Significance of critical degrees of saturation at freezing of porous and brittle materials

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SIGNIFICANCE OF CRITICAL DEGREES OF SATURATION AT FREEZING OF POROUS AND BRITTLE MATERIALS

CONTRIBUTION TO ACI-SYMPOSIUM DURABILITY OF CONCRETE, OTTAWA OCTOBER 1973

GÖRAN FAGERLUND

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PREFACE
This report is a contribution to the symposium "Durability of Concrete", which is sponsored by the American Concrete Institute and which will be held in Ottawa, Canada, in October 1973.

The report can be regarded as an extensive summary of my work within the field of frost-resistance of materials.

Lund, February 1st 1973

Göran Fagerlund
SYNOPSIS

The paper treats the problem "Frost-Resistance" as a general problem for all porous materials. The basis is the undeniable fact that well-defined critical degrees of saturation exist for all porous materials.

1st part—The difference between the new way of defining critical degree of saturation (as a materials constant) and the usual way (as functions of a combination of properties of material and environment) is discussed. Method of determination is shown and discussed.

2nd part—Possible definitions of moisture conditions are provided.

3rd part—By comparison of the critical degree of saturation and the actual reached in practise, the frost resistance can be expressed by a plain figure which makes a rational choice of material possible. The method is exemplified. A method of determination of the actual water content is shown. Hypothesis are put forward as regards frost-resistance of layered structures or particle composites and frost-resistance at use of thawing salts.

4th part—On basis of the hydraulic pressure theory connections between materials properties and critical degree of saturation are derived. Measurements of amount of ice formed, rate of ice formation and length-changes together with estimations on temperature-permeability relations show the reasonableness of the hydraulic pressure theory. Connections between pore properties and actual degree of saturation are discussed.
THE EXISTENCE OF CRITICAL DEGREES OF SATURATION AT FREEZING

General Discussion

The concept "critical degree of saturation" has got a rather bad reputation even by seriously working scientists. So for instance Powers writes (1):

"Whatever success such theories (about the existence of critical degrees of saturation, the authors remark) have had when applied to clay products, rock or concrete, may be ascribed to constancy of the effect of variable factors not explicitly represented in the analysis. For example, if among a certain group of materials a satisfactory correlation between degree of saturation and damage produced by freezing has been observed, factors other than degree of saturation have been constant or have had a simple, more or less fortuitous relationship to degree of saturation."

In another place Powers writes about concrete aggregates (2):

"Thus we see, that if the water is not uniformly distributed within an aggregate particle at the time of freezing, the critical saturation point for that particle based on its overall capacity might be considerably less than 91.7% (the theoretically lowest degree of saturation). It is therefore impossible to establish any single value for the critical saturation point that would be a reliable basis for predicting the effect of freezing of aggregate particles either alone or in concrete: obviously this must be true for concrete as a whole."

By his first statement Powers evidently means that a critical degree of saturation as a characteristic of a whole family of materials could reasonably not exist. Such materials properties as porosity, pore-size distribution, strength, permeability etc must have a decisive importance for the amount of water which can be contained within a material despite risk of frost damage. Thus a general critical degree of saturation could not exist.

By his second statement Powers shows the meaninglessness in trying to define a critical degree of saturation since the water content in a specimen or a part of structure often varies across its section. He evidently looks upon the degree of saturation as a mean value throughout the whole materials volume.
Powers' categoric statements, which are representative for many scientists might easily discourage from each further research work on critical degrees of saturation. However used in a more refined way the concept critical degree of saturation can be extremely useful at evaluation of the connections between materials structure and frost resistance. This will be shown further on in this paper.

Of course Powers has right in his cited statements but only from the starting-point of his own assumptions. If the concept critical "degree of saturation" should have any meaning at all it must be defined in a special way, viz. The critical degree of saturation is a materials constant that adopts individual values for each particular material. Each single value is valid for a special combination of materials properties. So for instance the critical degree of saturation for a material like concrete may vary from for instance 0.50 to 0.92 dependent on mix proportions, quality of constituents of the concrete, way of manufacturing, degree of hydration, etc. Frost damage does not occur even at a large number of frost cycles if the actual degree of saturation in a structure does not in any point of the structure exceed the critical degree of saturation in the same point.

Thus, a proper use of the principle of critical degrees of saturation demands, partly that the distribution of moisture in the structure is known, partly that the critical degree of saturation or the combination of materials properties, that determines the value of the critical degree of saturation, is known in all parts of the structure.

Such a condition that the materials properties within the same materials unit may vary throughout the unit, for instance with a layered construction, does therefore not reduce the servicableness of the critical degree of saturation as a criterion on frost resistance, as long as the critical and actual degrees of saturations are known throughout the unit.

Then, why has the critical degree of saturation got such a disrepute? Without doubt this depends on very unlogical ways of treating the concept.

- Attempts have been made to find universal critical degrees of saturation that would be valid for a whole group of materials or even for all porous materials. (3), (4, 5) and others. Such attempts are absurd and can easily be rejected by experiments. (6), (7).

