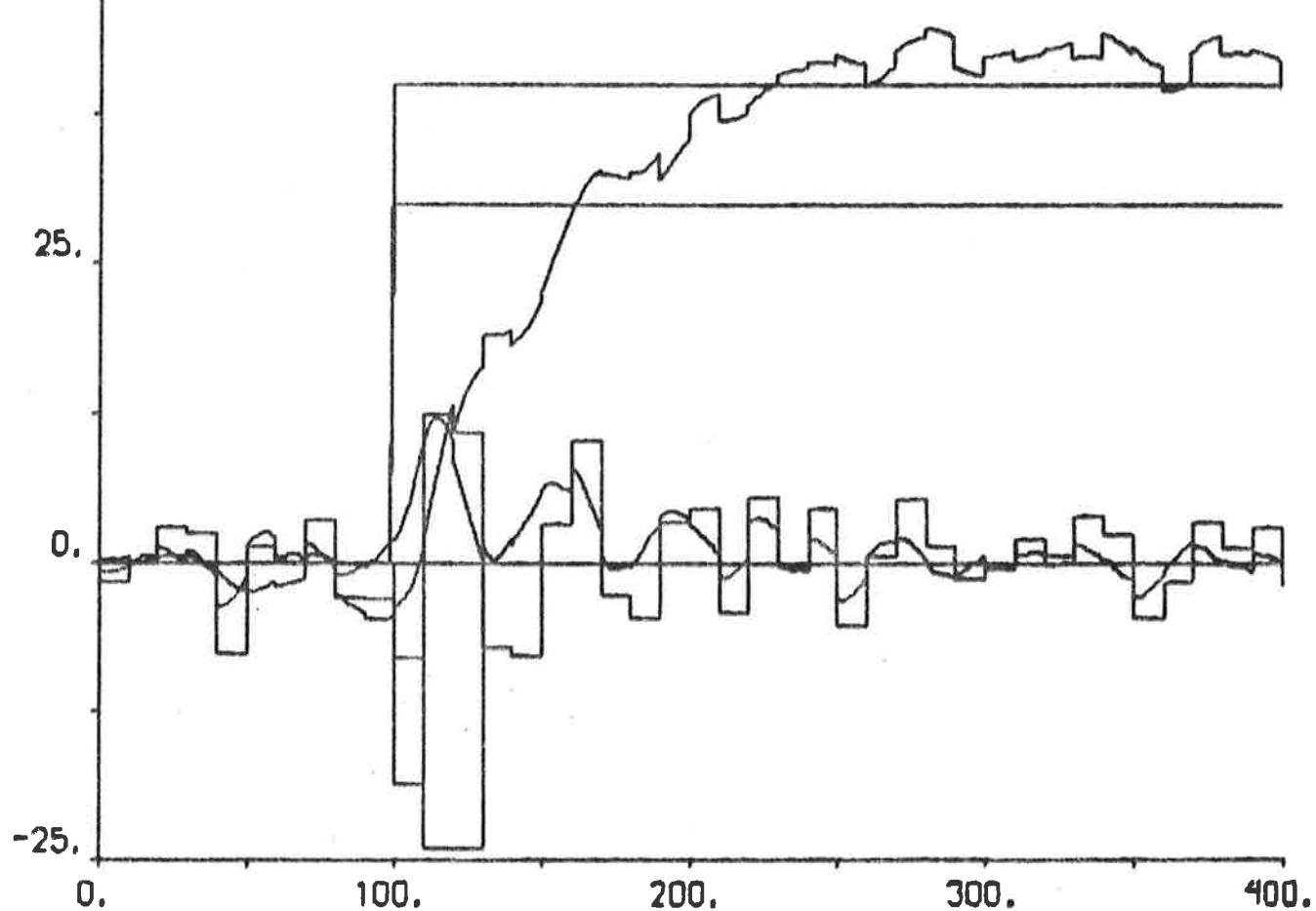


Fig. 5.27 - Stochastic disturbances: $T = 22.3$ m, $\alpha = 90$ deg,
 $\sigma_r = 0.01$ deg/s, $\Delta\psi_{ref} = 4$ deg, $r_{ref} = 0.3$ deg/s.



50.

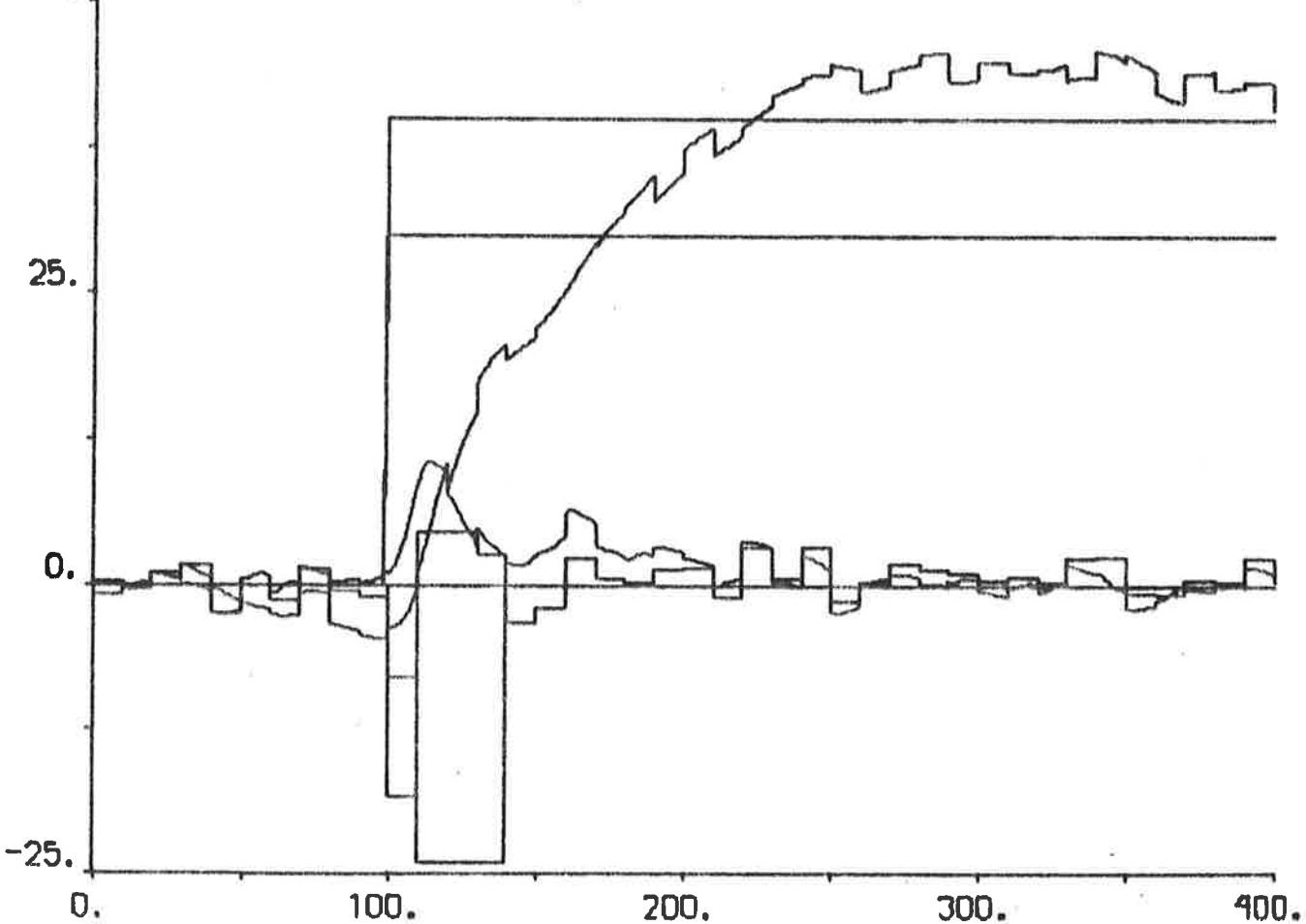


Fig. 5.28 - Stochastic disturbances: $T = 10.5 \text{ m}$, $\alpha = 90 \text{ deg}$,
 $\sigma_r = 0.01 \text{ deg/s}$, $\Delta\psi_{\text{ref}} = 4 \text{ deg}$, $r_{\text{ref}} = 0.3 \text{ deg/s}$.

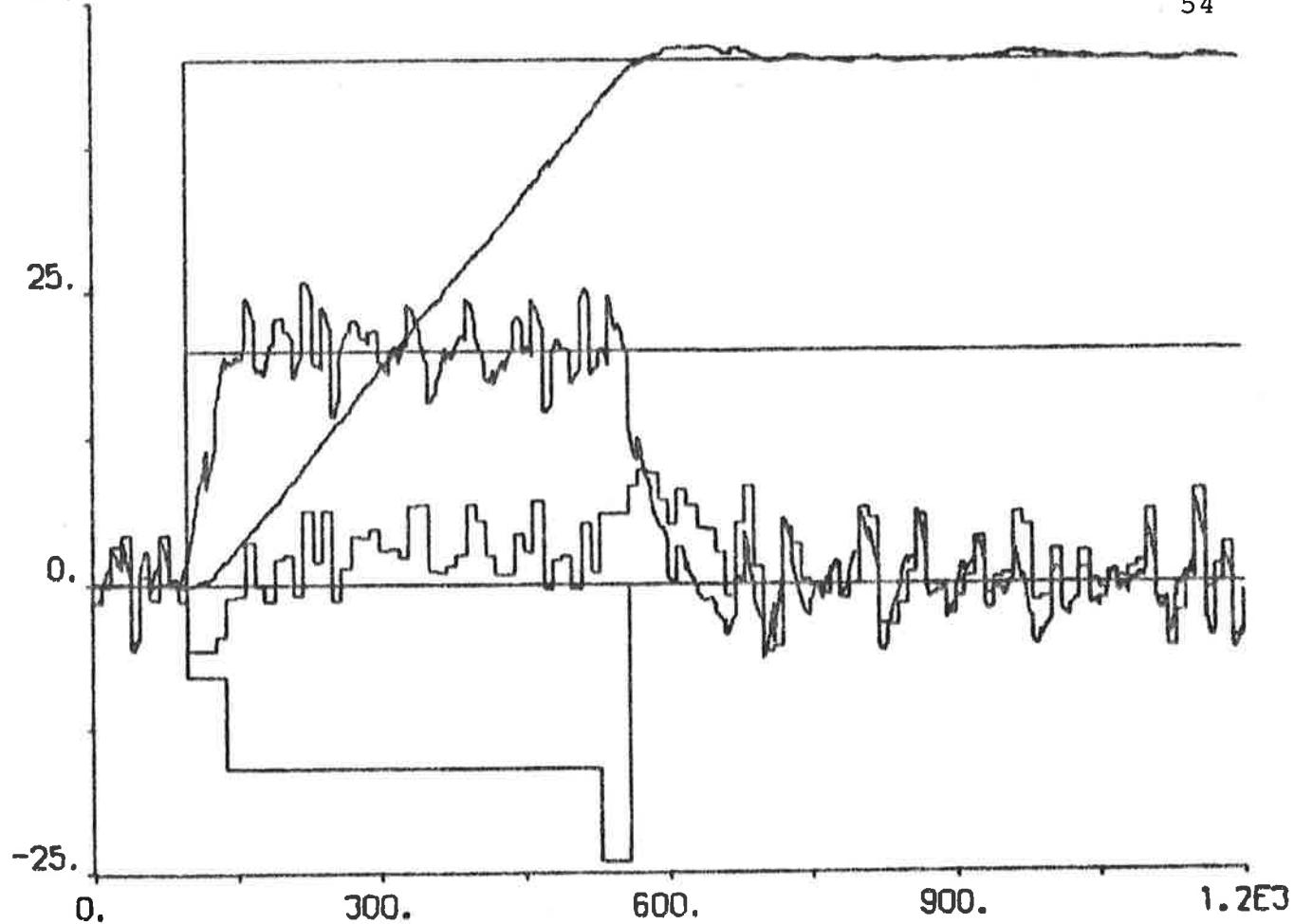


Fig. 5.29 - Stochastic disturbances: $T = 22.3$ m, $\alpha = 90$ deg,
 $\sigma_r = 0.01$ deg/s, $\Delta\psi_{ref} = 45$ deg, $r_{ref} = 0.1$ deg/s.

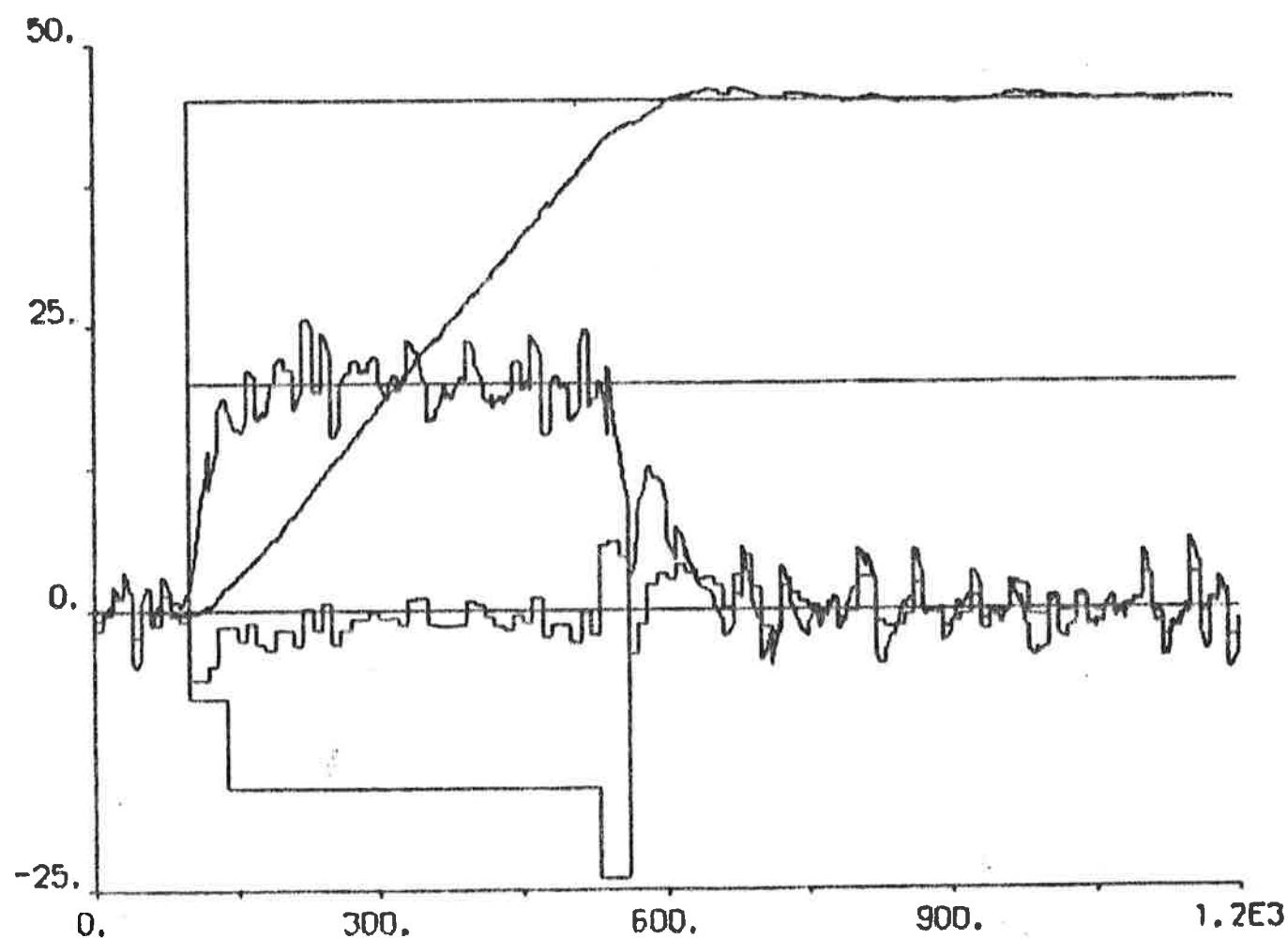
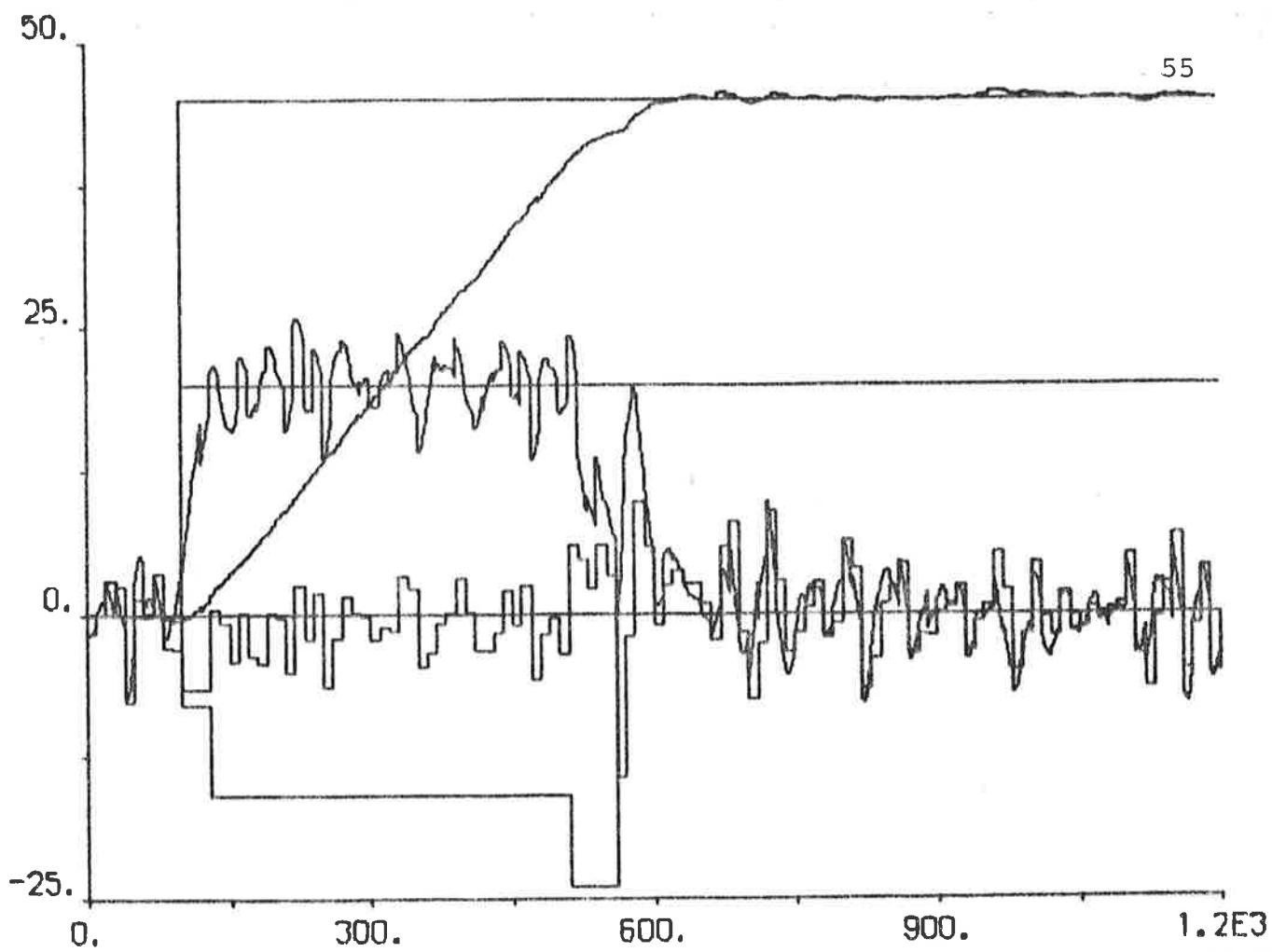


