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Nonlinear response of quantum cascade structures

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The gain spectrum of a terahertz quantum cascade laser is analyzed by a nonequilibrium Green’s functions approach. Higher harmonics of the response function were retrievable, providing a way to approach nonlinear phenomena in quantum cascade lasers theoretically. Gain is simulated under operation conditions and results are presented both for linear response and strong laser fields. An iterative way of reconstructing the field strength inside the laser cavity at lasing conditions is described using a measured value of the level of the losses of the studied system. Comparison with recent experimental data from time-domain-spectroscopy indicates that the experimental situation is beyond linear response. © 2012 American Institute of Physics.

Possible coherent radiation in the terahertz range has been a very strong motivation for research in the field of terahertz quantum cascade lasers1,2 (THz-QCLs), which would enable a wide range of applications such as imaging and spectroscopy. However, compact devices operating over cryogenic temperatures are a practical requirement for applications and currently the most promising designs are based on resonant phonon extraction, achieving operating temperatures up to ~200 K.

The key physical quantity in any QCL is the gain which describes the amplification of the optical field in the heterostructure material. In recent years, this quantity has been measured in detail in time-domain-spectroscopy (TDS) experiments2,3 where THz-QCLs are probed by ultra short pulses providing information on both phase and amplitude of the transmitted pulse, whereas the gain spectrum is reconstructed by a Fourier transform. The pulse is made as strong as possible in order to get a good signal to noise ratio but it is not known how the system dynamics are affected by such a measurement. The simulation of THz QCLs relies on a consistent treatment of tunneling and scattering, either by hybrid density matrix/rate equation schemes4–8 or more evolved nonequilibrium Green’s function (NEGF) theory9–13. Here, we present an extension of our NEGF scheme14 towards the treatment of high intensities inside the QCL, going beyond linear response.14–17

Higher harmonics of the response function were retrievable, providing a way to approach nonlinear phenomena in quantum cascade lasers theoretically. Gain is simulated under operation conditions and results are presented both for linear response and strong laser fields. An iterative way of reconstructing the field strength inside the laser cavity at lasing conditions is described using a measured value of the level of the losses of the studied system. Comparison with recent experimental data from time-domain-spectroscopy indicates that the experimental situation is beyond linear response. © 2012 American Institute of Physics.
We note that for both simulations, the main peak as well as the low-bias behavior are in good agreement with the experimental data. In contrast, for bias drops per period of about 40–45 mV, we observe a spurious extra peak due to tunneling between state 1 and state 3 of the next neighboring period. Such extra peaks for long-range tunneling have been observed in our model for other THz-structures as well, and we currently attribute them to the lack of electron-electron scattering processes.\(^2\)\(^5\)

Fig. 2 shows the calculated gain spectra (lines) for three different dc biases, as depicted in Fig. 1(b), both for low (a) and high (b) ac field strength. For comparison, we display the experimental data from Ref. 8 in both parts. The low current point (\(I_{\text{low}}\)) is considered to be at the bias where state 1 and 4 become aligned and electrons start to tunnel through the system as those levels are at resonance. Here, we are far below threshold and mainly absorption is seen at the laser frequency of 2.2 THz, as state 4 – the lower laser state – is populated, while 5 is still mostly empty. This is changed as current is increased and we approach the medium current point (\(I_{\text{med}}\)). This is taken where the system is almost at, but still below the threshold current. Here the states 1’ and 5 start to align, creating population inversion at the laser frequency. At operating conditions, where the third and last point (\(I_{\text{high}}\)) at high current is taken, gain is above the level of the losses\(^8\) of 18 cm\(^{-1}\) and can now sustain lasing as the population inversion is at its maximum.

The simulations at low and high ac field strength shown in Fig. 2 differ drastically, but the general picture is that around the laser frequency, large losses at low current develop into gain as bias is raised, as observed by Refs. 8 and 26. At a more detailed level, the low ac field strength simulations exhibit stronger features which are not reflected in the experimental data. At higher ac field strength however, the overall agreement becomes better, mainly due to a redistribution of carriers (bleaching). However, the strong absorption feature around 1.2 THz for medium and high current density in the experimental data does not appear in the simulations, for which we do not have any explanation. The better agreement of experimental data with high ac field indicates that the experimental conditions are beyond linear response.