- The critical degrees of saturation are, as far as we know, always based upon the state of moistening before the first freezing. So for instance the concept "coefficient of absorption" (S according to the definition in eq (1)) is often used as a concept synonymous to the critical degree of saturation.

\[ S_a = \frac{V_a}{P} \]  \hspace{1cm} (1)

All the specimens are consequently stored in water for a long time before the freezing test starts. Hence they all have the same state of
moistening, correspondent to $S$, before the first freezing. The freezing cycles do normally involve some period where the specimens are placed in water, for instance at thawings. Hence the degree of saturation changes all the time. Normally it increases with increasing number of cycles. Damage occurs when the increased degree of saturation exceeds the critical value. Therefore the choice of number of cycles is extremely important for the judgement of frost resistance, that is, for the judgement of critical coefficient of absorption.

On the basis of such freezing experiments some authors have tried to find correlations between the coefficient of absorption and the observed behaviour at freezing, (3), (4). Of course this is doomed to failure. There is from a logical point of view no correlation between the coefficient of absorption and the critical degree of saturation. The former is only a measure of the hydraulic properties of the material while the latter is a complicated function of strength, ductility and pore properties of material.

However, once the incompatibility of the coefficient of absorption and the critical degree of saturation is understood, things become more clear. The critical degree of saturation must be determined on specimens where the water content is constant throughout the whole test. Suitably a series of specimen are adapted to different degrees of saturation before the first freezing. This can be done by drying from a wetter condition or by wetting from a dryer condition. The specimens are sealed from water loss.

Each specimen is then frozen and thawed a couple of cycles in air with a reasonable rate of temperature lowering. The dynamic Young’s modulus or length or thickness is measured before and after the freezings. The critical degree of saturation can normally be indicated as a very evident knick-point in a diagram residual Youngs modulus or dimension versus degree of saturation.

The scattering around the critical value is normally small if the tested specimens have fairly similar properties, the greater the scattering in properties, the greater the uncertainty at definition of the critical value.

The number of cycles used is without greater importance in this experiment. Since there is no water exchange with the environment, damage does not occur even at many cycles, if the specimen has a lower water content than the critical. This has been experimentally confirmed up to 165 cycles.

However different materials are more or less ductile which means that a certain transgression of the knick-point value of degree of saturation is more or less disastrous.

In figure 1 is shown the determination of critical degrees of saturation of two almost identical concretes, one is a normal non-airentrained concrete, the other is reinforced with short pieces of steel fibre ($\phi$ 0.3 mm, length 25 mm). Each dot represents one specimen with size $40 \times 40 \times 160$ mm$^3$. 14 different specimens are used. $S$ is defined according to eq (3).
The critical values, as defined at the knick-point, are the same for both materials which is expected, (eq. (25)), but the reinforced specimen gets less damage if $S_{CR}$ is exceeded because of its greater ductility. Hence in reality the reinforced material can stand more water than the non-reinforced. It can therefore be suitable to supplement the $S_{CR}$ value defined as the knick-point value with information of the slope of the line of $S > S_{CR}$.

The values in fig 1 are obtained after 10 - 13 cycles. In fig 2 is shown principles of the evolution of the dynamic Young's modulus with increasing number of cycles when the water content is constant. The short time fracture character of frost damage (not fatigue character) is clear from the figure, as well as the relative ease of defining the value of $S_{CR}$. Often a relatively great decrease in modulus occurs at the first freezing (curves (b) and (c) ) even when $S$ is low. This is inevitable. However if no further damage occurs at the following freezings the water content in the specimen is lower than the critical. Curves(d), (e) and (f) are typical for specimen where $S > S_{CR}$.

The results in fig 1 are no exception. By the same freezing technique a large amount of different building materials, at the present more than 40 different qualities and types, have been tested as regards their critical degrees of saturation. The results are based upon more than 1000 specimens. See (8).

In no cases there has been any difficulties at indicating critical values. Therefore, the existence of critical degrees of saturation has been proved beyond each doubt. Their values defined according to eq (3) cover a range of 0,22, determined for a no fines light aggregate concrete, to 0,91 for a clay roofing tile. If consideration is taken to the fact that only a part of the water is freezeable the range is further broadened.

Practical aspects of determinations of critical degrees of saturation

Since the critical degree of saturation is regarded as a materials constant the specimens used are as small as possible in order to assure simultaneous freezing in the whole specimen and an even moisture distribution. However the specimens must be big enough to be representative cells of the material. Besides they must be bigger than the critical size. For a concrete the condition of representative cells gives relatively big specimens. With an aggregate size of 30 mm the diameter of a cylindrical specimen must be at least 100 mm. The need of a big specimen may however bring a conflict with the need of simultaneous freezing. When the temperature of the ambient air is lowered a temperature gradient arise in the specimen. As long as the rate of temperature lowering is moderate the temperature gradient in the specimen is limited. Since the specimen is frozen in air normally a substantial supercooling occurs. Hence all parts of the specimen may reach a temperature equal to or lower than the ordinary freezing temperature of the pore water, before ice formation is initiated somewhere in the supercooled water. Within a few seconds from initiation of freezing the ice front has penetrated all pores with water potentially freezeable at the prevailing temperature. Freezing is then seeded and
going on simultaneously in the whole specimen even when this is relatively big. Besides most of the water is formed around 0°C without any temperature lowering worth mentioning if the degree of saturation is fairly high. Therefore, the surface part and the inner parts of the specimen never get any great temperature difference even at big specimens. The principles are shown in fig 3 which shows halves of specimens of two different sizes. The specimen to the right is freezing almost simultaneously while the specimen to the left is freezing with a moving ice front.