Fig. 5.30 - Stochastic disturbances: $T = 10.5 \text{ m}$, $\alpha = 90 \text{ deg}$,
 $\sigma_r = 0.01 \text{ deg/s}$, $\Delta\psi_{\text{ref}} = 45 \text{ deg}$, $r_{\text{ref}} = 0.1 \text{ deg/s}$.

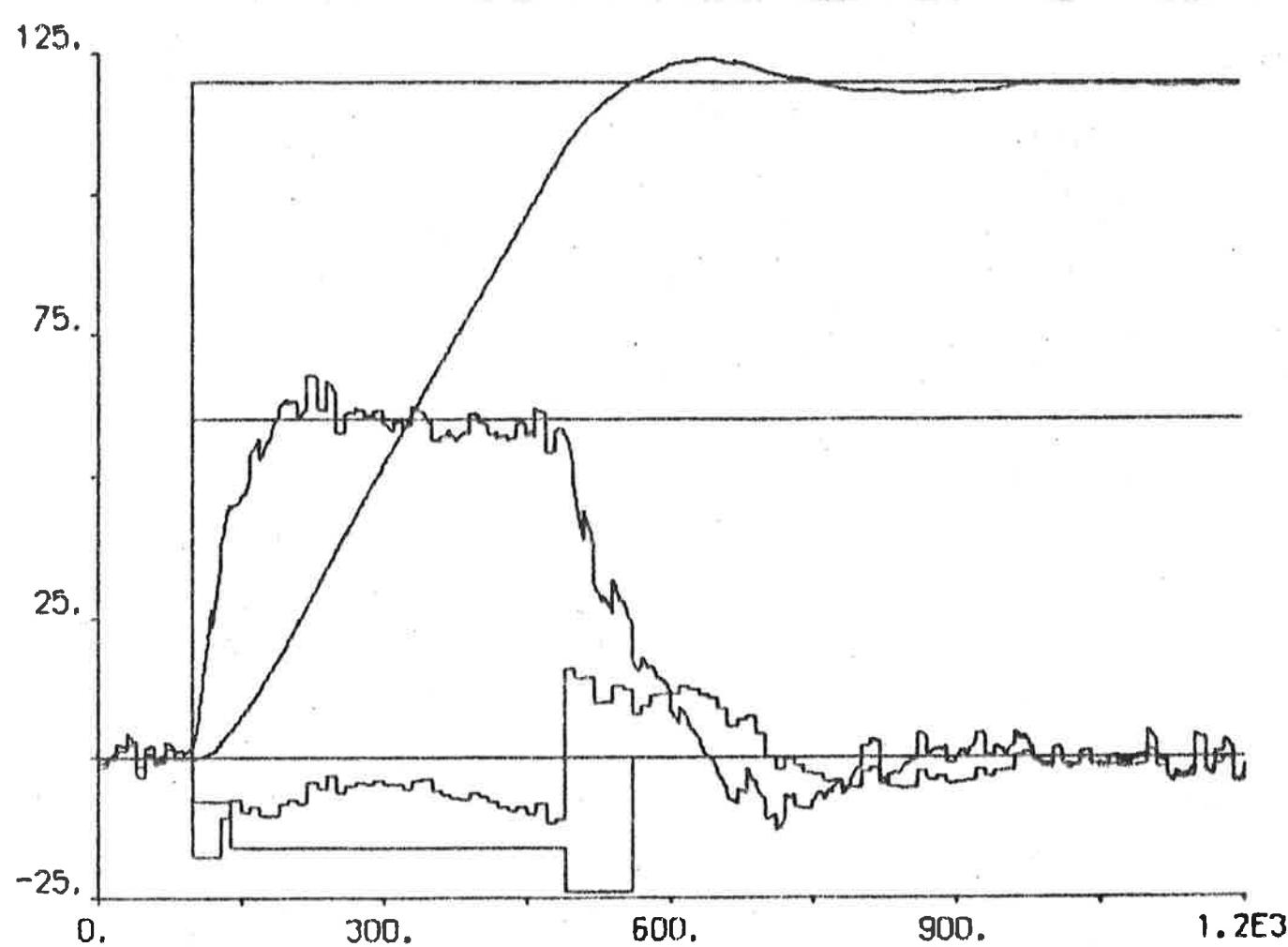
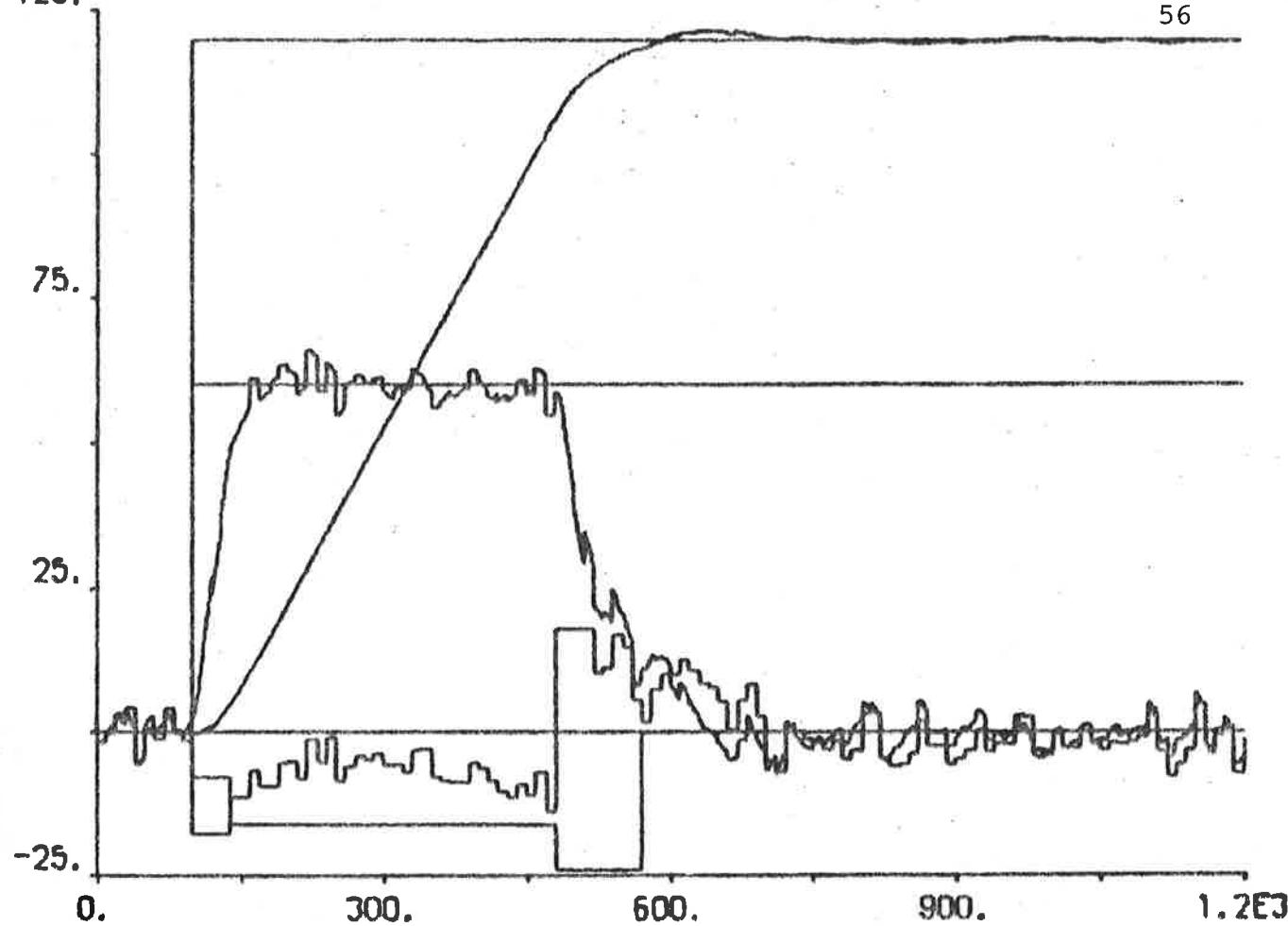


Fig. 5.31 - Stochastic disturbances: $T = 22.3$ m, $\alpha = 90$ deg,
 $\sigma_r = 0.01$ deg/s, $\Delta\psi_{ref} = 120$ deg, $r_{ref} = 0.3$ deg/s.

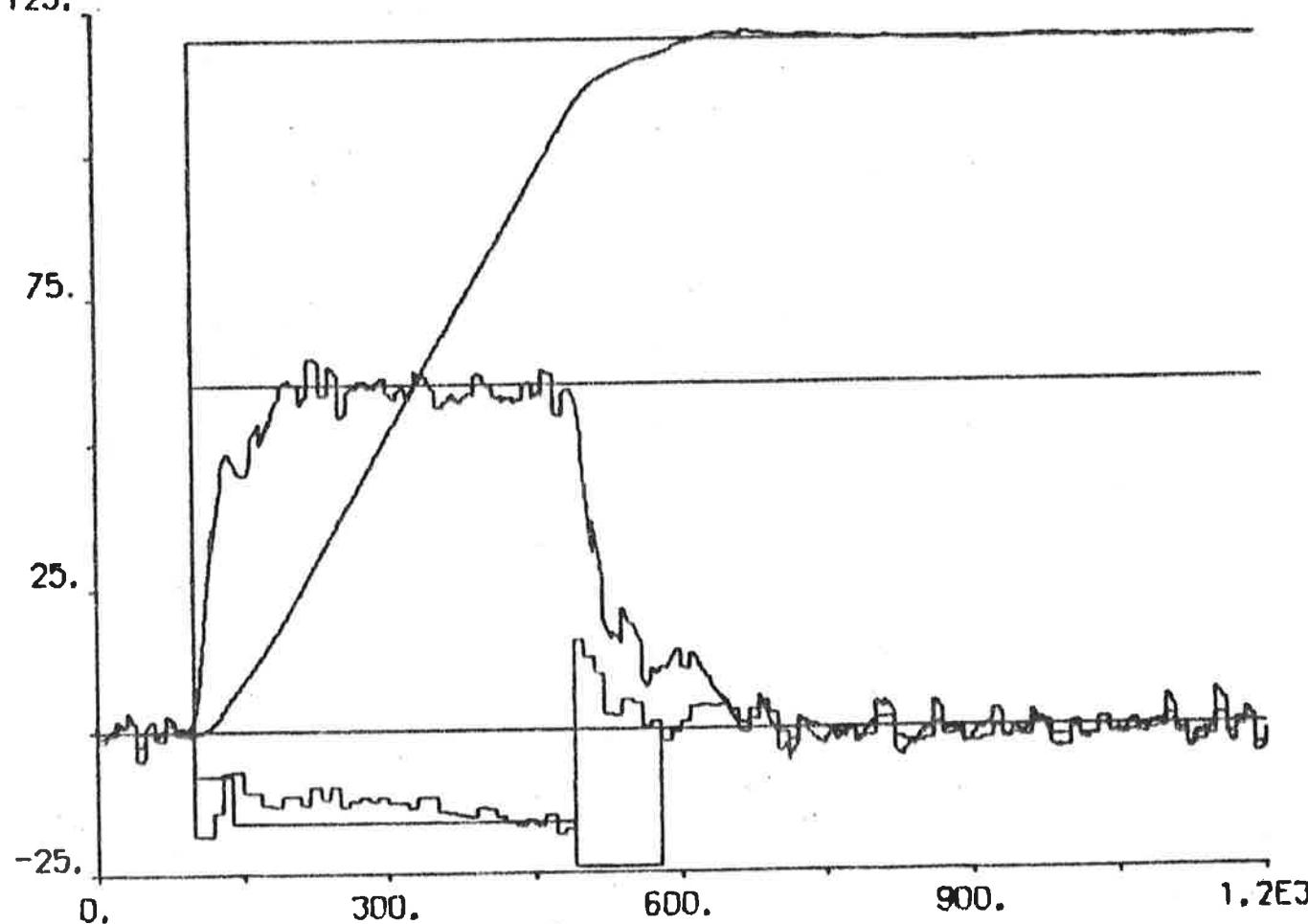
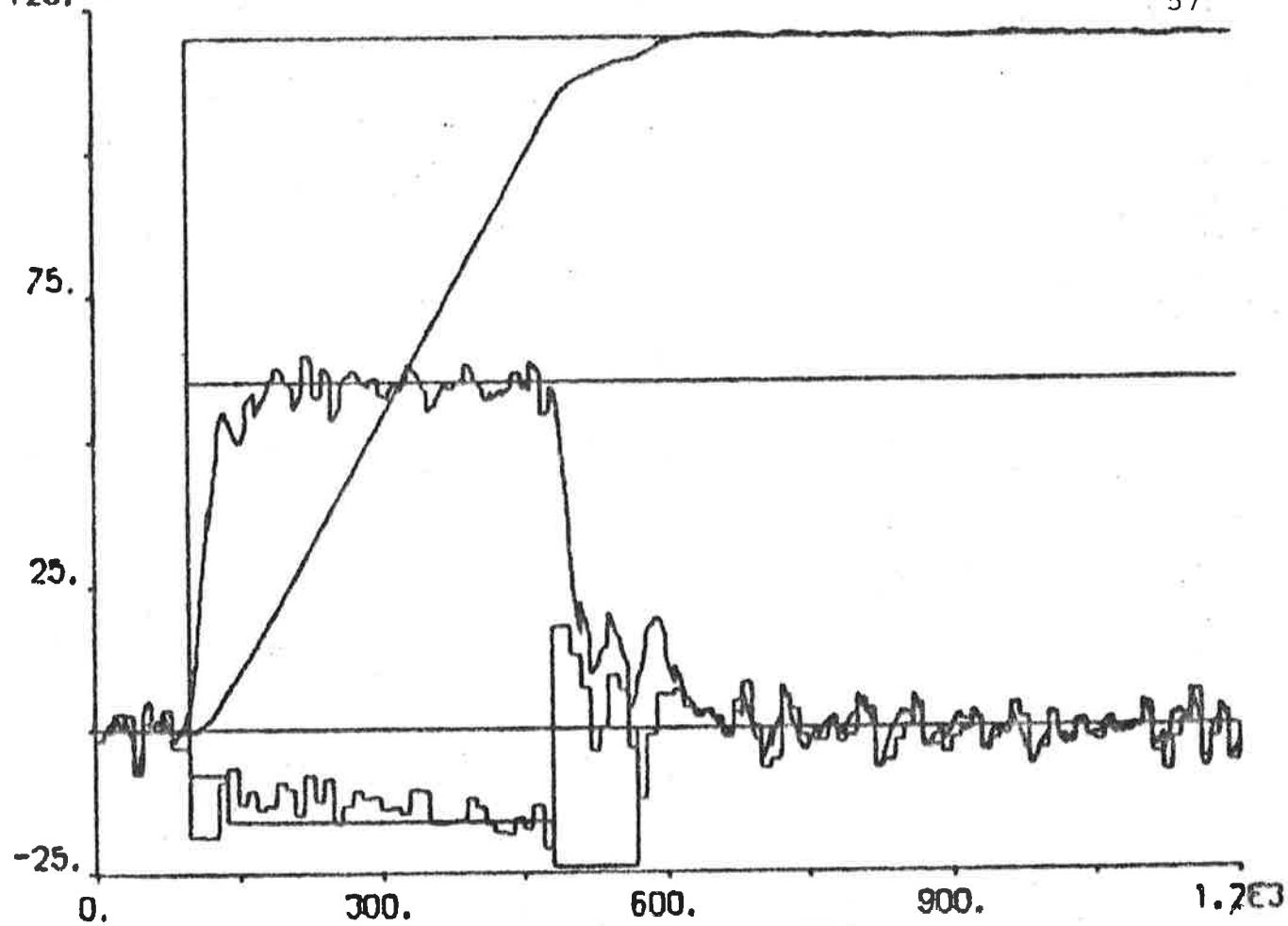


