Observation and Quadrupole-Moment Measurement of the First Superdeformed Band in the $A \sim 60$ Mass Region


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A high-spin rotational cascade of six $\gamma$ rays has been observed in $^{62}\text{Zn}$. The quadrupole moment of $2.7^{+0.5}_{-0.6}$ $b$ measured for this band corresponds to a deformation $\beta_2 = 0.45^{+0.07}_{-0.08}$. The properties of this band are in excellent agreement with calculations that predict high-spin superdeformed bands in $^{62}\text{Zn}$ with deformations $\beta_2 \approx 0.41 \pm 0.49$. These results establish a new region of superdeformation for nuclei with neutron and proton numbers $N, Z \approx 30 \sim 32$. [S0031-9007(97)03901-X]

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In recent years, the study of superdeformed (SD) bands has been one of the most exciting topics in nuclear structure research. Since the first observation of high-spin superdeformation in $^{152}\text{Dy}$ [1], SD bands have been identified in many nuclei in the $A \sim 190, \sim 150, \sim 130$, and $\sim 80$ mass regions [2]. Based on calculations of large SD shell gaps in the single-particle energy levels for particle numbers $N, Z = 30 \sim 32$ [3,4], SD bands have also been predicted in the $A \sim 60$ mass region [5]. Because of the limited number of particles in these nuclei and their proximity to the $N = Z$ line, superdeformation in this mass region is of particular interest. Studies of $A \sim 60$ SD bands will enable comparisons between mean-field cranking models of SD nuclei and large-scale shell model calculations [6], studies of the onset of isospin $T = 0$ neutron-proton pairing at high rotational frequency [7,8], and investigations of the loss of collectivity in these SD bands resulting from the limited spin content of their single-particle configurations [9]. However, because of a number of experimental difficulties, previous searches for these bands have been unsuccessful. In this Letter we report on the observation of a SD band in $^{62}\text{Zn}$, the first observation of $A \sim 60$ superdeformation.

High-spin states in $^{62}\text{Zn}$ were populated via the $^{40}\text{Ca}(^{28}\text{Si}, \alpha 2p)^{62}\text{Zn}$ reaction at a bombarding energy of 125 MeV. A thin ($500 \mu\text{g/cm}^2$) target enriched to 99.9% in $^{40}\text{Ca}$ was used, and the detection system consisted of the Gammasphere array [10] comprising 83 Compton-suppressed Ge detectors, 13 neutron detectors, and the Microball [11], a $4\pi$ charged-particle detector array consisting of 95 CsI(Tl) scintillators. The collimators were removed from the Ge detectors, allowing $\gamma$-ray multiplicity and sum-energy information to be measured for each event [12]. With an event trigger requiring coincidences between at least three Ge detectors or between at least two Ge detectors and a neutron detector, $2.7 \times 10^9$ events were recorded in five days of beam time. The $\alpha 2p$ evaporation channel leading to $^{62}\text{Zn}$ comprised $\sim 10\%$ of the total fusion cross section in this reaction and was selected by applying the total energy plane channel-selection method [13] to events in which an alpha particle and two protons were detected in the Microball. Events passing the selection criteria were unpacked into a symmetrized $E_\gamma - E_\gamma$ correlation matrix which contained $5.0 \times 10^8 \gamma-\gamma$ coincidences, 95% of which were associated with $^{62}\text{Zn}$.