It can of course be questioned whether the critical degree of saturation should not be determined on specimens freezing from one side, that is with a moving ice-front. However, as we see it, this way of freezing brings greater difficulties at determination of the exact value of $S_{CR}$. Besides the problem of moving icefront as well as the problem of moisture gradient at freezing can probably be treated theoretically once $S_{CR}$ is known for a small volume of the material freezing simultaneously and with no moisture gradient. Eqs (15)(16).

Normally there is no important moisture gradient through the specimen when freezing starts. This has been confirmed on specimens 30 x 30 x 120 mm$^3$ of different materials. Those specimens adapted by drying to different degrees of saturation have been placed in the freezing box and a normal freezing cycle has started. Immediately before 0°C-temperature the specimens were taken out and chopped in pieces. The pieces were dried at +105°C. A result is shown in fig 4. The risk of moisture gradients is less the higher the moisture content. Besides the risk ought to be less if the specimens are adapted to proper water content by wetting than by drying, viz at drying the surface of the specimen might reach moisture contents lower than the average aimed at. Then because of hysteresis wetting - drying the outer parts of the specimen might not reach the same high degree of saturation as the inner part even at equilibrium in pore water pressure through the whole specimen. Therefore the average water content does not give the proper answer of the wettest part of the specimen. The principles of this is shown in fig 5.

A suitable way of reaching a certain degree of saturation in a specimen is to use relatively dry specimens (drier than $S_{CR}$), put each specimen separately in a vacuum chamber, evacuate the pore-air to a certain remaining pressure for a few minutes and then let the water into the chamber. Fig 6. In this way, by choosing suitable pressures, a spectrum of specimens of different degrees of saturation is obtained. Since all parts of the specimen has reached its degree of saturation by wetting no problems of hysteresis exist.

It is however not quite sure that $S_{CR}$ will get the same value for specimens dried as for specimens wettened to their water contents at freezing. Fig 5 shows two hypothetical moisture equilibrium curves. The drying curve do always correspond to a higher suction value (pF-degree). Hence, at a certain moisture ratio the water is located in smaller pores if the moisture ratio has been attained by drying than if it is attained by wetting. It will later on be shown that this means that the critical degree of saturation is minimum when it has been attained by drying from
a complete wet condition.

Normally, the pore water pressure of a specimen is not determined by the extreme wetting- or drying curves but by a scanning curve between the two extreme-curves. Fig 5.

However, by experiments it seems as if $S_{CR}$ is not influenced to any great extent by the way of adapting specimens to proper water contents. Besides, the effect ought to be greatest at the first freezing. After a couple of freezings moisture is probably redistributed in the specimen in about the same way despite method of adaptation.

In our test method the specimens are mounted on rotating wheels in order to facilitate the mounting of specimens in the freezing chamber, to avoid inevitable temperature gradients in the ambient air and above all to avoid moisture redistribution in coarse-pored materials because of gravitational forces. The wheels rotate 1 rpm. The rotational direction is changed for each full revolution in order to make temperature measurements possible.

The freezing apparatus consists of an ordinary freezing box. It has been provided with two fans on the lid, with a temperature sensor, with a controle cell of copper containing 25 grams of pure water and a thermocouple and with two heating elements.

The system of regulating the temperature will not be described in detail. It will be published elsewhere (8). However described in brief: The temperature in the box is measured by the sensor. The information goes to a tyristorized temperature regulator. The actual temperature is compared with the temperature aimed at. This in turn is provided to the regulator from a potentiometer mechanically regulated by a revolving disc on which periphery the freezing cycle is cut. The freezing box is working with full capacity for which reason any divergence from the proper cycle is adjusted by the regulator supplying more or less effect to the heating elements in the box.

The disc rotates one round per 6 hours. 5 hours corresponds to the freezing part and 1 hour to the thawing part of the cycle. However by a microswitch the disc is stopped at the lowest temperature, $-18^\circ C$, for 1,5 $\times$ 3 hours and at $+5^\circ C$, for 3 multiples of 1,5 $\times$ 3 hours. The first stop brings the specimen down to $-18^\circ C$ and the last makes a complete thawing possible.

The controle cell is used as a guard of the function of the temperature regulator. viz, when corrections are made for the rapid freezing caused by supercooling of the water in the cell, it should always take the same amount of time to freeze the water. The freezing apparatus is shown in fig 6 and the cycle in fig 7.

It must be noticed that only the air-temperature is carefully controled. Hence the rate of temperature lowering of each specimen can be quite different dependent on its heat capacity, its total amount of water and its amount of freezable water at different temperatures. Beside its surface/volume ratio may influence the rate of temperature lowering,
since a high such ratio causes a high rate of heat loss and consequently a high rate of freezing, cf eq(39). Hence, in order to get fair comparisons between different materials, the specimen size and form ought to be the same for all materials, or the cycle ought to be somewhat changed when the specimen size is changed. The difference in surface/volume-ratio is sometimes rather big for imaginable specimens; 0.5 for a cylinder $\phi$ 100 x 200 $\text{mm}^3$ and 1.1 for a prism $h$ 40 x 40 x 160 $\text{mm}^3$.

The rate of temperature lowering is in average $\frac{46}{U_j}^\circ\text{C/h}$, faster at the start and the end of the freezing cycle and slower at the middle.