Fig. 5.32 - Stochastic disturbances: $T = 10.5 \text{ m}$, $\alpha = 90 \text{ deg}$, $\sigma_r = 0.01 \text{ deg/s}$, $\Delta\psi_{\text{ref}} = 120 \text{ deg}$, $r_{\text{ref}} = 0.3 \text{ deg/s}$.

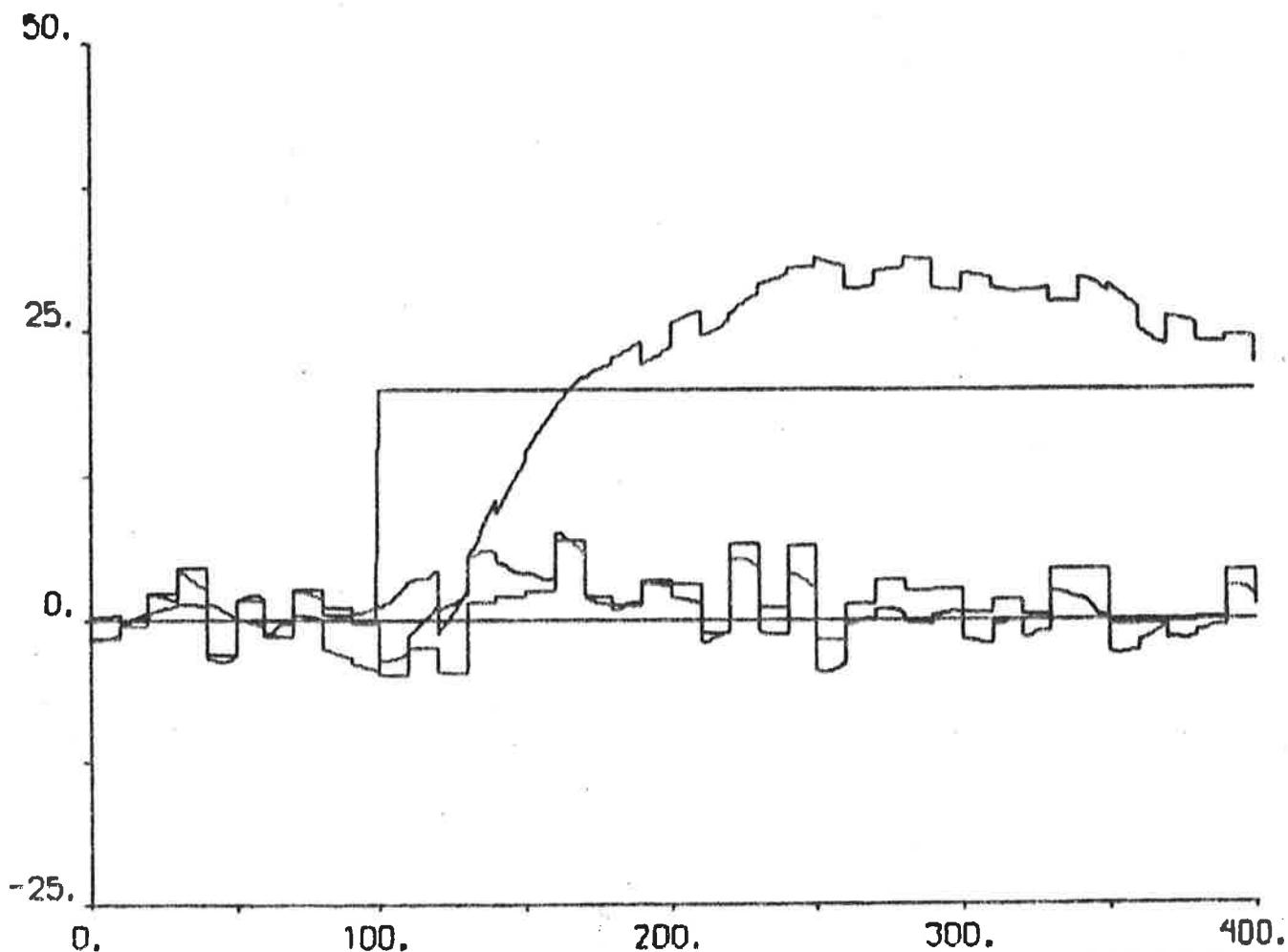
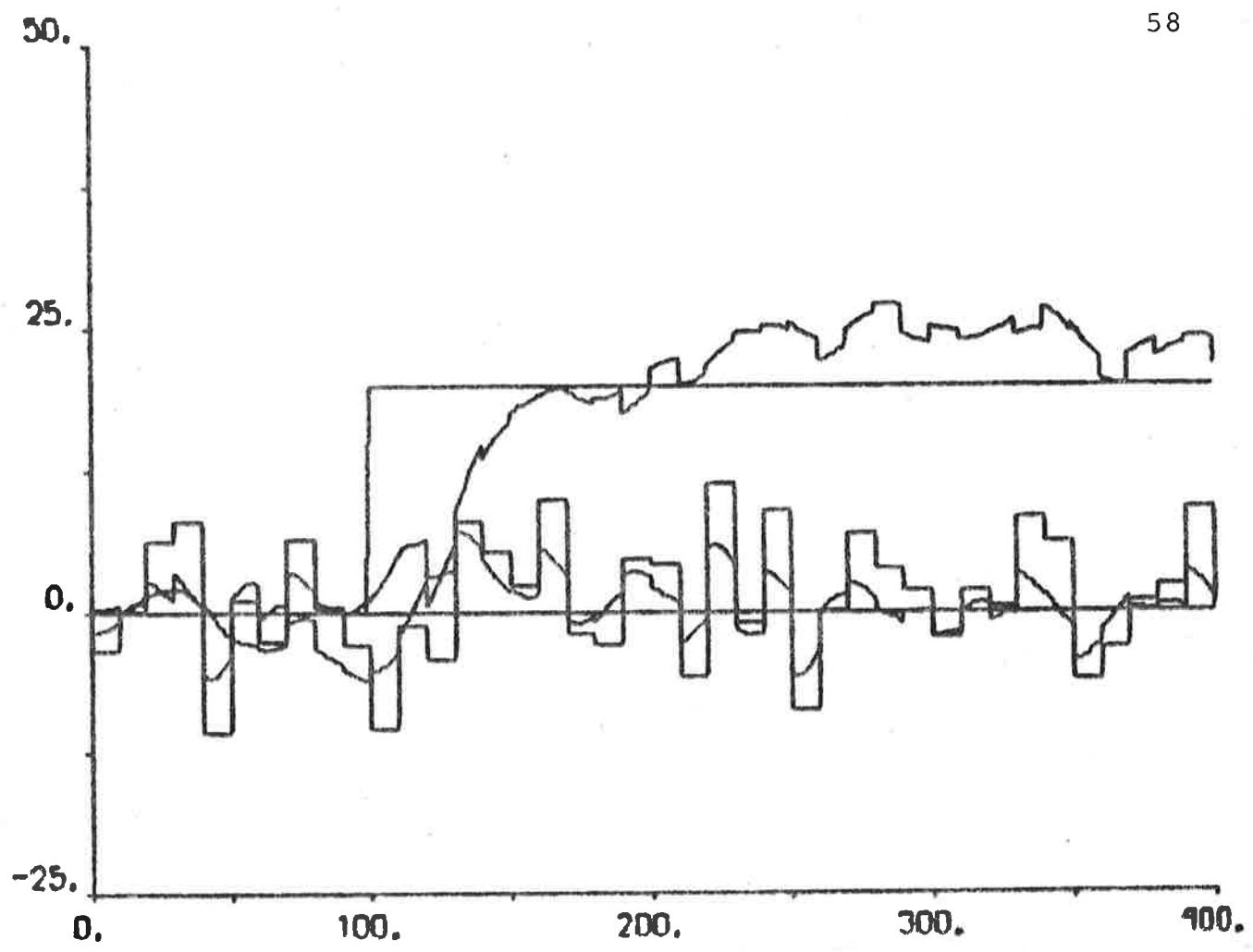


Fig. 5.33 - Stochastic disturbances: $T = 22.3$ m, $\alpha = 90$ deg,
 $\sigma_r = 0.02$ deg/s, $\Delta\psi_{ref} = 2$ deg.

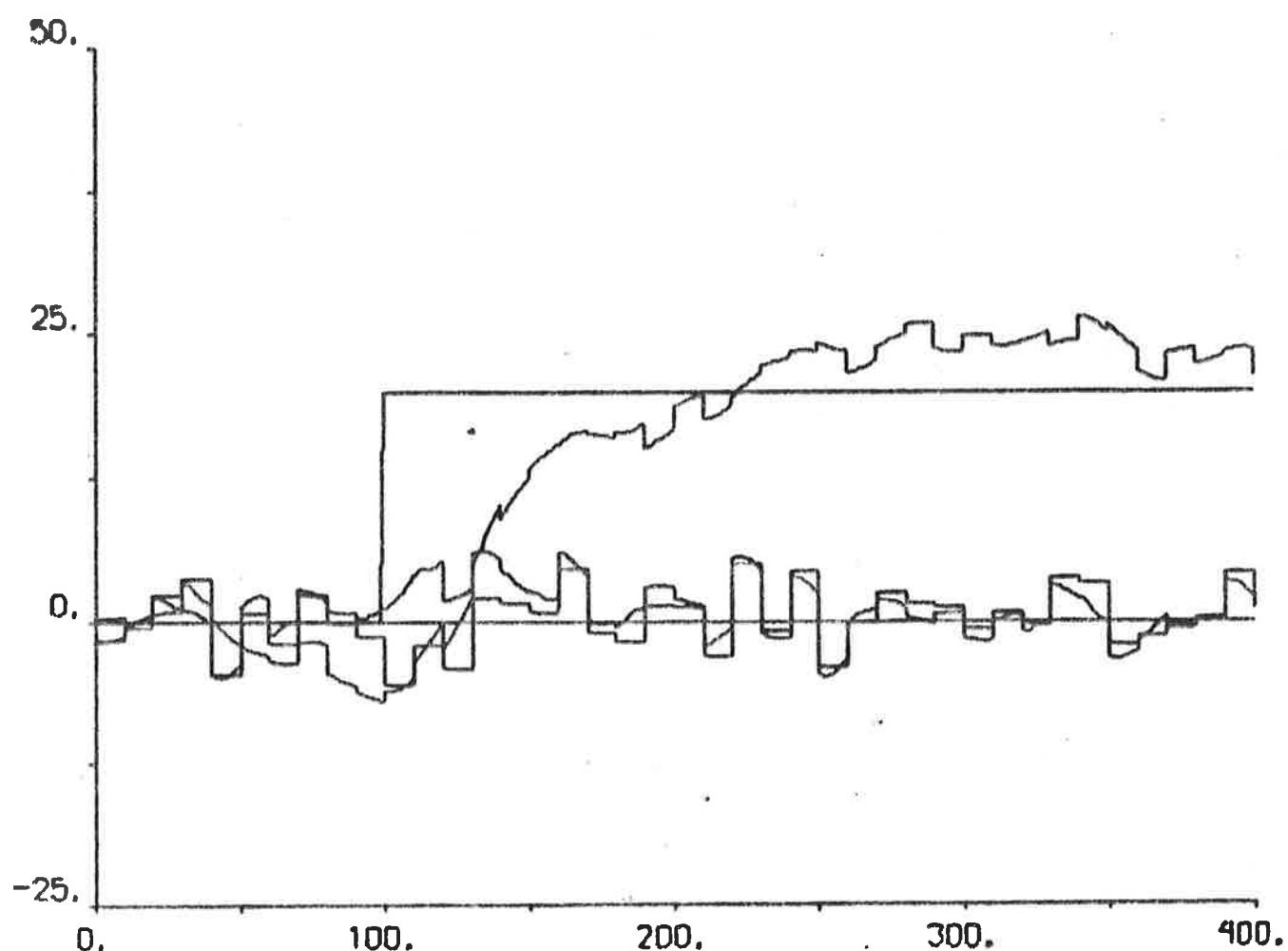
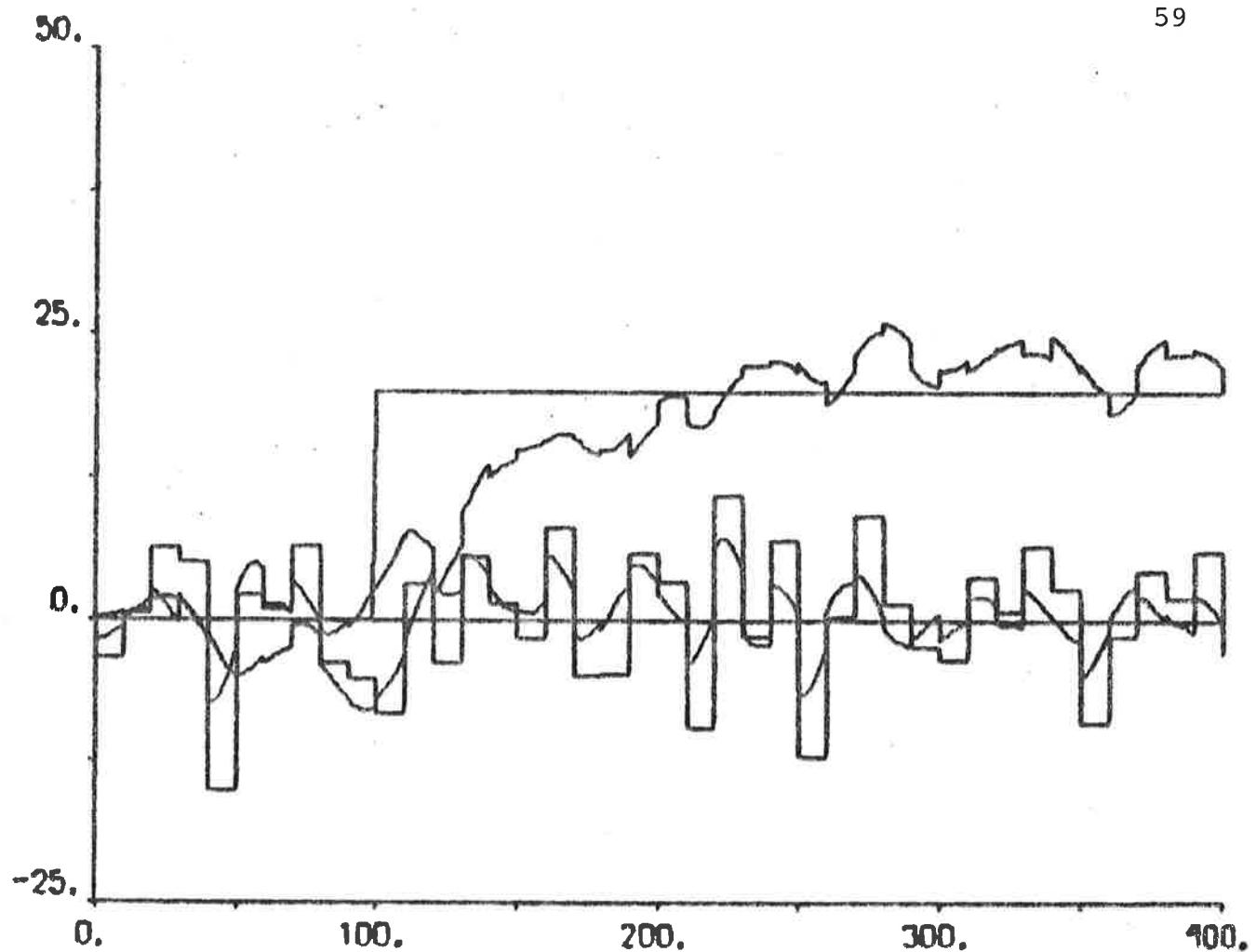


Fig. 5.34 - Stochastic disturbances: $T = 10.5 \text{ m}$, $\alpha = 90 \text{ deg}$,
 $\sigma_r = 0.02 \text{ deg/s}$, $\Delta\psi_{ref} = 2 \text{ deg}$.