In addition to the normally deformed (ND) bands in $^{62}\text{Zn}$ identified in an earlier experiment [14], a new band consisting of a cascade of six $\gamma$ rays was observed. Figure 1 shows the $\gamma$ spectrum obtained by summing coincidence gates set on all of the members of this band. The $\gamma$-ray energies, which have uncertainties of $\pm 2\text{ keV}$, are labeled in this figure. Also labeled are the energies of known transitions in $^{62}\text{Zn}$ which firmly establish the new band as belonging to this nucleus. The observed intensity of the band in the plateau region was $\sim 1\%$ of the channel intensity, as shown in the inset of Fig. 1(a). Although the band was weakly populated, single gates were sufficiently clean to confirm the mutual coincidence of all of the $\gamma$ rays except the 1993 keV transition. This transition was confirmed as a member of the band by summing double gates set on the band members in an $E_\gamma - E_\gamma - E_\gamma$ coincidence cube. The stretched $E2$ character of the $\gamma$ rays was confirmed by their angular distributions.
Particle kinetic energies

$T_p$ be accurately determined by measuring the sum of the

dition, the excitation energy at which the band is fed can

tra show that the band is populated by only the highest

states with $g$ and 1791 keV

vealed by its decay into known high-spin states. The 1161

linked into the decay scheme, its high-spin nature is re-

dence with the band (solid line) and low-spin states in

$^{62}$Zn, respectively.

Although a 3986 keV $\gamma$ ray was observed in coinci-

dence with the band and appears to be a decay-out trans-

it, the lack of statistics prevented a conclusive linking of

this band into the $^{62}$Zn decay scheme. The 3986 keV $\gamma$

carry only $\sim$8% of the intensity of the band and the

remainder of the decay-out intensity is highly frag-

mented, as is typical of the decay out of SD bands in

other mass regions (e.g., [15]). Although the band is not

linked into the decay scheme, its high-spin nature is re-

vealed by its decay into known high-spin states. The 1161

and 1791 keV $\gamma$ rays in Fig. 1(a), for example, arise from

states with $I^\pi$ = 14$^+$ and 13$^-$, respectively [14]. In ad-

dition, the excitation energy at which the band is fed can

be accurately determined by measuring the sum of the

particle kinetic energies $T_p$ in the center of mass frame

[16]. The inset in Fig. 1(b) shows $T_p$ spectra in coin-

cidence with the band (solid line) and low-spin states in

$^{62}$Zn (dashed line). The mean $T_p$ of 28.8 MeV for events

feeding the band is 6.2 MeV below the average for the

$\alpha 2p$ channel. The corresponding mean total $\gamma$-ray en-

ergy of 32.0 MeV for decays that pass through the band is

thus 6.2 MeV larger than the $^{62}$Zn average. These spec-

tra show that the band is populated by only the highest

excitation energy, and hence highest spin, components of

the $^{62}$Zn entry distribution. Based on the decay of the

band into known high-spin states, a decay-out energy of

at least 3986 keV, the excitation energy at which the band

is fed, its intensity profile, and calculations (see below)

which predict that the SD bands in $^{62}$Zn become yrast for

spins $I \geq 24\hbar$, we estimate that the observed band ex-

tends from $I = 18\hbar$ to $30\hbar$ with a $\pm 2\hbar$ uncertainty.

In Fig. 2 we plot the dynamical moment of inertia $J^{(2)}$

as a function of rotational frequency for the new band and

for typical SD bands from the other regions of superdefor-

mation. In order to remove the mass dependence, all of

the $J^{(2)}$ values have been divided by $A^{5/3}$ [17]. The scaled

$J^{(2)}$ values for the $^{62}$Zn band are comparable to those for

SD bands in other mass regions, and we note that the $^{62}$Zn

band extends to the highest rotational frequency observed

for a SD band.

Although the large moment of inertia of the new band,

its intensity profile, its feeding from the highest-spin

components of the entry distribution, and its fragmented

decay out into known high-spin states all support a SD

interpretation, a definitive conclusion on the deformation

of this band requires a measurement of its transition

quadrupole moment $Q_t$. Because of the high collectivity

and high transition energies of this band, the state

lifetimes (on the order of 1 fs) are much shorter than the

time taken by the recoiling nucleus to leave the target (on

the order of 100 fs). The entire band thus decays while

the nucleus is slowing down in the target and $Q_t$ can be

measured by the thin target Doppler shift attenuation

method [18]. The measured fraction $F$ of the full Doppler

shift is plotted versus $\gamma$-ray energy for a number of

transitions in Fig. 3. Most of the transitions from states

with $I \leq 14\hbar$ decay outside of the target with constant

shift $F = 0.872$, the ND bands in $^{62}$Zn decay on the same
time scale as the time to recoil out of the target, and all of

the transitions in the new band have very short lifetimes

and are almost fully shifted.