However as shall be discussed later it is not so much the rate of temperature lowering that is interesting as the absolute temperature difference between the surface of the specimen and the ambient air. This difference determines the rate of heat loss from the specimen. Eq(38)

If the degree of saturation is defined according to the physically correct eq (2) there is a need of knowledge of non freezeable water contents in the specimen at the lowest temperature used. At our institution non freezeable water contents have been determined for $10^4$ different materials and qualities of materials. The apparatus used is a "relatively adiabatic" calorimeter built at the institution. The experiments are performed by thawing of specimens with different degrees of saturation frozen to $-25^\circ\text{C}$, $-12^\circ\text{C}$ and $-6^\circ\text{C}$.

In order to define proper values of $S$, it is essential to know the total open-pore-volume as accurate as possible. This has therefore been determined by vacuum treatment of dried specimens ($+105^\circ\text{C}$ or $+50^\circ\text{C}$ dependent on the material). The minimum pressure is about 2 mm Hg kept for some hour after which water is let into the specimens. The specimens are then stored for many days in the water before determinations of pore-volume, volume and density.

**DEFINITIONS OF CRITICAL MOISTURE CONDITIONS**

The physically correct definition is:

$$S = \frac{w_f}{w_f + 1}$$  (2)

Sometimes it is more convenient to use the following definition:

$$S_e = \frac{w}{P}$$  (3)

Definition (2) as well as (3) need the pore volume to be known. For some materials like cellular concretes or no fines concretes with porous aggregate, the exact determination of open porosity is difficult. In this case the moisture ratio can be used.

$$u = \frac{Q_{\text{w:e}}}{Q_{\text{dry}}}$$  (4)

The three definitions are coupled together so that the existence of for instance a critical degree of saturation according to eq (2) is accompanied by the existence of a critical degree of saturation according to eq (3) and a critical moisture ratio according to eq (4).
The difference between definitions (2) and (3) is greater the greater
the non freezeable water contents. So for instance $S_{\text{eq}}(2) = S_{\text{eq}}(3)$
for a material like well burnt clay brick. For a material like a dense
cement paste the difference is considerable.

**USE OF CRITICAL DEGREES OF SATURATION AT EVALUATION OF FROST RESISTANCE**

**General Discussion**

The fact that critical moisture conditions evidently exist, make
a rational judgement on the frost resistance of different materials
possible.

The pre-requisite condition for this is however, that the moisture
conditions reached in practise are known.

Then the frost resistance is defined:

\[
\text{FROST RESISTANCE} = s = S_{\text{CR}} - S_{\text{ACT}}
\]

By using this definition all materials are treated in the same way
despite their densities, porosities and non freezeable water contents
are quite different.

Often the non freezeable water contents expressed as fraction of
total pore volume are about the same for many materials. In this case
the frost resistance can be expressed:

\[
s_{e} = S_{e_{\text{CR}}} - S_{e_{\text{ACT}}}
\]

which equation expressed in moisture ratios is:

\[
s_{u} = s_{e} = \frac{u_{\text{CR}} - u_{\text{ACT}}}{u_{o}}
\]

A comparison between the frost resistance of two materials A and
B can be done in the following way.

\[
\frac{s_{A}}{s_{B}} = \frac{(S_{\text{CR}})_{A} - (S_{\text{ACT}})_{A}}{(S_{\text{CR}})_{B} - (S_{\text{ACT}})_{B}}
\]

When the definition of moisture condition according to eq (3) is
used the comparison of frost resistance gets the form:

\[
\frac{s_{A}}{s_{B}} = \frac{\left[ (S_{e\text{CR}})_{A} - (S_{e\text{ACT}})_{A} \right] \left[ 1 - K_{B} \right]}{\left[ (S_{e\text{CR}})_{B} - (S_{e\text{ACT}})_{B} \right] \left[ 1 - K_{A} \right]}
\]

where $K$ is defined:

\[
K = \frac{w_{nf}}{p}
\]

A test method is consequently divided in two parts of quite.

rent character.

- **part 1**: Determination of critical degrees of saturation according to the principles discussed above. The same type of method is used for each material.

- **part 2**: Determination of actual degrees of saturation. The method should from a theoretical point of view be designed according to the actual way of using the material.

The problem of determination of frost resistance is now divided in two parts.

- **part 1** principally dependent only on materials properties.

- **part 2** for each material principally dependent only on properties of the environment.

One of the main difficulties of the problem of frost resistance has been its utmost complexity. This in turn is above all dependent on the problem being a coalescence between the materials own properties and properties of the environment in which the material is used.

In ordinary used freezing tests the same coalescence is maintained. So for instance consideration is taken to different ways of using a certain material by varying the "wetness" of the test or the number of cycles.

By the new way of defining the concept frost resistance, materials properties and properties of the environment are separated from each other which leads to the following advantages:

- Theoretically, the test method takes consideration to different ways of using the same material.

- The determination of $S_{cr}$ is rapid since only a few cycles are needed. See above. The determination of proper $S_{ACF}$ is more difficult but normally simple water uptake tests are sufficient.

- The frost resistance is quantified for which reason materials can be ranked according to their durability.

- The method gives great potential possibilities of making connections between materials structure and frost-resistance clear. See below. Besides, for instance the frost resistance of materials combinations and composite materials could be better understood.

A comparison by Arni & al (9) of the four methods according to ASTM of testing frost resistance of concrete is a good example of the confusions arising, when properties of materials and properties of the environment are mixed together.

In fig 9 is shown the authors results. Each pile within one test
method corresponds to one type of concrete. Evidently, the judgement of the frost resistance is completely dependent on which method was chosen.