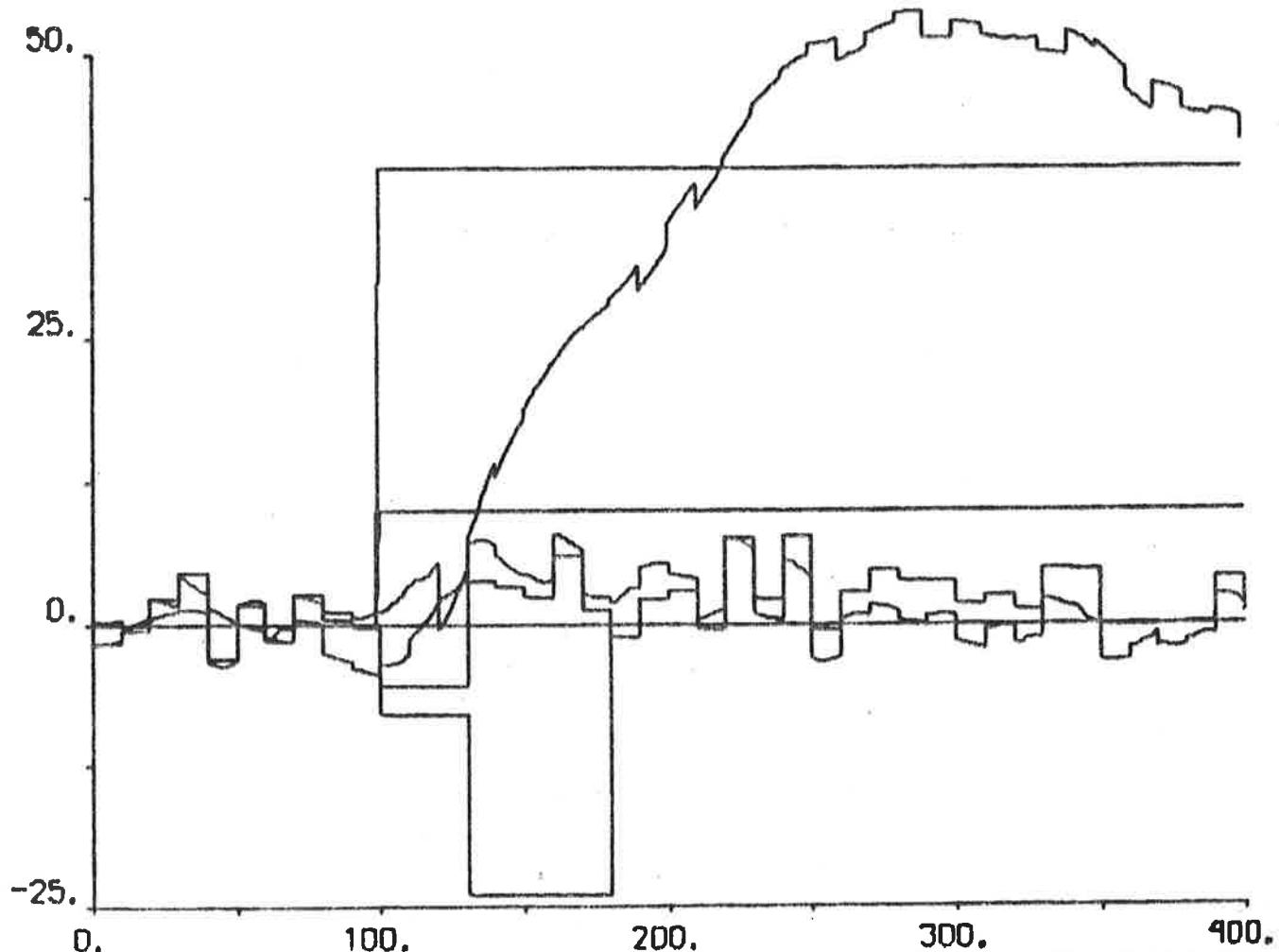
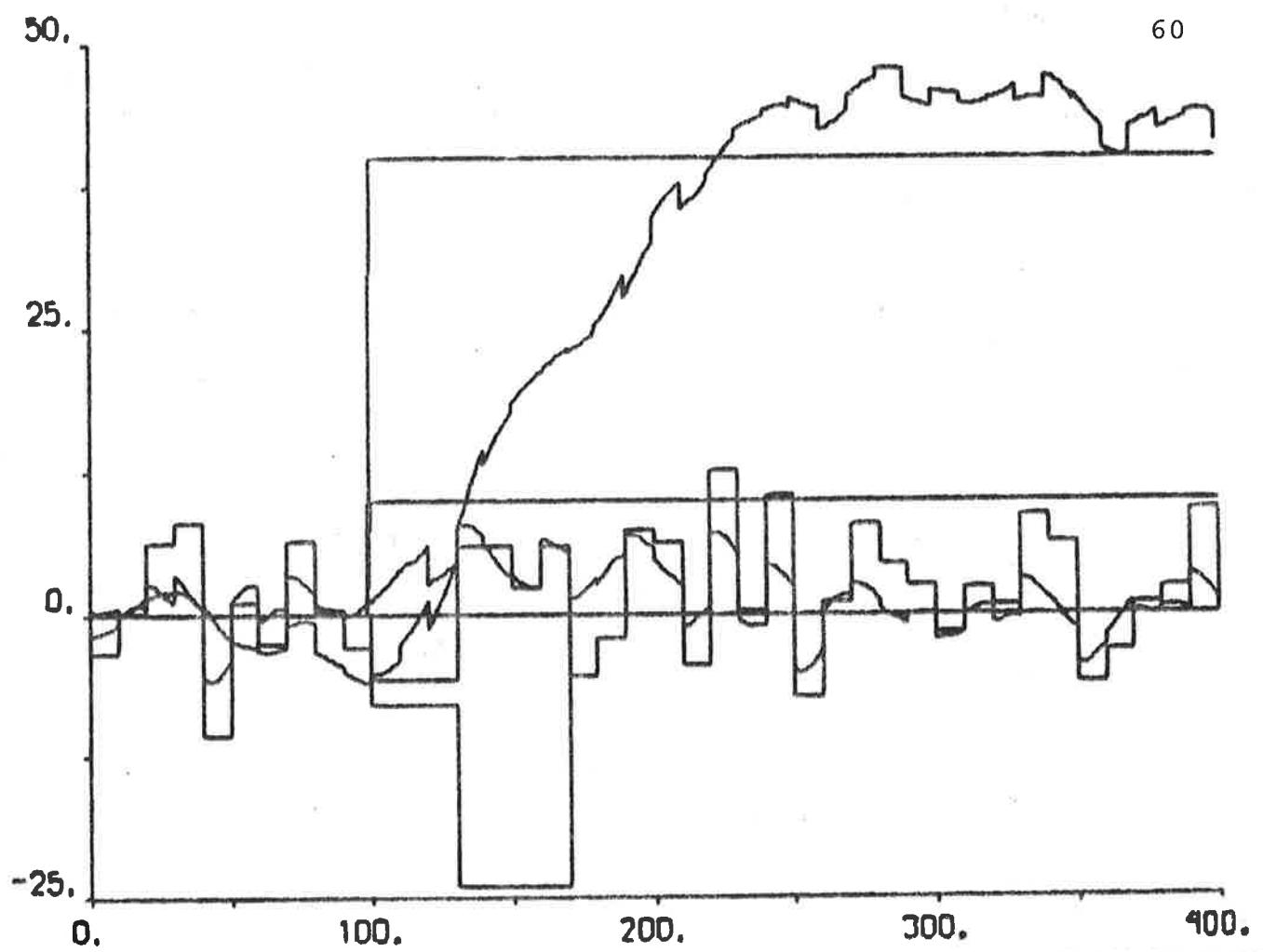


Fig. 5.35 - Stochastic disturbances: $T = 22.3$ m, $\alpha = 90$ deg,
 $\sigma_r = 0.02$ deg/s, $\Delta\psi_{ref} = 4$ deg, $r_{ref} = 0.1$ deg/s.

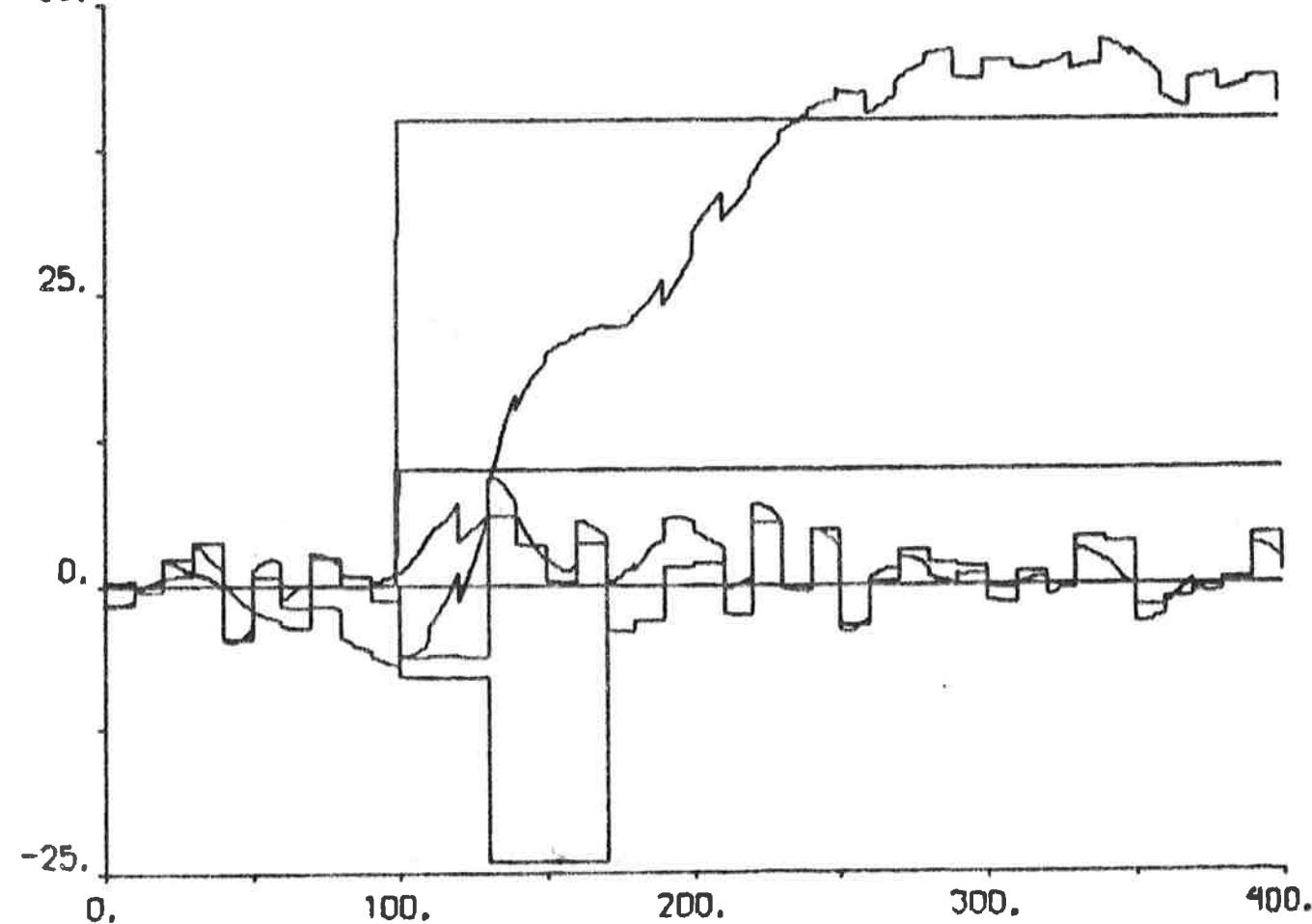
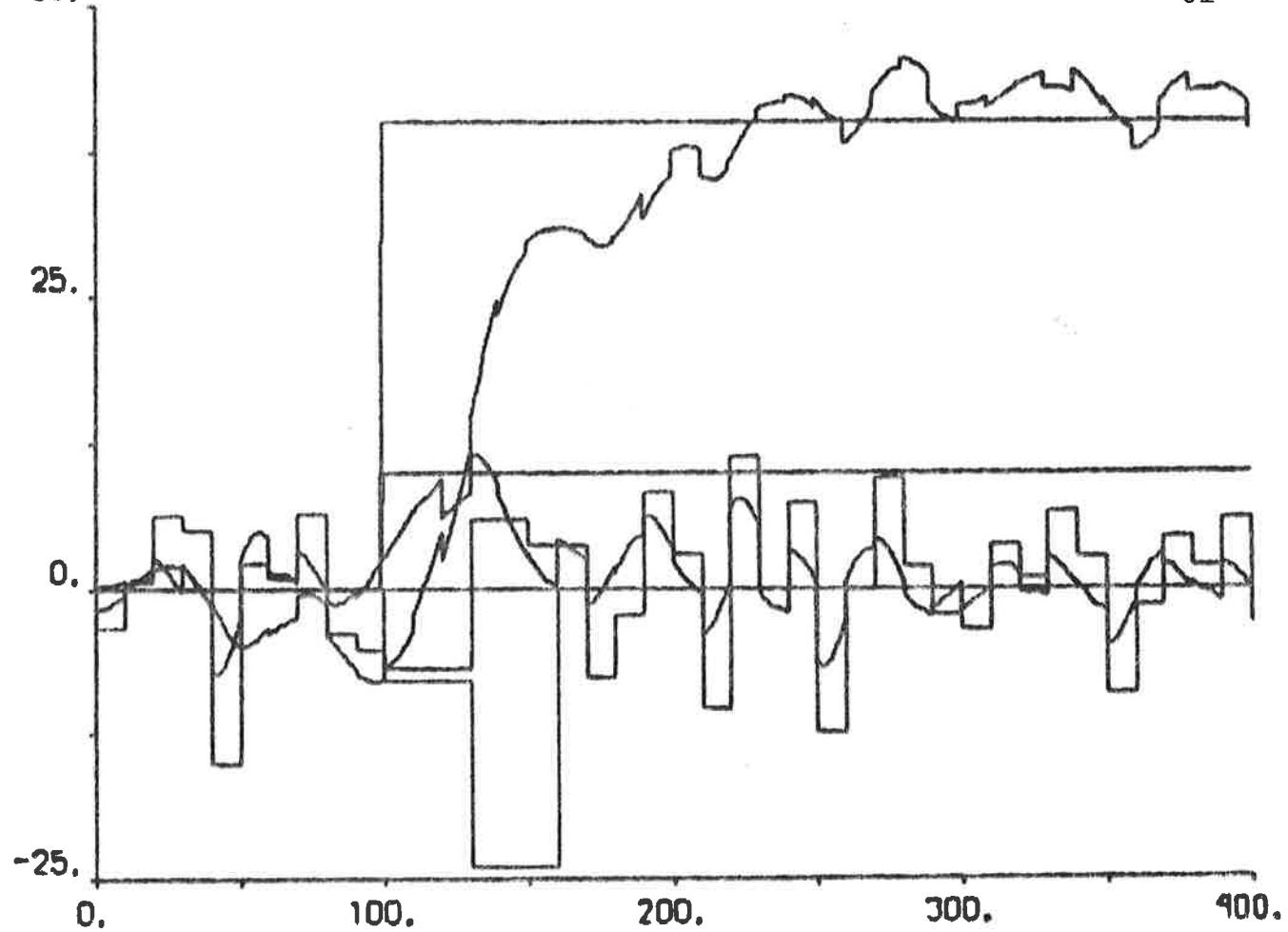


Fig. 5.36 - Stochastic disturbances: $T = 10.5 \text{ m}$, $\alpha = 90 \text{ deg}$,
 $\sigma_r = 0.02 \text{ deg/s}$, $\Delta\psi_{\text{ref}} = 4 \text{ deg}$, $r_{\text{ref}} = 0.1 \text{ deg/s}$.