In order to extract the quadrupole moment of the new

band, the slowing down of the recoiling nuclei in the

target was modeled using the electronic stopping powers

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure1.png}
\caption{\label{fig:fig1} $\gamma$-ray spectrum generated by summing coincidence
gates set on all of the transitions in the new band (diamonds). (a) Energies label the band members and known transitions in

$^{62}$Zn; (b) expanded view of the band. The inset in (a) shows

the intensity of the band relative to the channel. The inset in

(b) shows spectra of the sum of the particle kinetic energies $T_p$

in the center of mass frame for the band (solid line) and the

$\alpha 2p$ channel (dashed line) obtained by triple gating on $\gamma$ rays from the band and from low-spin states in $^{62}$Zn, respectively.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure2.png}
\caption{\label{fig:fig2} Plot of the dynamical moment of inertia $J^{(2)}$ divided by $A^{5/3}$ versus rotational frequency for the new band in $^{62}$Zn and for SD bands from other mass regions. For reference, the dashed line represents the moment of inertia of a rigid rotor with quadrupole deformation $\beta_2 = 0.5$.}
\end{figure}
various outside of the thin target, respectively. Calculated for various \( \Qt \) the band. The fractional shifts calculated in this model same lifetime as the precursor in-band state \([22]\) and calculated as a function of time by integrating over the small target and averaging over 100 reaction locations within the thin target. The decay of the nucleus was modeled by assuming a constant in-band \( \Qt \) and side feeding into each state was modeled by a single transition with the same lifetime as the precursor in-band state \([22]\) and an intensity to match the observed intensity profile of the band. The fractional shifts calculated in this model for various \( \Qt \) values are shown by solid curves in Fig. 3. The new band is best fit by \( \Qt = 2.7^{+0.4}_{-0.3} \text{ e.b.} \).

We have carried out a theoretical analysis of high-spin states in \(^{62}\text{Zn}\) employing the configuration-dependent shell-correction approach with the cranked Nilsson potential \([23,24]\). Representative potential energy surfaces calculated for \( I^\pi = 20^+ \) and \( 24^+ \) are shown in Figs. 4(a) and 4(b), respectively, and the energies of favored high-spin collective configurations are plotted versus spin in Fig. 4(c). At moderate spins the yrast configurations are triaxial signature-degenerate ND bands \( (\beta_2 = 0.3, \gamma = 30^\circ) \) which approach the \( \gamma = 60^\circ \) noncollective axis at higher spins. These correspond to the smoothly terminating strongly coupled bands previously observed \([14]\) in \(^{62}\text{Zn}\). For higher spins \( (I \geq 24\hbar) \) the yrast configurations are calculated to be SD bands with deformations \( \varepsilon_2 = 0.36-0.43 \) \( (\beta_2 = 0.41-0.49), \gamma = 0^\circ-15^\circ \).