However the result can be logically interpreted by use of the concept critical degree of saturation. For each concrete type \( S_{CR} \) is the same in all four methods (possibly there is some variation because of differences in rate of freezing, see above), but \( S_{ACT} \) varies. Evidently \( S_{ACT} \leq S_{CR} \) in the methods "rapid air" and "slow air" whereas \( S_{ACT} > S_{CR} \) in the methods "rapid water" and "slow water". An idea of the values of \( S_{ACT} \) in the four methods can be obtained by analysing the data in the original report. In Table 1 are listed approximative values of total time in unfrozen water, \( t_w \), and in air, \( t_a \), per cycle. Since the more essential drying occurs when the pore-water is unfrozen, the time in air at temperatures down to \(-5^\circ C\) is listed in the table, \( t_{aw} \). \(-5^\circ C\) is chosen because supercooling of the pore water down to that temperature normally occurs.

The table shows that the specimens ought to have the highest degree of saturation at method "slow air" since each cycle involves 29 hours in water and the freezing are at maximum continued for 300 cycles. The specimens ought to be driest at method "slow air" since each cycle involves 1,5 hours drying in air just before freezing.

A comparison between table 1 and fig 9 shows the direct correlation between degree of saturation at test and damage at freezing. The result is therefore an excellent confirmation of the fact that the degree of saturation is the variable in freezing tests with dominating significance. So for instance rate of freezing seems to be quite inferior, cf table 1, which increases the possibility of a practical use of the concept critical degree of saturation.

Practical Aspects

The definition of frost resistance according to eq (5) is of course only valid for materials with \( S_{CR} < 1,0 \) that is for normal building materials. A material with only a few percent pores filled with freezable water has \( S_{CR} = 1,0 \) since the expansion at ice formation is to small to give any damage. If at the same time \( S_{ACT} = 1,0 \) the frost resistance according to eq (5) is zero despite the material is extremely frost resistant. Another such case is a material where the pores are so narrow that the water cannot freeze at ordinary temperatures. Even in this case \( S_{CR} = 1,0, S_{ACT} = 1,0 \) also since the pores are filled already by capillary condensation. As a consequence the frost-resistance is zero, according to eq (5). However in those two rare cases \( S_{CR} \) can be regarded as greater than 1,0 despite this is impossible from a theoretical point of view. Hence the frost resistance \( s > 0 \) but its absolute value is unknown and consequently the frost resistance cannot be compared to that of other materials.

The safety term, \( s \), is used instead of an ordinary safety factor in order not to underestimate the frost resistance of materials with high
critical values.

Any systematic smaller error at determination of the exact pore volume, for instance use of unsufficient vacuum before saturation, is almost eliminated at use of eqs (5), (6) or (7). As mentioned earlier the exact determination of actual degrees of saturation may be difficult since this demands an exact knowledge of all data on climatic conditions. After that, the actual environment can eventually be reproduced and the moisture condition reached eventually be measured or calculated with the aid of advanced moisture mechanics.

However, the problem of determination of $S_{ACT}$ can be substantially reduced by use of simple water uptake tests, viz. a minimum condition of frost resistance of a material used in a normal way is, that the degree of saturation reached on a dangerous depth (see below) at a short time suction from a free water surface is less than the critical.

This short time moisture condition can easily be discerned as the knick-point value in a diagram degree of saturation at a water uptake test according to fig 10 (or moisture ratio) versus root of time or log time. The knickpoint corresponds to the sudden decrease in rate of water uptake, when the water front has penetrated the total top surface of the specimen. The knickpoint may be somewhat dependent on the thickness of the specimen. The knickpoint is easier to discern the thinner the specimen. Examples of the determination of knick-point values of certain concretes is shown in fig 11. Examples of the effect of specimen thickness on the knick-point value is shown in fig 12.

The specimen normally continues to absorb water after the occurrence of the knick-point, but with a considerably reduced rate. Hence, at a refined judgement of frost resistance not only the knick-point absorption but the rate of this later secondary stage absorption must be considered.

However, simple water uptake tests can be used as a criterion on the value of $S_{ACT}$ after which eqs (8) or (9) can be used for a comparison of frost resistance of different materials. The pre-requisite condition for this is however that the following factors are considered.

- $S_{CR}$ can normally be defined as the knick-point value in a diagram residual Youngs modulus versus degree of saturation.

- The knick-point value of $S_{CR}$ must be supplemented with information of the effect of a transgression of $S_{CR}$, that is, of the slope of the curve for $S > S_{CR}$, of fig 1.

- $S_{ACT_{min}}$ can be defined as the knick-point value in a diagram degree of saturation versus time at a capillary water uptake.

- The knick-point value must be supplemented with information of the "long time absorption", and of the rate of drying after a finished absorption.
Examples of a Determination of Frost Resistance

In table 2 are shown typical results of a determination of frost resistance based upon the new principles. The materials are all no fines concretes with porous aggregate of Leca. The frost resistance is defined according to eq (7).

The degrees of saturation is calculated as if all pores were open, which of course gives somewhat too low values. The critical moisture ratio is very well defined for all 4 materials. Fig 13 shows the result for one of the materials.

The mean frost resistance of the four materials related to the resistance of type 1 at knick-point absorption is shown graphically in fig 14. Evidently the durability is reduced for all materials with increasing time of water storage. The materials 3 and 4 both get a negative safety term at 10 days storage while material 1 is very durable even after a very long time of water absorption.