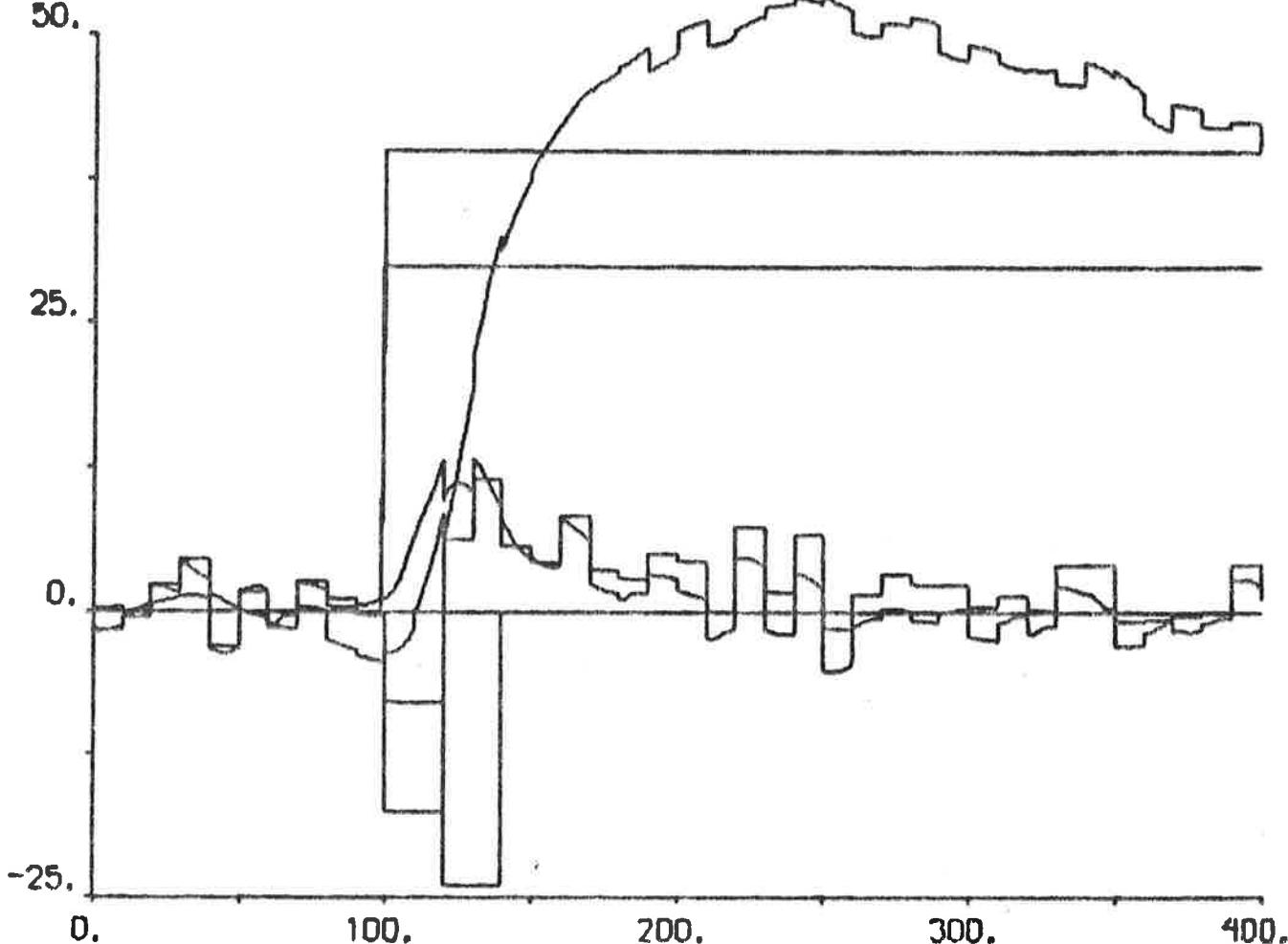
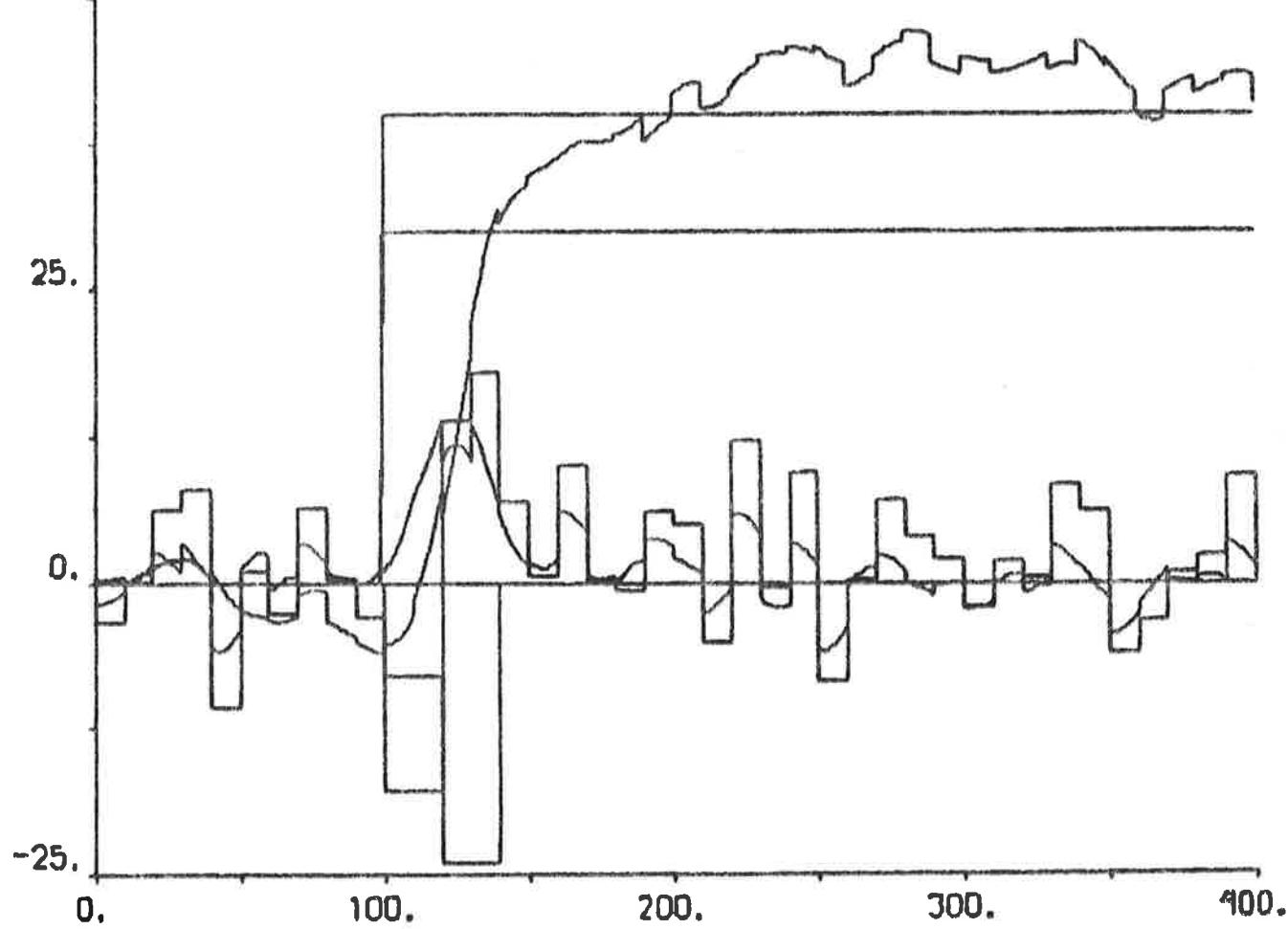


Fig. 5.37 - Stochastic disturbances: $T = 22.3$ m, $\alpha = 90$ deg,
 $\sigma_r = 0.02$ deg/s, $\Delta\psi_{ref} = 4$ deg, $r_{ref} = 0.3$ deg/s.

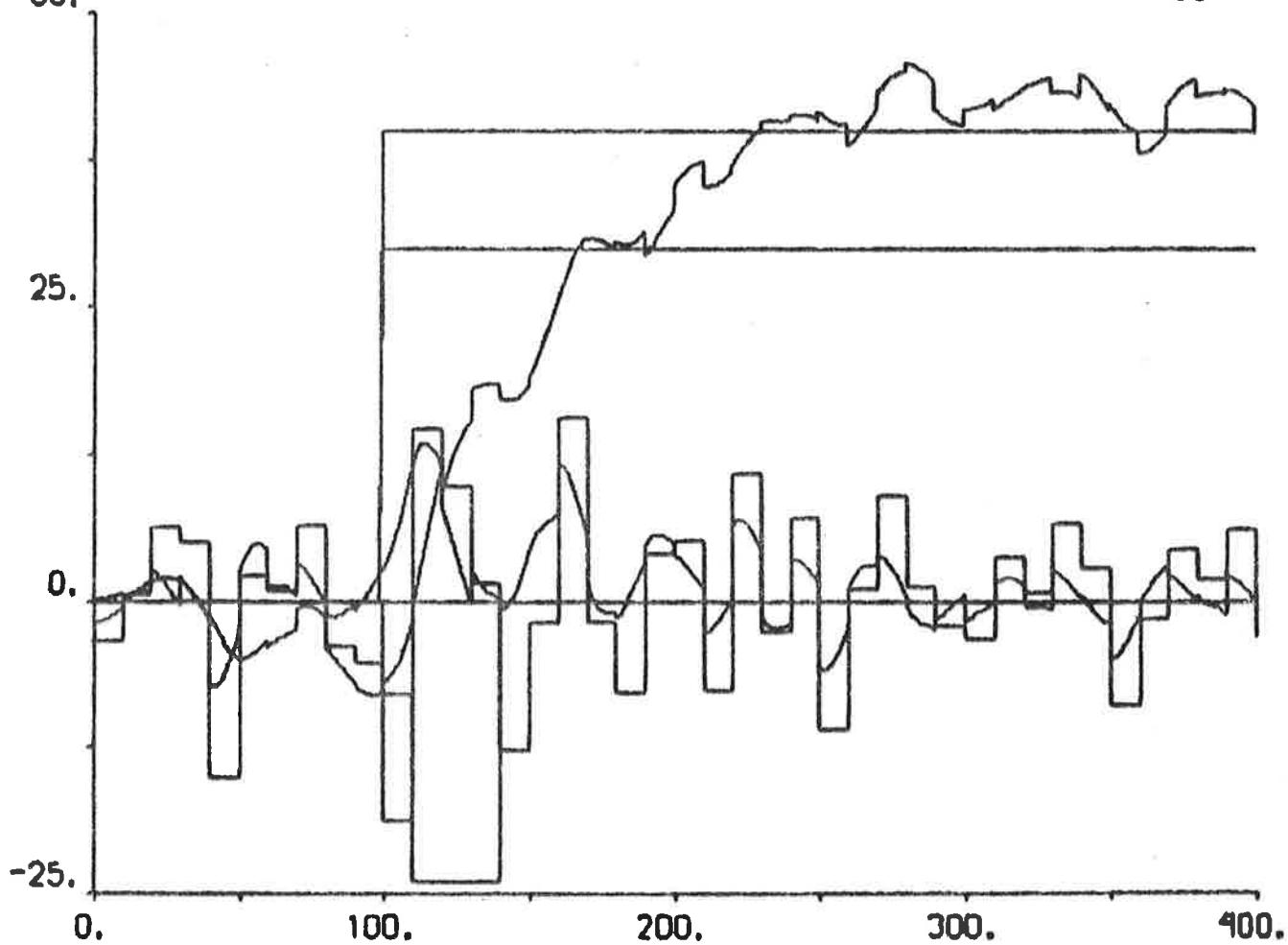


Fig. 5.38 - Stochastic disturbances: $T = 10.5 \text{ m}$, $\alpha = 90 \text{ deg}$,
 $\sigma_r = 0.02 \text{ deg/s}$, $\Delta\psi_{\text{ref}} = 4 \text{ deg}$, $r_{\text{ref}} = 0.3 \text{ deg/s}$.