Here, it is important to address the fundamental differences between experiment and simulation. In the simulations, a monochromatic ac field is applied and the gain spectrum is constructed frequency by frequency. In the experimental case, the situation is quite different. A pulse, containing all frequencies within the bandwidth (typically 3 THz (Ref. 7)), is sent into the sample, and the way this...
pulse has changed by passing through the structure determines the gain spectrum. Compared to the simulations, where we only measure at the frequency where we excite, this is the opposite, as all frequencies are subject to excitations and all frequencies are also measured. Therefore, our modeling can only be seen as approximate. In addition, the experimental data are the difference of measurements between the unbiased QCL and the QCL at the chosen measuring bias. This way the background is effectively subtracted. If the structure exhibits less losses at some point than it does at zero bias, this is measured as gain. In the simulations however, we only extract the gain from the conductivity extracted from the $h=1$ component of the Green’s functions, as we do not have to take losses into account and thus only look at the intrinsic gain spectra. Simulations at very low bias, i.e., the off-state, show absorption peaks at $0.9$ THz and $2.7$ THz, which could explain corresponding features in the experimental gain spectra.

We have demonstrated that the response varies significantly with the ac field strength. Thus, it is important to question whether the ac field strengths used in the simulations are comparable to their experimental counterpart. In order for the effects of high ac field strengths shown in Fig. 2(b) to be of any relevance, the power coupled into the QCL structure during the experimental measurements must be sufficient. Addressing this question, consider the experimental situation governing the in-coupling of light.\textsuperscript{8} A pumping femtosecond pulse of $125$ mW hits the emitter section of the same QCL as described in Fig. 1. The pulse generates a photocurrent giving an electric field transient that is coupled across an air distance of $4$ μm into the QCL section of interest. Our value $eF_{ac,d} = 6$ meV corresponds to a power of $40$ mW in the cavity, which requires an extremely efficient conversion in the emitter and good coupling between the structures. It is far from clear, whether the probing field can reach these intensities. Strong ac fields at lasing conditions would be capable of generating these effects, but this would then only contribute above threshold current.

In a working laser, the gain will clamp at the level of the losses, as the population inversion will stabilize around the current. Effects, but this would then only contribute above threshold at lasing conditions would be capable of generating these intensities. Strong ac fields at lasing conditions would be capable of generating these effects, but this would then only contribute above threshold current.

To show the importance of including higher orders of the Fourier decomposed Green’s function in Eq. (1), simulations with $|h| \leq 1$ only and also $|h| \leq 3$ are shown in Fig. 3(a) for $eF_{ac,d} = 8$ meV which is the highest ac-field used. $|h| \leq 1$ (dashed) shows a clear deviation from the $|h| \leq 2$ case (full line) while the simulations with $|h| \leq 3$ confirm the quality of our $|h| \leq 2$ calculations for $eF_{ac,d} \leq |h|\Omega$.

The $F_{ac}$-assisted current at the intensities shown in Fig. 3(b) is displayed as a dotted line in Fig. 1(b). It increases proportional to the intensity compared to the non-lasing current. Thus when lasing sets in, we see a kink in the current, just as in the experimental data of Fig. 1(b) at $53$ mV per period. As the calculated kink appears somewhat stronger, our calculated lasing intensities could be a little bit too high. This may be related to the fact that the experimental lasing frequency of $2.2$ THz is not precisely at the peak of the gain spectrum.

In conclusion, we have simulated gain under operation by including higher orders of the Fourier decomposed Green’s function in order to include nonlinear effects. We have found a way to calculate the power of the laser using an experimental value of the level of the losses and by iteratively matching the gain to that level and then extract the intensity of such a configuration. It has also been shown that gain bleaches under high intensity conditions and that this might be a non-negligible effect in THz-TDS measurements.

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\textsuperscript{2}B. S. Williams, \textit{Nat. Photonics} \textbf{1}, 517 (2007).
23. A higher values of $g$ also reduces gain below 18 cm$^{-1}$, which would prevent from lasing operation, not shown.
25. This possibility had been pointed out to us by H. Callebaut and Q. Hu.