All four materials show good durability in practise which they ought to do according to the test result. However, on basis of the test a use of materials 3 and 4 is not recommended in a situation where they have free access to water and where freezing might occur. In such places material 1 is superior.

Use of Critical Degrees of Saturation at Multi-layer Structures and Multi-phase Materials - Hypothesis

Fig 15 shows an example of multiphase materials. Material A shall be combined with material B. Their critical degrees of saturation are $S_{CR}^A$ and $S_{CR}^B$. At water uptake for a long time they reach different actual degrees of saturation, $S_{ACT}^A$ and $S_{ACT}^B$. The condition $S_{CR}^A > S_{ACT}^A$ is valid for both materials for which reason they both have a good frost resistance when used single. Fig 15a.

The two materials shall now be combined as in fig 15b, that is, as a layered structure or as in fig 15c, that is, with material B as particle phase in a matrix of material A. Fig 15b represents for instance a rendered wall (or why not the upper part of a concrete slab with different properties of the surface layer and the normal concrete (10)). Fig 15c represents for instance a concrete with porous aggregate.

In fig 15b $S_{ACT}$ will now get exactly the same value as when the two materials were single. Hence there will be a jump in $S_{ACT}$ at the interphase. In fig 15c $S_{ACT}$ can be at maximum just as high as in the case single material. Normally material B is surrounded by a more dense material, for instance cement paste. Then according to eq (59) the particles could not be filled as when they are single since water in the paste pores seal the particles.

Probably $S_{CR}$ will vary at the interphase. Water from the more dense material will be forced into the more porous and with greater ease than within the dense material itself. Hence $S_{CR}$ will be raised.
locally. In material B the degree of saturation is therefore raised at
the interphase. Besides water can only be forced into the interior of
material B at freezing. As a consequence $S_{CR}$ ought to decrease at
the interphase. If this happens the dangerous condition $S_{CR} < S_{ACT}$
might occur at the interphase despite the two materials are frost resistant
at the same moisture condition when they are isolated from each other.

The important case with a transitional zone between the two
materials is discussed in (14).

Use of Critical Degrees of Saturation at Freezing in Presence of
Deicing Agents - Hypothesis

It is a well-known fact that frost damage is increased in presence
of deicing agents such as Ca Cl$_2$, Na Cl.

This is possibly an effect of a decrease in $S_{CR}$ and of an increase
in $S_{ACT}$.

The decrease in $S_{CR}$ should be an effect of additional forces
because of osmotic pressure (12). However at high salt concentrations
the effective degree of saturation according to eq (2) at a constant
water content is decreased since the freezable water content is de­
creased. Therefore a pessimum salt concentration can be expected. This is
also confirmed by experiments in which a concentration of 3 to 5 % is
normally found to be most dangerous.

An eventual increase in $S_{ACT}$ because of thawing/surface gets wet
for very long periods. The prolonged drying depends on the lowering of
the vapor pressure of the water and is confirmed by experiments, (13).
Another eventual "$S_{ACT}$-raising effect" is redistribution of water
within the material. Regard a concrete slab with the same moisture
content across its thickness. A salt solution is poured on the top
surface of the slab. Then because of concentration gradients a redistri­
bution of water might occur and the surface layer gets wetter than in
the original state.

Thus the hypothesis is, that in presence of deicing salts the gap
between $S_{CR}$ and $S_{ACT}$ gets smaller than at "ordinary" freezing. Conse­
quently the frost resistance is diminished.

USE OF CRITICAL DEGREES OF SATURATION AT EVALUATION OF CONNECTIONS
BETWEEN MATERIALS STRUCTURE AND FROST RESISTANCE

In General

Informations on connections between materials structure and frost
resistance can be gained by analysing the effect of materials proper­
ties on the values of $S_{CR}$ and $S_{ACT}$. Such an analysis has been carried
through more comprehensively in (15).

Influence of Materials Properties on the Critical degree of saturation

At first there is a need of a model for frost damage.
A successful model used in our work is provided by Powers' hydraulic pressure theory (16).

This theory predicts the existence of critical distances at freezing. Such a critical distance is the critical thickness which is the thickest completely water saturated slice of a material that is not damaged by freezing.

The critical thickness can be expressed (15):

\[ D_{CR} = \sqrt{\frac{8 \cdot \sigma_B \cdot B}{0.09 \cdot v_r \cdot \frac{df}{dt}}} \]  \hspace{1cm} (11)

If the water saturated material is situated within a specimen that is not saturated eq (11) can be expressed (15):

\[ D_{CR} = \sqrt{\frac{8 \cdot \sigma_B \cdot B(1 - P(1 - S_e))}{0.09 \cdot v_r \cdot \frac{df}{dt}}} \]  \hspace{1cm} (12)

At the derivation, there is assumed that the permeability, \( B \), is constant. This is however a wrong assumption. For materials with a minor part of non freezable water the permeability at lower temperatures is extremely reduced because of ice filling up and blocking the pores. cf eq (12).

Another critical distance is the critical wall thickness of a spherical saturated material surrounding an air filled pore. This thickness is normally the same as Powers' spacing factor, \( L \). (16). The connection between the two critical distances is (17):

\[ D_{CR} = \frac{2}{3} \left( \frac{L_{CR} \cdot a}{3} + \frac{3 \cdot L_{CR}^2}{2} \right) \]  \hspace{1cm} (13)

The critical radius of a spherical freezing material, \( R_{CR} \) is related to \( D_{CR} \) through eq (14):

\[ R_{CR} = \frac{D_{CR}}{2} \]  \hspace{1cm} (14)

This later model can be used for the critical size of a saturated piece of aggregate.