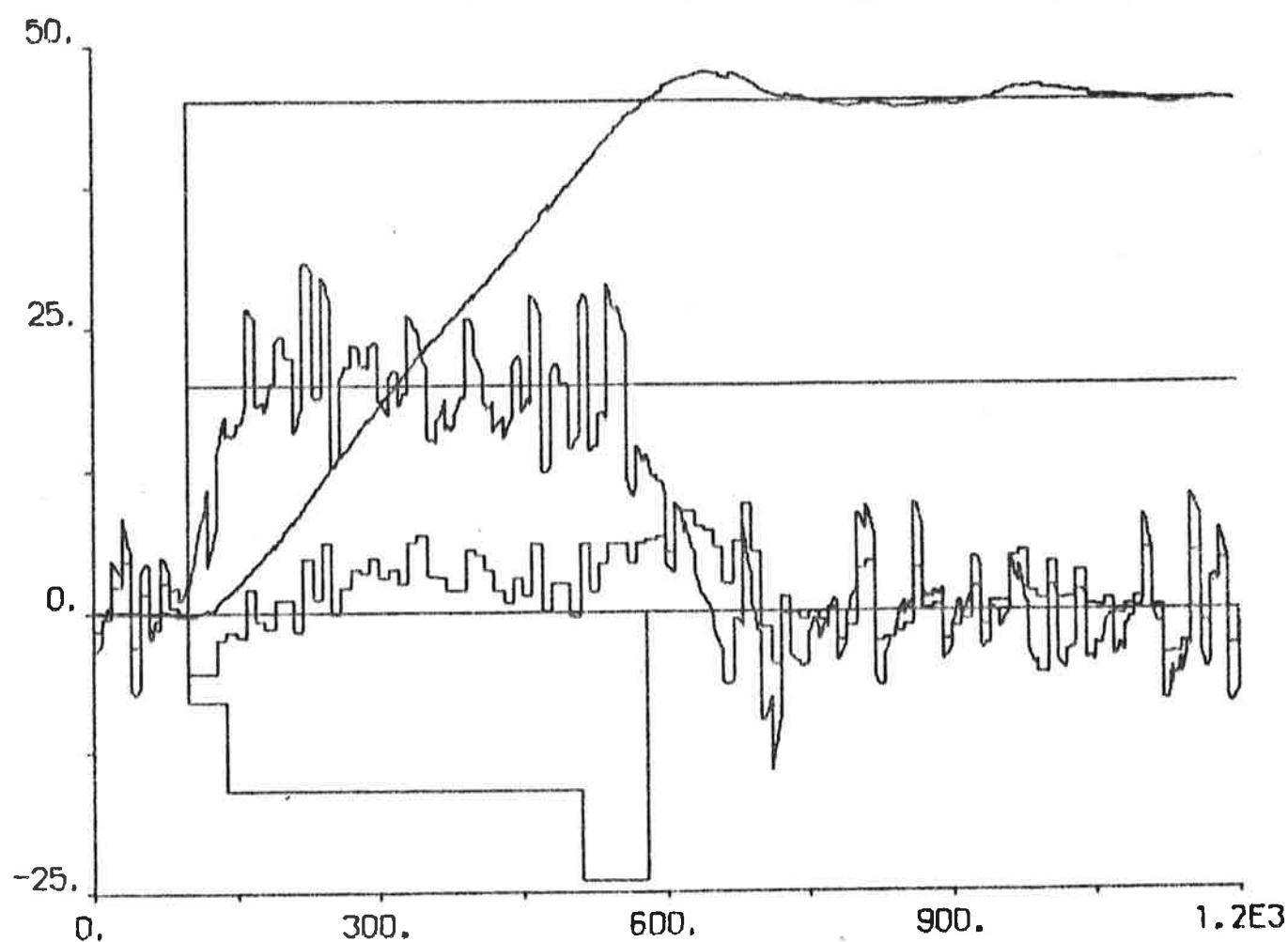
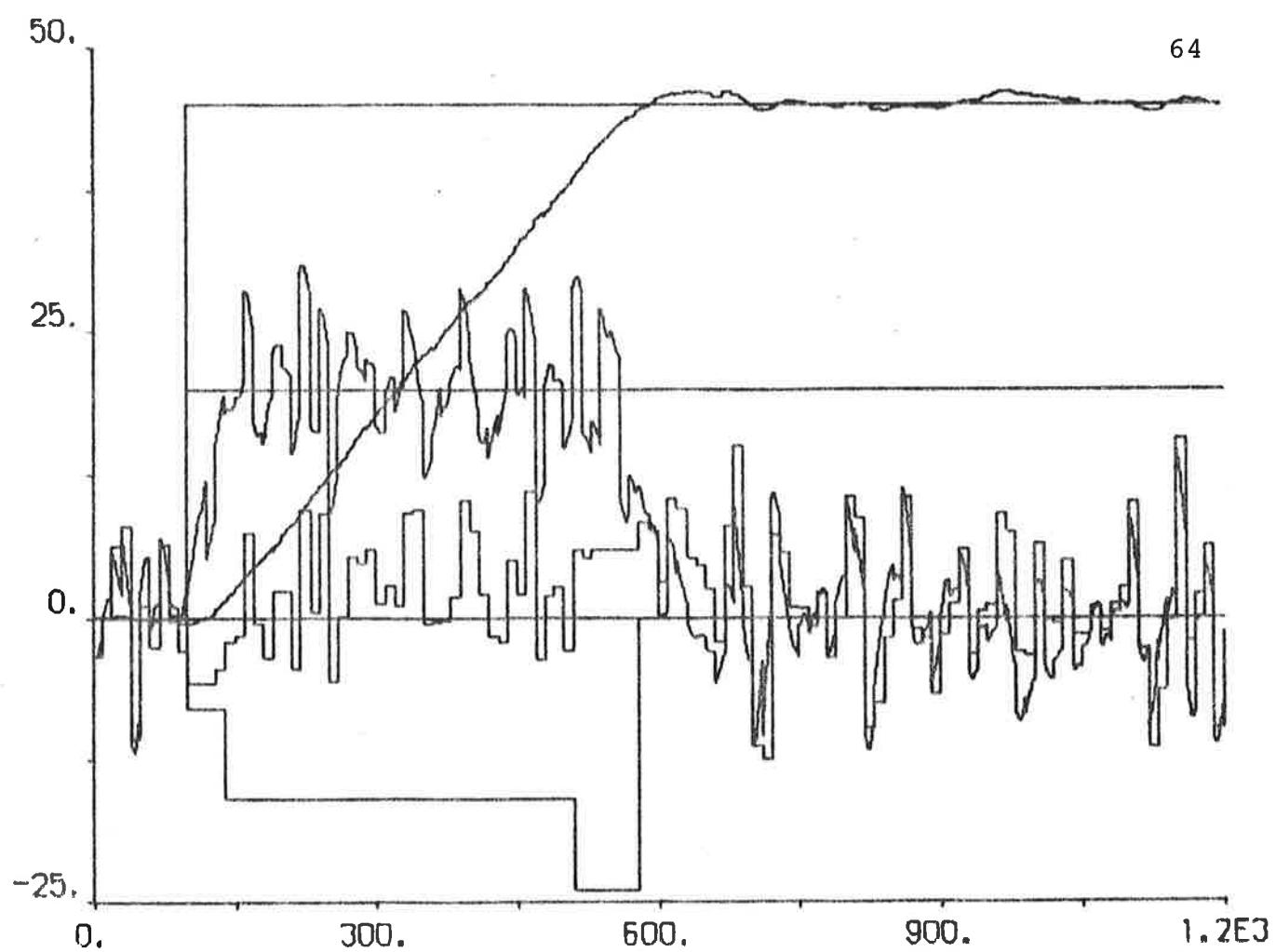


Fig. 5.39 - Stochastic disturbances: $T = 22.3 \text{ m}$, $\alpha = 90 \text{ deg}$,
 $\sigma_r = 0.02 \text{ deg/s}$, $\Delta\psi_{\text{ref}} = 45 \text{ deg}$, $r_{\text{ref}} = 0.1 \text{ deg/s}$.

50.

65

25.

0.

-25.

0.

300.

600.

900.

1.2E3

50.

25.

0.

-25.

0.

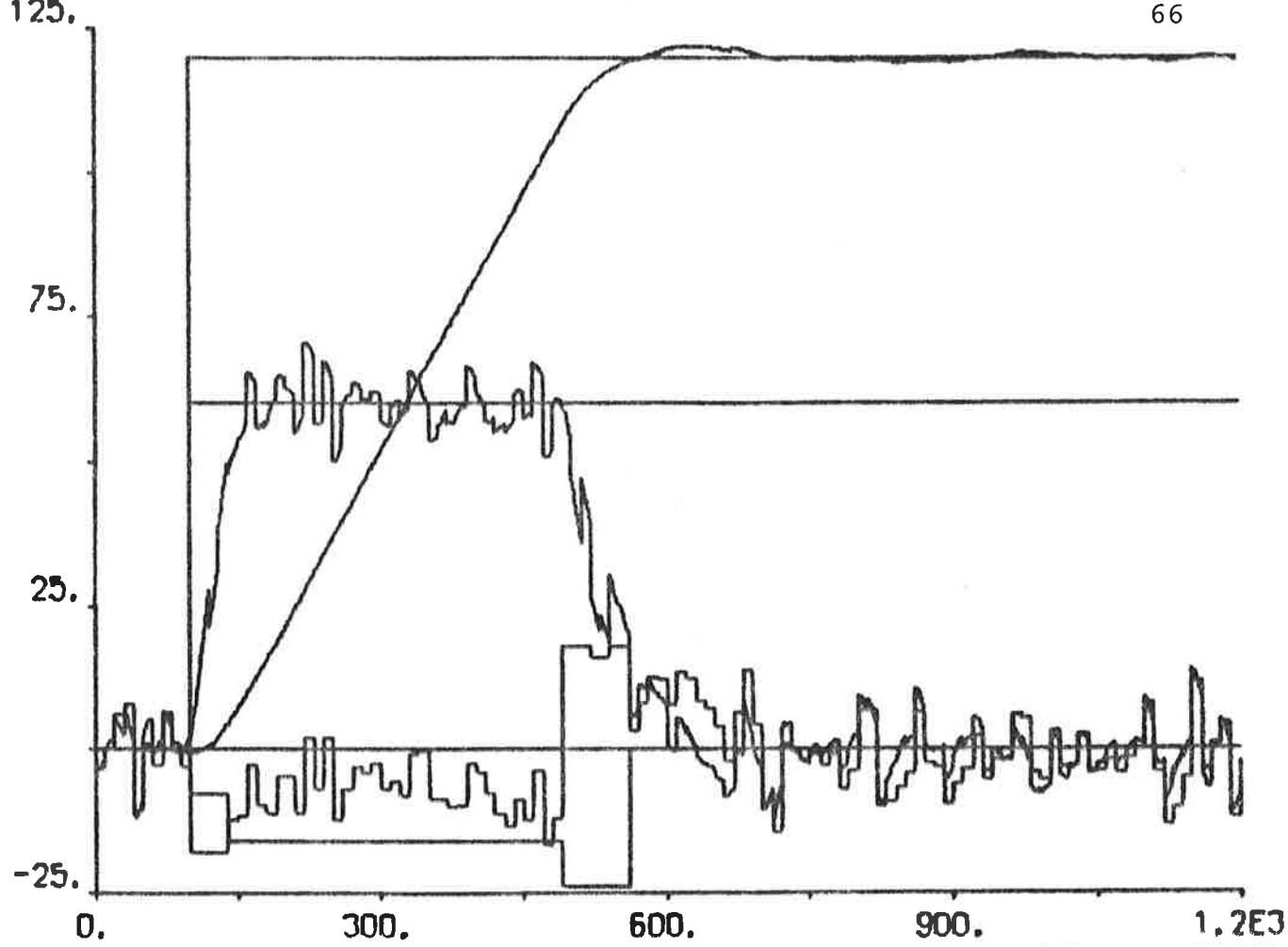
300.

600.

900.

1.2E3

Fig. 5.40 - Stochastic disturbances: $T = 10.5 \text{ m}$, $\alpha = 90 \text{ deg}$,
 $\sigma_r = 0.02 \text{ deg/s}$, $\Delta\psi_{\text{ref}} = 45 \text{ deg}$, $r_{\text{ref}} = 0.1 \text{ deg/s}$.



300.

600.

900.

1.2E3

300.

600.

900.

1.2E3

Fig. 5.41 - Stochastic disturbances: $T = 22.3$ m, $\alpha = 90$ deg,
 $\sigma_r = 0.02$ deg/s, $\Delta\psi_{ref} = 120$ deg, $r_{ref} = 0.3$ deg/s.

75.

25.

-25.

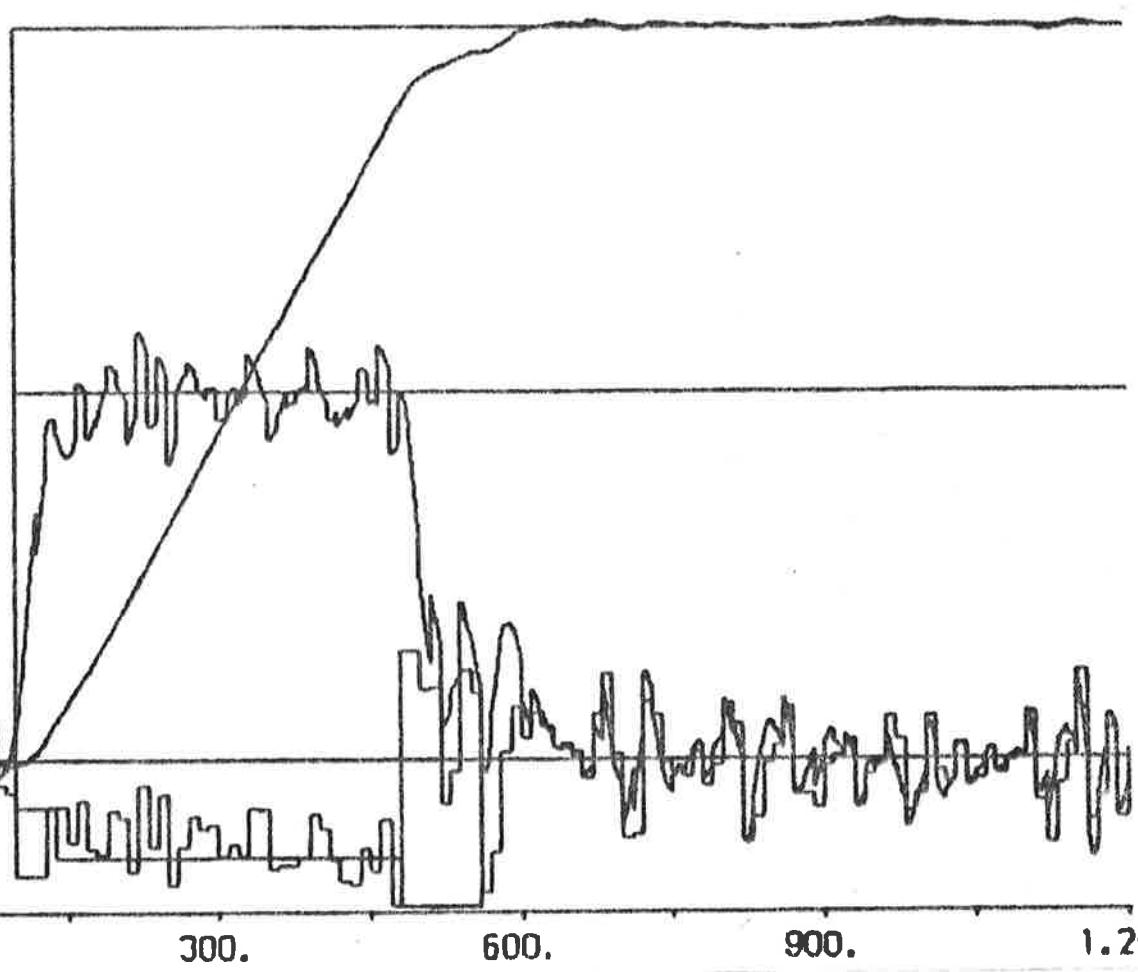
0.

300.

600.

900.

1.2E3



125.

75.

25.

-25.

0.

300.

600.

900.

1.2E3

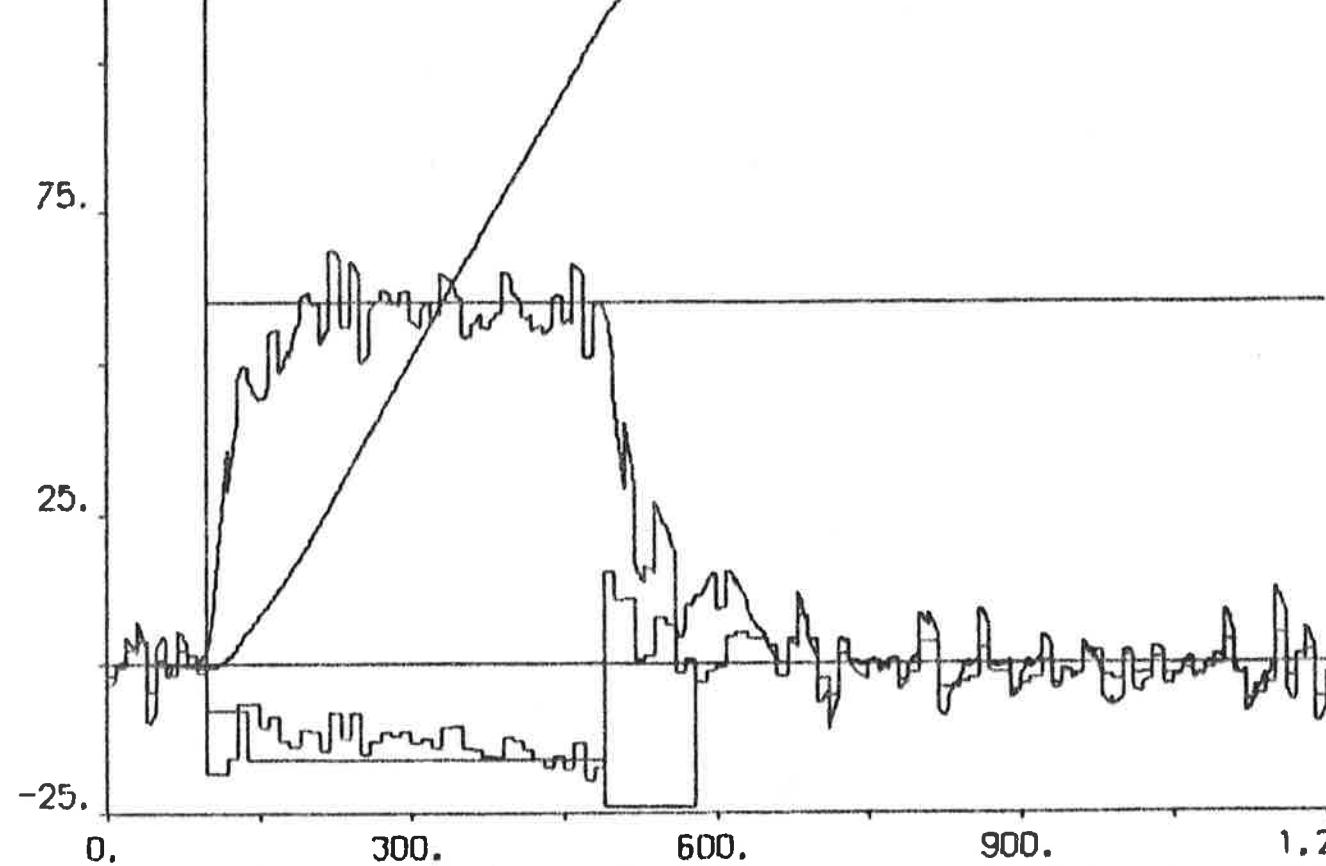


Fig. 5.42 - Stochastic disturbances: $T = 10.5$ m, $\alpha = 90$ deg,
 $\sigma_r = 0.02$ deg/s, $\Delta\psi_{ref} = 120$ deg, $r_{ref} = 0.3$ deg/s.