In all of the favored SD bands the neutron and proton orbitals up to the \( N,Z = 30 \) SD shell gap corresponding to the \( f_{7/2} \) hole \( g_{9/2} \) particle configuration \( [f_{7/2}]^{-2}[g_{9/2}]^2 \) are filled. Different SD bands are formed depending on the orbitals occupied by the last two neutrons. The observed band in \(^{62}\text{Zn}\) is assigned to one of the neutron SD configurations \( \nu[f_{7/2}]^{-2}[g_{9/2}]^2 \). The \( \Qt \) values calculated (as in \([9]\)) for these bands in the spin range of interest, namely, \( \Qt = 2.7-2.1 \text{ e.b.} \) for the \( \nu[f_{7/2}]^{-2}[g_{9/2}]^2 \) configuration and \( \Qt = 3.2-2.5 \text{ e.b.} \) for the \( \nu[f_{7/2}]^{-1}[g_{9/2}]^2 \) configurations agree well with the measured value of \( 2.7^{+0.3}_{-0.3} \text{ e.b.} \). The \( \nu[f_{7/2}]^{-1}[g_{9/2}]^2 \) SD configuration shown in Fig. 4(c) is not a likely candidate for the observed band. The \( \Qt \) of

![FIG. 3.](image1) Fractional Doppler shifts \( F \) for transitions from states with \( I \leq 14\hbar \) (diamonds), for a ND band in \(^{62}\text{Zn}\) (squares), and for the new band (circles). The dashed lines at \( F = 1.00 \) and 0.872 represent the full shift and the constant shift for decays outside of the thin target, respectively. Calculated \( F \) curves for various \( \Qt \) values are shown by solid lines. The new band is best fit by \( \Qt = 2.7^{+0.4}_{-0.3} \text{ e.b.} \).

![FIG. 4.](image2) Calculated high-spin properties of \(^{62}\text{Zn}\). Potential energy surfaces are shown for (a) \( I^\pi = 20^- \) and (b) \( I^\pi = 24^- \). Equipotential lines separated by 0.25 MeV are shown up to 5.5 MeV above the minima. (c) Energies of favored collective configurations relative to an \( I(I+1) \) reference plotted versus spin. The SD configurations are labeled by their neutron and proton \( f_{7/2} \) holes and \( g_{9/2} \) particles and by their equilibrium deformations at \( \hbar \approx 22\hbar \). Solid (dashed) lines represent positive (negative) parity, and closed (open) symbols denote signature \( \alpha = 0 \) (\( \alpha = +1 \)). Terminating ND states are encircled. For \( I > 30\hbar \) the yrast lines for different combinations of parity and signature are shown by lines of different type without symbols. The states corresponding to the “maximum spin” extracted from the low-spin SD configurations are indicated by large open squares. Note that these states are collective and that the SD bands can be extended to higher spins, as indicated by the dotted lines.
2.1–1.2 e\,\!b calculated for this band is outside of the experimental uncertainty on the measured value, and the absence of the signature-partner band that should be observed with a single signature-degenerate $f_{7/2}$ hole also argues strongly against this configuration. It is expected that future experiments in this mass region will establish links between SD bands and ND states. The definite configuration assignments resulting from such links will provide important information on the, as yet unknown, single-particle energies at large deformation in this mass region. We also note that the states corresponding to the “maximum spin” extracted from the low-spin SD configurations [large open squares in Fig. 4(c)] occur at spins only slightly higher than observed in this experiment. Although these states are collective and the SD bands do not terminate in the usual sense, their properties in the $I = 30\hbar–40\hbar$ range are strongly affected by the limited spin content of their single-particle configurations.

In summary, we have observed a cascade of six $\gamma$ rays in $^{62}\text{Zn}$ that forms a rotational band over an estimated spin range of $I = 18\hbar–30\hbar$. The scaled $I(2)$ moment of inertia is comparable to those of SD bands in other mass regions, and the measured quadrupole deformation of $\beta_2 = 0.45\pm 0.10$ is in excellent agreement with theoretical calculations which indicate that SD bands with $\beta_2 = 0.41\sim 0.49$ become yrast in $^{62}\text{Zn}$ for spins $I \geq 24\hbar$. These results establish a new region of superdeformation in nuclei with neutron and proton numbers $N, Z = 30–32$. A systematic study of SD bands in this mass region is clearly required to define the limits of this newest region of superdeformation and to extract detailed information about the single-particle energies at large deformation for these light nuclei.

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