Warris (17) treats the important case where an ice front is propagating into the interior of a material. The excess water created at ice formation is supposed to be forced only into the interior of the specimen. As a consequence a hydraulic pressure is created.
The maximum depth of water transport \((X_u - X)\), can be obtained from a heat balance equation in which is neglected the heat loss at lowering the temperature (damage is supposed to occur at the major ice formation in the neighbourhood of 0°C). Then according to (15) the connection between \(D_{CR}\) and the critical "depth of unsaturation" is:

\[
(X_u - X)_{CR} = \frac{D_{CR}}{8} \cdot \frac{1}{dx} \left[ \frac{1 - P(1 - S_e)}{(1 - P(1 - S_e))} \right] F(x - S_e)
\]  

(15)

\(dx\) is the thickness within which ice is forming simultaneously. The value of \(dx\) is dependent on the degree of supercooling and on the rate of temperature lowering. However, since the derivation of \(D_{CR}\) assumed simultaneous freezing in the whole slice, \(dx\) ought to be greater than \(D_{CR}\). When there is no moisture gradient eq (15) is changed to eq (16).

\[
(X_u - X)_{CR} = \frac{D_{CR}^2}{8} \cdot \frac{1}{dx} = \frac{D_{CR}}{8} \text{ when } dx = D_{CR}
\]  

(16)

Warris (17) gives eq (16) in somewhat different form. \(\frac{1}{dx}\) is replaced by the surface-volume ratio of the specimen.

Eqs (15) and (16) are oversimplified, especially since they assume that all excess water is forced only into the specimen and above all since \(D_{CR}\) in reality is determined by a permeability reduced by ice formation, while in eqs (15) and (16) the permeability is constant and equal to the permeability of the unfrozen material. Both those factors make \((X_u - X)_{CR}\) calculated from eq (16) too small.

The occurrence of critical distances is not only predicted by the hydraulic pressure theory but also by Powers' theory of microscopic ice lens segregation. (1,12).

The existence of critical thicknesses has been confirmed by experiments at our institution. Specimen were cut with area 30 x 30 mm² and variable thicknesses. They were vacuum saturated, weighed, wrapped in plastic foil or put in small beakers with water and then frozen a couple of times to about -18°C. After the final thawing they were vacuum saturated again and weighed. The eventual increase in weight is a measure of volume change caused by freezing. Normally visual inspection was satisfactory. 4 types of cellular concrete, 1 type of sand lime brick and two types of clay bricks were tested.

All specimens of sand lime brick and cellular concretes were completely destructed, which means that the critical thickness is less than 1,7 mm. This is confirmed by freezing experiments on bigger specimens, where the surface damage at \(S > S_{CR}\) is a scaling of very thin flakes or even crumbling. The crack system of the cellular concrete was mainly parallel to the surface. The distance between the cracks was about 0,5 mm.

The clay bricks had very evident critical thicknesses of about...
On specimens thinner than $D_{CR}$ no damage could be observed. An ice-crust covered the specimens when they were frozen in air which confirms that ice is actually forced out of the specimen at freezing. This water was regained by the specimen at thawing.

Since critical distances at freezing evidently exist the existence of critical degrees of saturation is a necessary consequence.

The problem of finding a theoretical expression of $S_{CR}$ is reduced to the problem of finding a geometrical connection between the distance and the degree of saturation.

A general equation for $S_{CR}$ is (15).

$$S_{CR} = 1 - \frac{1_{CR}}{P(1 - K)}$$

(17)

Where the critical air content $1_{CR}$ is coupled to the distance between air filled pores. Such expressions are given by Powers (16), Warris (17) and Larson et al (18). All those expressions suppose that the air filled pores are spherical.

Warris (17) base his expression on the critical thickness, $D_{CR}$. His expression is chosen since the pores may have an arbitrary pore size distribution.

$$1_{CR} = \frac{1}{1 + \alpha \cdot \frac{D_{CR}}{2}}$$

(18)

Powers' (16) expression for $1_{CR}$ is similar for $1_{CR} > 0.188$.

$$1_{CR} = \frac{1}{1 + \alpha \cdot \frac{L_{CR}}{2}}$$

(19)

Insertion of eq (18) or (19) in (17) gives:

$$S_{CR} = 1 - \frac{D_{CR}}{(1 + \alpha \cdot \frac{D_{CR}}{2})P(1 - K)}$$

or

$$S_{CR} = 1 - \frac{1}{(1 + \alpha \cdot \frac{L_{CR}}{2})P(1 - K)}$$

(20)

Insertion of eq (12) in (20) make it possible to express $S_{CR}$ in materials properties:

$$S_{CR} = 1 - \frac{1}{\left(1 + \alpha \sqrt{\frac{2 \cdot \sigma_B \cdot B(1 - P(1 - S_e))}{0.09 \cdot \omega \cdot dB/dt}}\right) P(1 - K)}$$

(21)
$S_{CR}$ can however not be calculated from eq (20) as far as the specific surface, $a$, of the air filled pores is not known.