6. CONCLUSIONS

The simulations have shown that a yaw regulator consisting of different discrete, fixed gain PID-regulators is able to perform quite satisfactorily yaws of a 350 000 tdw tanker in both full load condition and ballast condition. It is not necessary to change the parameters of the yaw regulator when the load is changed, but it is, however, possible to improve the performance of the yaw regulator if information of the draught is available. Only full speed simulations have been performed. It is, of course, necessary to introduce speed-dependent parameters of the yaw regulator to obtain a good performance for all speeds.

Two sets of yaw regulator parameters have been tested. The simulations have shown that the first parameter set, containing rather large gain factors, is preferable. If, however, the yaw rate signal is very noisy, the second parameter set with smaller gain factors may be considered to decrease the rudder deviations.

7. REFERENCES

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SSPA (1974) : "Kockums 350 000 tdw tankfartyg", PM 1965-1,
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CONNECTING SYSTEM T1

TIME T

W1@TANK1@=0.
W2@TANK1@=0.
EE1@TANK1@=0.
EE2@TANK1@=0.
DELC@TANK1@=DEL0

DEL0:10.

END

CONNECTING SYSTEM T2
W1ATANK1A=0,
W2ATANK1A=0,
EE1ATANK1A=0,
EE2ATANK1A=0,
DELCAATANK1A=DOUTAZIGA
PSAZIGA=PSIMNATANK1A
DELZAZIGA=DOUTAZIGA
PSINN=PSIMNATANK1A
END

CONNECTING SYSTEM T3
F
TIME T
E
W1ATANK1A=0.
W2ATANK1A=0.
EE1ATANK1A=0.
EE2ATANK1A=0.
RREFAYAW1A=IF T<TO THEN U, ELSE R0
PREFAYAW1A=IF T<TO THEN U, ELSE PSIO
RAYAW1A=RMNATANK1A
PSIAYAW1A=PSIMNATANK1A
DELCATANK1A=DELCAYAW1A
RSC=SC★RMNATANK1A
RFSC=IF T<TU THEN 0, ELSE R0★SC
PSC=SCP★PSIMNATANK1A
PFSC=IF T<TU THEN 0, ELSE PSI0★SCP
ZERO=U.
E
PSIO:45,
R0:0,1
TU:99.99
SC:200.
SCP:1.
E
END

CONNECTING SYSTEM T5
F
TIME T
F
X1ALPFI1A=E1ANOIS1A
X1ALPFI2A=E2ANOIS1A
W1ATANK1A=XOALPFI1A
W2ATANK1A=XOALPFI2A
EE1ATANK1A=E1ANOIS2A
EE2ATANK1A=E2ANOIS2A
RREFAYAW1A=IF T<TU THEN 0. ELSE RU
PREFAYAW1A=IF T<TU THEN 0. ELSE PSIO
RAYAW1A=RMNATANK1A
PSIAYAW1A=PSIMNATANK1A
DELCATANK1A=DELCAYAW1A
RSC=SC*RMNATANK1A
RFSC=IF T<TU THEN 0. ELSE RU*SC
PSC=SCP*PSIMNATANK1A
PFSC=IF T<TU THEN 0. ELSE PSIO*SCP
ZERO=0.
F
PSIO:45.
RU:0.1
TU:99.99
SC:200.
SCP:1.
F
END

```
CONTINUOUS SYSTEM ZIG
TIME T
INPUT PS DELZ
OUTPUT DOUT
DOUT=IF T<10 THEN DEL0 ELSE IF -PS<DELZ THEN DEL0 ELSE -DEL0
DEL0:10
END
```

CONTINUOUS SYSTEM TANK1

INPUT DELC W1 W2 EE1 EE2

$\#DEL_C$ = RUDDER COMMAND ÄDEGR
 $\#W_1$ = FILTERED NOISE ÄM/(S*S)
 $\#W_2$ = FILTERED NOISE Ä1/(S*S)
 $\#E_E1$ = MEASUREMENT NOISE ÄDEG/S
 $\#E_E2$ = MEASUREMENT NOISE ÄDEGR

OUTPUT RMN PSIMN

$\#RMN$ = YAW RATE INCL. NOISE ÄDEG/S
 $\#PSIMN$ = HEADING INCL. NOISE ÄDEGR

STATE DEL U V R PSI X Y

$\#DEL$ = RUDDER ANGLE ÄRADÄ
 $\#U$ = FORWARD VELOCITY ÄM/S
 $\#V$ = SWAY VELOCITY ÄM/S
 $\#R$ = YAW RATE Ä1/SÄ*100
 $\#PSI$ = HEADING ÄRADÄ
 $\#X$ = X-COORDINATE ÄKMA
 $\#Y$ = Y-COORDINATE ÄKMA

DER DDEL DU DV DR DPSI DX DY

INITIAL

$U_0=U_0/CMK$
 $U=U_0$
 $SGL=SQRT(G*L)$

$F_1=(22.3-TT)/11.8$
 $F_2=(TT-10.5)/11.8$
 $N=1.46*U_0/(17.25*F_1+15.8*F_2)$

$TS_1=1/TS$
 $TS_2=TS_1/CRG$
 $DL_1=DL/CRG$

$XUD=XUD_1*F_1+XUD_2*F_2$
 $XUDL=XUD*L$
 $XUU=(XUU_1*F_1+XUU_2*F_2)/XUDL$
 $XVR=(XVR_1*F_1+XVR_2*F_2)/XUD$
 $XRR=(XRR_1*F_1+XRR_2*F_2)*L/XUD$
 $XUV=XUVVV/(G*L*XUDL)$
 $XUDD=(XUDD_1*F_1+XUDD_2*F_2)/XUDL$
 $XT=X1T/XUD$

$YVD=YVD_1*F_1+YVD_2*F_2$
 $YVDL=YVD*L$
 $YRU_1=YRU/YVD$
 $YRUU_1=YRUU/(SGL*YVD)$
 $YUV=(YUV_1*F_1+YUV_2*F_2)/YVDL$
 $YUUV=(YUUV_1*F_1+YUUV_2*F_2)/(SGL*YVDL)$
 $YVV=(YVV_1*F_1+YVV_2*F_2)/YVD$
 $YRAV=(YRAV_1*F_1+YRAV_2*F_2)/YVD$
 $YARV=(YARV_1*F_1+YARV_2*F_2)/YVD$
 $YUUD=(YUUD_1*F_1+YUUD_2*F_2)/YVDL$
 $YTD_1=YTD/YVD$
 $KTY_1=KTY/YVD$

```

NRDL=NRD*L
NRDLL=NRDL*L
NRU=(NRU1*F1+NRU2*F2)/NRDL
NRUU=(NRUU1*F1+NRUU2*F2)/(SGL*NRDL)
NUV=(NUV1*F1+NUV2*F2)/NRDLL
NUUV=(NUUV1*F1+NUUV2*F2)/(SGL*NRDLL)
NVV=(NVV1*F1+NVV2*F2)/NRDLL
NRR=(NRR1*F1+NRR2*F2)/NRD
NRAV=(NRAV1*F1+NRAV2*F2)/NRDL
NARV=(NARV1*F1+NARV2*F2)/NRDL
NUUD=(NUUD1*F1+NUUD2*F2)/NRDLL
NTD1=NTD/NRDL
KTN1=KTN/NRDL

```

```

XF=FW/XUD
YF=FW/YVD
NF=FW*L V/NRDLL

```

```

JJ1=(1-W)/(N*D)
DISPL=DISP1*F1+DISP2*F2
TT1=N*N*D*D*D*D/DISPL
JJ=U01*JJ1
JJP=JJ/SQRT(1+JJ*JJ)
KKT=-0.33*JJP*JJP-0.38*JJP+0.35
TM0=KKT*(1+JJ*JJ)*TT1
LL1=CMK*L1
ALF1=ALFA/CRG

```

OUTPUT

```

RM=CRG*R/100.
RMN=RM+EE1
PSIM=CRG*PSI
PSIMN=PSIM+EE2
DELM=CRG*DEL
UM=CMK*U
VM=CMK*V
V1=LL1*R/100.+CMK*V
VV=SQRT(UM*UM+VM*VM)
BETA=-CRG*ATAN(V/U)

```

DYNAMICS

```

RR=R/100.
APSI=ALF1-PSI
SINW=SIN(APSI)
SINP=SIN(PSI)
COSP=COS(PSI)
J=U*JJ1
JP=J/SQRT(1+J*J)
KT=-0.33*JP*JP-0.38*JP+0.35
TM=KT*(1+J*J)*TT1
TM1=IF TM<TM0 THEN TM ELSE TM0
TMD =TM1*DEL
U2=U*U
AV=ABS(V)
AR=ABS(RR)
RU=RR*U
RU2=RU*U
UV=U*V
U2V=U*UV
VAV=V*AV
RAV=RR*AV
ARV=AR*V

```

```

U2D=U2★DEL
DDEL1=-TS1★DEL+TS2★DELC
DDEL=IF DDEL1<-DL1 THEN -DL1 ELSE IF DDEL1>DL1 THEN DL1 ELSE DDEL1
DU=XUU★U2+XVR★V★RR+XRR★RR★RR+XUV★UV★VAV+XUUD★U2D★DEL+XT★TM-XF★COS(APSI)
SL=YRU1★RU+YRUU1★RU2+YUV★UV+YUUV★U2V+YVV★VAV+YRAV★RAV
DV=YARV★ARV+YUUD★U2D+YTD1★TMD+KTY1★TM-YF★SINW+W1/YVD+SL
SL1=NRU★RU+NRUU★RU2+NUV★UV+NUUV★U2V+NVV★VAV+NRR★RR★AR
DR=(SL1+NRAV★RAV+NARV★ARV+NUUD★U2D+NTD1★TMD+KTN1★TM+NF★SINW+W2/NRD)*100.
DPSI=RR
DX=(U★COSP-V★SINP)/1000.
DY=(U★SINP+V★COSP)/1000.

G:9.80665
CMK:1.943844
CRG:57.2958
L:350.
UU:15.8
TT:22.3
TS:5.0
DL:2.32 F2 PUMPS
XUD1:
XUD2:
XUU1:
XUU2:
XVR1:
XVR2:
XRR1:
XRR2:
XUVVV:
XUDD1:
XUDD2:
X1T:
YVD1:
YVD2:
YRU:
YRUU:
YUV1:
YUV2:
YUUV1:
YUUV2:
YVV1:
YVV2:
YRAV1:
YRAV2:
YARV1:
YARV2:
YUUD1:
YUUD2:
YTD:
KTY:
NRD:
NRU1:
NRU2:
NRUU1:
NRUU2:
NUV1:
NUV2:
NUUV1:
NUUV2:
NVV1:
NVV2:

```

NRR1:
NRR2:
NRAV1:
NRAV2:
NARV1:
NARV2:
NUUD1:
NUUD2:
NTD:
KTN:

Fw:0.
Lv:25.
W:0.
D:0.
DISP1:17247.
DISP2:3891200.
L1:164.35
ALFA:0.

END

```

DISCRETE SYSTEM YAW1
F
INPUT R PSI RREF PREF
F
FR = YAW RATE ADEG/SA
FPSI = HEADING ADEGA
FRREF = REF. VALUE OF YAW RATE ADEG/SA
FPREF = REF. VALUE OF HEADING ADEGA
F
OUTPUT DELC
F
FDELc = RUDDER COMMAND ADEGA
F
TIME T
F
STATE PRO MODY MDEL STD INT1 INT2 TF1 TF3
F
FPRO = OLD REF. VALUE OF HEADING ADEGA
FMODY = YAW INDICATOR
FMDEL = MEAN VALUE OF RUDDER ADEGA
FSTD = WEIGHTING FACTOR
FINT1 = INTEGRAL TERM OF PHASE 0
FINT2 = INTEGRAL TERM OF PHASE 2
FTF1 = TIME PHASE 1
FTF3 = TIME PHASE 3
F
NEW NPRO NMODY NMDEL NSTD NINT1 NINT2 NTF1 NTF3
F
TSAMP TS
F
INITIAL
F
STD=1.-BD
F
OUTPUT
F
S1=ABS(PREF-PRO)
S2=PSI-PREF
S3=R-RREF
DD1=K4*S3
DR1=ABS(C1*RREF)
D1=IF DD1<-DR1 THEN -DR1 ELSE IF DD1>DR1 THEN DR1 ELSE DD1
DD2=K7*S2+K8*R
DR2=ABS(C3*RREF)
D2=IF DD2<-DR2 THEN -DR2 ELSE IF DD2>DR2 THEN DR2 ELSE DD2
F
M1=IF MODY<0.5 AND S1>PSIMX THEN 1. ELSE 0.
MA=IF M1>0.5 OR (MODY>0.5 AND MODY<1.5) THEN 1. ELSE 0.
MM1=IF MA>0.5 AND RREF>0. AND S3>-EPS1 THEN 1. ELSE 0.
MM2=IF MA>0.5 AND RREF<0. AND S3<EPS1 THEN 1. ELSE 0.
M2=IF MM1>0.5 OR MM2>0.5 OR TF1>T1 THEN 1. ELSE 0.
MB=IF M2>0.5 OR (MODY>1.5 AND MODY<2.5) THEN 1. ELSE 0.
MM3=IF (MA>0.5 OR MB>0.5) AND S2<0. AND -C2*R<S2 THEN 1. ELSE 0.
MM4=IF (MA>0.5 OR MB>0.5) AND S2>0. AND -C2*R>S2 THEN 1. ELSE 0.
M3=IF MM3>0.5 OR MM4>0.5 THEN 1. ELSE 0.
MC=IF M3>0.5 OR MODY>2.5 THEN 1. ELSE 0.
MC1=IF MC>0.5 AND ABS(R)<EPS2 THEN 1. ELSE 0.
MC2=IF MC>0.5 AND RREF>0. AND S2>-EPS3 THEN 1. ELSE 0.
MC3=IF MC>0.5 AND RREF<0. AND S2<EPS3 THEN 1. ELSE 0.
M4=IF MC1>0.5 OR MC2>0.5 OR MC3>0.5 OR TF3>T3 THEN 1. ELSE 0.
MD=IF M3<0.5 AND M4<0.5 THEN 0. ELSE 1.
ME=IF M3>0.5 AND M4<0.5 THEN 1. ELSE 0.
MF=IF M2>0.5 AND MD<0.5 THEN 1. ELSE 0.

```

```
MG=IF M1>0.5 AND M2<0.5 AND MD<0.5 THEN 1. ELSE 0.
MM5=IF MG>0.5 THEN 1, ELSE IF MF>0.5 THEN 2, ELSE 0,
MM6=IF ME>0.5 THEN 3, ELSE IF M4>0.5 THEN 0, ELSE MODY
MM=IF MM5>0.5 THEN MM5 ELSE MM6
MMS=MM★SCM
F
DC0=K1★S2+K2★R+K3★INT1
DC1=D1+MDEL
DC2=K5★S3+K6★INT2+MDEL
DC3=D2
DDC=IF MM<0.5 THEN DC0 ELSE IF MM>0.5 AND MM<1.5 THEN DC1 ELSE 1000.
DC=IF DDC<999. THEN DDC ELSE IF MM>1.5 AND MM<2.5 THEN DC2 ELSE DC3
F
SS1=MDEL+(STD+BD)★(DC-MDEL)
MH=IF MM>1.5 AND MM<2.5 THEN 1. ELSE 0.
SS2=IF MM<0.5 THEN SS1 ELSE MDEL
SS3=IF M4>0.5 THEN DC ELSE SS2
SS4=IF M4>0.5 THEN 1.-BD ELSE STD
F
NPRO=PREF
NMODY=MM
NMDEL=SS3
NSTD=IF MM<0.5 THEN (1.-BD)*SS4/(1.-BD+SS4) ELSE STD
NINT1=IF MM<0.5 THEN INT1+S2★DT ELSE 0,
NINT2=IF MH>0.5 THEN INT2+S3★DT ELSE 0,
NTF1=IF MM>0.5 AND MM<1.5 THEN TF1+DT ELSE 0.
NTF3=IF MM>2.5 THEN TF3+DT ELSE 0.
F
DELC=DC
F
TS=T+DT
F
DT:10.
BD:0.05
PSIMX:2.5
K1:5.
K2:200.
K3:0.005
K4:200.
K5:200.
K6:8.
K7:2.
K8:200.
EPS1:0.
EPS2:0.02
EPS3:1.
C1:60.
C2:50.
C3:60.
T1:30.
T3:80.
SCM:-8.
F
END
```

```
CONTINUOUS SYSTEM LPFI1
INPUT XI
OUTPUT XO
STATE X1 X2
DER DX1 DX2
INITIAL
X1:0
X2:0
T=TP/6.283185
A1=-2*CS/T
A2=-1/(T*T)
CC2=AK/(T*T)
OUTPUT
XO=CC2*X2
DYNAMICS
DX1=A1*X1+A2*X2+XI
DX2=X1
F
AK:1    FILTER GAIN
TP:8    PERIOD TIME OF PEAK FREQ.
CS:0.25 DAMPING FACTOR
F
F    PEAK GAIN FOR FREQ.=1/TP : AK/(2*CS)
F
END
```

```
CONTINUOUS SYSTEM LPFI2
INPUT XI
OUTPUT XO
STATE X1 X2
DER DX1 DX2
INITIAL
X1:0
X2:0
T=TP/6.283185
A1=-2*CS/T
A2=-1/(T*T)
CC2=AK/(T*T)
OUTPUT
XO=CC2*X2
DYNAMICS
DX1=A1*X1+A2*X2+XI
DX2=X1
F
AK:1    FILTER GAIN
TP:8    PERIOD TIME OF PEAK FREQ.
CS:0.25 DAMPING FACTOR
F
F    PEAK GAIN FOR FREQ.=1/TP : AK/(2*CS)
F
END
```

```
C SUBROUTINE SYSTS
C
C      DIMENSION S(60)
C      COMMON/DESTIN/ISYST, IDUM
C      COMMON/NSYSTS/NSYST
C      COMMON/NALLOC/NS
C      COMMON/SAVEAR/IS(18)
C
C      NSYST=2
C      NS=60
C
C      GO TO (1,2),ISYST
C
1      CALL SNOISE('NOIS1',IS(1),S)
      RETURN
2      CALL SNOISE('NOIS2',IS(10),S)
      RETURN
      END
```

C SIMNON -
 C AN INTERACTIVE SIMULATION PROGRAM
 C FOR NONLINEAR SYSTEMS
 C
 C MAIN PROGRAM
 C
 C AUTHOR HILDING ELMQVIST
 C
 C REFERENCE
 C -----
 C H. ELMQVIST: SIMNON - AN INTERACTIVE SIMULATION
 C PROGRAM FOR NONLINEAR SYSTEMS -
 C USER'S MANUAL
 C
 C DATA BASE
 C -----
 C /PSCODE/ IPSEUD()
 C IPSEUD- PSEUDO CODE AREA
 C
 C /VARTAB/ VARS(),IPNTS(),ITYPES()
 C VARS - IDENTIFIER TABLE
 C IPNTS - ADDRESS TABLE
 C ITYPES- TYPE TABLE
 C 1: TIME
 C 2: STATE
 C 3: INPUT
 C 4: OUTPUT
 C 5: INIT
 C 6: DER
 C 7: NEW
 C 8: TSAMP
 C 9: PAR
 C 10: VAR
 C
 C /VALUES/ VALUE()
 C VALUE - VALUE TABLE AND LITTERAL TABLE
 C
 C /SYSINF/ NASYST,ASYSTS(),IVARS(,2),INFSYS(),LENTRY(,3)
 C NASYST- NUMBER OF ACTIVE SYSTEMS
 C ASYSTS- SYSTEM IDENTIFIERS FOR ACTIVE SYSTEMS
 C IVARS - DEFINING THE POSITION OF THE VARIABLE
 C TABLE FOR EACH SYSTEM
 C INFSYS- SYSTEM TYPE
 C 1: CONNECTING
 C 2: CONTINUOUS
 C 3: DISCRETE
 C 4: CONTINUOUS (FORTRAN)
 C 5: DISCRETE (FORTRAN)
 C LETRY- ENTRY POINTS FOR EACH ACTIVE SYSTEM
 C (,1): INITIAL-SECTION
 C OR THE NUMBER OF A FORTRAN-SYSTEM
 C (,2): OUTPUT- OR CONNECT-SECTION
 C (,3): DYNAMICS-SECTION
 C
 C /EXTCOM/ IEVAL,IERR,TYPE,SYSID,NEXTSY,NS
 C IEVAL - POINTER IN VARIABLE TABLE
 C IERR - ERROR INDICATOR
 C TYPE - SYSTEM TYPE FROM SUBROUTINE IDENT
 C 'CONT' OR 'DISCR'

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C      SYSID - SYSTEM IDENTIFIER FROM SUBROUTINE IDENT
C      NEXTSY- NUMBER OF EXTERNAL SYSTEMS
C      NS     - NUMBER OF ELEMENTS IN THE ALLOCATION AREA
C /ENTRY/ NTRINT,NTRDER,NTRSMP
C      NTRINT- ENTRY POINT FOR INITIAL COMPUTATIONS
C      NTRDER- ENTRY POINT FOR COMPUTATIONS OF DERIVATIVES
C      NTRSMP- ENTRY POINT FOR SAMPLING

C /ENTRY/ LENTRY
C      LENTRY- ACTUAL ENTRY POINT FOR CALCUL

C /PNTS/ NXC,NXD,KXC( ),KDXC( ),KXI( ),KTSAMP( )
C      NXC   - NUMBER OF STATES IN CONTINUOUS SYSTEMS
C      NXD   - NUMBER OF STATES IN DISCRETE SYSTEMS
C      KX    - POINTERS TO STATE VARIABLES
C      KDX   - POINTERS TO DER- AND NEW-VARIABLES
C      KXI   - POINTERS TO INIT-VARIABLES
C      KTSAMP- POINTERS TO TSAMP-VARIABLES

C /COMINF/ (SEE INTRAC)

C /MACINF/ (SEE INTRAC)

C /MESS/ MESS
C      MESS - MESSAGE INDICATOR

C /SIMN/ NOSYST,OVFLO,IPLCOM,IEXIT,IWARN,ICOMPU,LDARK
C      ,NOCONT,LLPCOM,INIDRA
C      NOSYST- TRUE IF NO SYSTEM DEFINED
C      OVFLO - TRUE IF OVERFLOW CHECK PERFORMED
C      IPLCOM- TRUE IF PLOT-COMMAND SHOULD BE WRITTEN
C      IEXIT - TRUE IF THE EDITOR IS TO MAKE
C              AUTOMATIC EXIT (SYST)
C      IWARN - TRUE IF WARNINGS SHOULD BE WRITTEN
C      ICOMPU- TRUE IF MESSAGE ABOUT COMPUTATIONS
C              IN OUTPUT-SECTION SHOULD BE GIVEN
C      LDARK - TRUE IF NOT VISABLE LINES AT SAMPLINGS
C      NOCONT- TRUE IF CONTINUATION OF THE SIMULATION
C              IS NOT POSSIBLE
C      LLPCOM- TRUE IF COMMANDS SHOULD BE ECHOED ON THE LP
C      INIDRA- TRUE IF INITIALIZATION OF DRAW

C /PLT/ NPLT,IVADRC( ),IHADR,PLTCOM( )
C      NPLT - NUMBER OF PLOT-VARIABLES
C      IVADR - POINTERS TO VERTICAL VARIABLES
C      IHADR - POINTER TO HORIZONTAL VARIABLE
C      PLTCOM- BUFFER FOR PLOT-COMMAND

C /STOVAR/ NSTV,IVARS( ),ISYSS( )
C      NSTV - NUMBER OF VARIABLES TO BE STORED
C      IVARS - POINTERS TO VARIABLE NAMES
C      ISYSS - POINTERS TO SYSTEM IDENTIFIERS

C /DATCOM/ FILE,DTF
C      FILE - STORE FILE NAME
C      DTF  - MINIMAL TIME INCREMENT

C /SHOVAR/ NSHVAR
C      NSHVAR- NUMBER OF SHOWED VARIABLES SINCE AXES

C /AX/ HMIN,DH,VMIN,DV
C      HMIN - HORIZONTAL MINIMUM
C      DH   - HORIZONTAL VALUE PER CENTIMETER
C      VMIN - VERTICAL MINIMUM

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C          DV      - VERTICAL VALUE PER CENTIMETER
C
C          /ERRWEI/ EPS,WEIGHT( )
C                  EPS   - ERROR BOUND
C                  WEIGHT- ERROR WEIGHTS
C
C          /ALG/ IALG
C                  IALG  - SPECIFIES INTEGRATION ALGORITHM
C                               1: HAMPC
C                               2: RK
C                               3: RKFIX
C
C          /MARKS/ IMARK,MRK,TMRK,DTMRK
C                  IMARK - TRUE IF MARKS WANTED
C                  MRK   - SPECIFIES WHICH MARKS
C                  TMRK  - TIME FOR NEXT MARKS
C                  DTMRK - TIME DISTANCE BETWEEN MARKS
C
C          /USER/ LSTOP,LDARK,LCALUS,NRESUM,LFIRST,NOPLLOT
C                  LSTOP - TRUE IF SIMULATION SHOULD BE STOPPED
C                  LDARK - TRUE IF DARK LINE
C                  LCALUS- TRUE IF THE SUBROUTINE USRSUB SHOULD BE CALLED
C                  NRESUM- NUMBER OF DISCRETE SYSTEMS THAT HASN'T
C                           PRODUCED A DISCONTINUITY
C                  LFIRST- TRUE IF SYSTS CALLED FIRST TIMES
C                  NOPLLOT- IF TRUE NO PLOT
C
C          /DESTIN/ ISYST,IPART
C                  ISYST - SYSTEM NUMBER
C                  IPART - PART NUMBER
C
C          /NSYSTS/ NSYST
C                  NSYST - NUMBER OF EXTERNAL SYSTEMS
C
C          /NALLOC/ NALL
C                  NALL  - NUMBER OF ELEMENTS IN THE ALLOCATION AREA
C
C          /TIME/ T
C                  T      - THE SIMULATION TIME
C
C          /STATES/ X( )
C                  X      - STATES OF CONTINUOUS SYSTEMS
C
C          /DERS/ DX( )
C                  DX    - DERIVATIVES OF THE STATES
C
C          /CMPVAR/ MODE,IASYST,ISYTYP,IERR,IVAR1,IVAR2,IVAL1,IVAL2
C                  L,LENTR1,LENTR2,LENTR3
C                  MODE  - COMPILER MODE
C                               1: SYSTEM HEADING
C                               2:
C                               3: DECLARATIONS
C                               4:
C                               5: INITIAL-SECTION
C                               6: OUTPUT-SECTION
C                               7: DYNAMICS-SECTION
C                               8: CONNECT-SECTION
C                               9: END
C
C                  IASYST- INDEX FOR ACTUAL SYSTEM
C                  ISYTYP- SYSTEM TYPE
C                               1: CONNECTING
C                               2: CONTINUOUS
C                               3: DISCRETE
C
C                  IERR  - ERROR FLAG

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C      IVAR1 - INDEX FOR LOWER BOUND IN VARIABLE TABLE
C      IVAR2 - INDEX FOR UPPER BOUND IN VARIABLE TABLE
C      IVAL1 - POINTER IN THE VALUE TABLE
C      IVAL2 - POINTER IN THE LITTERAL TABLE
C      L    - POINTER IN THE PSEUDO CODE AREA
C      LENTR1- POINTER TO INITAL-SECTION
C      LENTR2- POINTER TO OUTPUT- OR CONNECT-SECTION
C      LENTR3- POINTER TO DYNAMICS-SECTION
C
C      /NXPNT/ NXP( >2)
C          NXP   - SPECIFIES WHICH STATES THAT BELONGS
C                      TO EACH DISCRETE SYSTEM
C
C      /COND/ LSAMP,LSAMPS( )
C          LSAMP - TRUE IF SAMPLING IS TO BE DONE
C          LSAMPS- SPECIFIES WHICH SYSTEMS THAT IS TO BE SAMPLED
C
C      /LIMITS/ MPSC,MVAR,MVAL,MX
C          MPSC - NUMBER OF ELEMENTS IN PSEUDO CODE AREA
C          MVAR - NUMBER OF ELEMENTS IN VARIABLE TABLE
C          MVAL - NUMBER OF ELEMENTS IN VALUE TABLE
C          MX    - MAXIMUM NUMBER OF STATES
C
C      /SIMARG/ T1,T2,DT,LCONT,LMARK
C          T1-     START TIME
C          T2-     STOP TIME
C          DT-     TIME INCREMENT
C          LCONT-  LOGICAL VARIABLE TO INDICATE IF CONTINUATION
C                      OF SIMULATION IS WANTED
C          LMARK-  LOGICAL VARIABLE INDICATING IF MARKS IS WANTED
C                      DURING THE PLOTTING
C
C      /ARGSAV/ H1,H2,V1,V2
C          H1    - LAST HORIZONTAL MINIMUM (AXES)
C          H2    - LAST HORIZONTAL MAXIMUM
C          V1    - LAST VERTICAL MINIMUM
C          V2    - LAST VERTICAL MAXIMUM
C
C      /AX1NF/ IX0,IY0,XAX,YAX
C          IX0,IY0 - ORIGO FOR AXES (TEKPOINTS)
C          XAX,YAX - LENGTH OF AXES (CM)
C
C
C      SUBROUTINE REQUIRED
C          ISIMN
C          ESIMN
C          SIMNSY
C          SIMU
C
C
COMMON/ALLCOM/IDD(3)
COMMON /PSCODE/ IDUM1(4000)
COMMON /VARTAB/ IDUM2(1000),DUM2(500)
COMMON /VALUES/ DUM3(500)
COMMON /SYSINF/ IDUM4(151),DUM4(25)
COMMON /EXTCOM/ IDUM5(4),DUM5(2)
COMMON /ENTRYS/ IDUM6(3)
COMMON /ENTRY/ IDUM7
COMMON /PNTS/ IDUM8(177)
COMMON /COMINF/ IDUM9(33),DUM9(41)
COMMON /MACINF/ IDUM10(191),DUM10(107)
COMMON /MESSS/ IDUM11
COMMON /SIMN/ IDUM12(10)

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COMMON /PLT/    IDUM13(12),DUM13(16)
COMMON /STOVAR/  IDU135(101)
COMMON /DATCOM/  DUM136(2)
COMMON /SHOVAR/  IDU137
C ***** HCOPY *****
COMMON/HCPCom/DUM138(10),IDU138(30)
C *****
COMMON /AX/      DUM14(4)
COMMON /ERRWEI/   DUM15(51)
COMMON /ALG/     IDUM16
COMMON /MARKS/   IDUM17(2),DUM17(2)
COMMON /USER/    IDUM18(6)
COMMON /DESTIN/  IDUM19(2)
COMMON /NSYSTS/  IDM191
COMMON /NALLOC/  IDM192
COMMON /TIME/    DUM20
COMMON /STATES/  DUM21(50)
COMMON /DERS/    DUM211(50)
COMMON /CMPVAR/  IDUM23(12)
COMMON /NXPNT/   IDUM24(50)
COMMON /COND/    IDUM25(26)
COMMON /LIMITS/  MPSC,IDM261,MVAL,MX
COMMON /SIMARG/  IDUM26(2),DUM26(3)
COMMON /ARGSAV/  DUM0(4)
COMMON /AXINF/   IDUM27(2),DUM27(2)

C
C
MPSC=4000
MVAL=500
MX=20
CALL LOGG(0)
CALL LPHDL(0)
C
CALL ISIMN
C
MODE=1
10 CALL ESIMN(MODE)
C
GOTO(1,2,3,4),MODE
C
1 CALL LPHDL(1)
CALL LOGG(1)
STOP
C
2 CALL SIMNSY
GO TO 10
C
3 CALL SIMU
GO TO 10
C
4 CALL LPHDL(2)
CALL LOGG(2)
STOP
END

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