By knowledge of the pores which can be air filled, it is possible to calculate the variation of $a$ with varying $S_{ACT}$.

$$S_{ACT} = 1 - \frac{1_{ACT}}{P(1 - K)} \quad (22)$$

Where $1_{ACT}$ is a certain function of $a_{ACT}$ at a certain pore size distribution and under the assumption of a certain distribution of water in the pores.

$$1_{ACT} = f(a_{ACT}) \quad (23)$$

Warris (17) has shown a theoretical method of calculation. Eq (20) can be drawn with $a \cdot \frac{D_{CR}}{2}$ or $a \cdot \frac{L_{CR}}{D}$ as independent variable and with $P(1 - K)$ as parameter. These functions are independent on the materials properties.

Eq (22) can also be drawn with $a \cdot \frac{D_{CR}}{2}$ or $a \cdot \frac{L_{CR}}{D}$ as independent variable, which means a division of the equation with the critical distance. However this curve is quite dependent on the materials properties via the function (23) and on the properties determining the value of the critical distance, $L_{CR}$ or $D_{CR}$.

The intersection of the two curves give the value of $S_{CR}$. An example is shown in fig 17. ($S_{CR}$)$_{min}$ is obtained when the pore water is located in the smallest pores since $a$ is minimum in this case.

If the aim is to study the influence of one single structural parameter on $S_{CR}$, it must be observed that each change, that according to eq (21) increase the value of $S_{CR}$, as a consequence of this, contributes to a decrease of $a_{1}$, that is, to a decrease of $S_{CR}$. So for instance a doubling of tensile strength can never correspond to an increase of $S_{CR}$ according to eq (21) with all parameters except $a_{1}$ constant.

An example is shown in fig 17. The doubling of $a_{1}$ gives an increase of $D_{CR}$ by a factor $1,41$ according to eq (11). Then according to eq (21) $S_{CR}$ is increased from 0,34 to 0,50. However because of the increase in $D_{CR}$ the curve $S_{ACT} = f(a)$ is displaced towards the right with a factor $1,41$. The new intersection between the curves of $S_{CR}$ and $S_{ACT}$ give the new value of $S_{CR} = 0,39$.

In the same manner an already exploited part of the strength does not influence the value of $S_{CR}$ in the same proportion that the residual strength is influenced. (However it might influence $S_{ACT}$).

A proof of the correctness of eqs (17), (18) and (19) can be obtained by knowledge of the critical degree of saturation, and the specific
surface of the air filled pores. Approximate specific surfaces of the coarse pores have been measured for two of the cellular concretes and the two clay bricks for which $D_{QR}$ and $S_{QR}$ were experimentally determined. The water was assumed to be present in the smallest pores at all degrees of saturation. The measurements were made with linear traverse technique on magnified photographs of ground surfaces. Then equations from (16) were applied in order to determine the connection between air content, $l_{ACT}$, and specific surface, $a_{ACT}$, (eq (23)). Those equations are based on spherical pores whereas the pores in the clay bricks were more elliptical. Eq (19) was used for calculation of $L_{CR}$ after which $D_{CR}$ was calculated from eq (13). The calculated values of $L_{CR}$ and $D_{CR}$ are given in table 3 together with experimental values of $D_{CR}$.

The theoretical critical thicknesses are about the same for both types of cellular concretes which is expected because of the same structure of the materials. Besides the values are reasonable since thin slices, 1.7 mm, have been delaminated at freezing.

The calculated $D_{QR}$-values of the two bricks are of the same order of size as the measured values. For the underburnt brick the agreement is perfect. The slight deviation may for instance be dependent on the assumption of spherical pores. Use of eq (18) instead of eq (19) give about the same $D_{CR}$ values for the cellular concretes but smaller values for the bricks.

The validity of eq (21) is limited by the following condition based on the ductility of the material (15).

$$S_{CR} \leq 0.917 + \frac{\varepsilon \cdot 3(1 - 2v)}{1.09 \cdot P(1 - K)}$$

For a completely brittle material, $S_{CR} < 0.917$. For the surface layer with thickness $D_{CR}/2$ of a materials unit or for a materials unit smaller than the critical size, $S_{CR} = 1.0$.

In the following the connections between materials structure and the parameters determining the values of $S_{CR}$ and $S_{ACT}$ are discussed very briefly.

Specific surface—The specific surface, $a$, of the air filled pores is one of the most important properties determining $S_{CR}$ which is clear from eq (21). The smaller the air filled pores the higher the value of $S_{CR}$ at constant materials properties. This has also been confirmed by experiments. See for instance table 3 where the two cellular concretes have about the same materials properties except the size distribution of coarse pores expressed by $a_{CR}$.

Thus the often noticed positive effect as regards frost resistance of diminishing the size of air bubbles in concrete is probably a result of the rise of the value of $S_{CR}$ at the same time as $S_{ACT}$ is constant if the air content is constant.

For a concrete with no air entrainment the coarse compaction pores
are distributed so far from each other that they could not serve as recipients, \( L > L_{CR} \). On the other hand the capillary pores are very small (< 0.1\( \mu \)). Hence their specific surface is very high (\( \sigma > 50000 \text{ mm}^{-1} \)). As a consequence, \( S_{CR} \) of the material is determined by the condition: 
\[
S_{CR} = 0.917 \text{ for the material that is left when the compaction pores are omitted.}
\]

The following equation can be derived for \( S_{CR} \) of a non air entrained concrete (15). The basis is wellknown data on the physical properties of cement paste (20).
\[
S_{CR} = \frac{\nu_{o}/c - \beta(0.19 + 0.25 \cdot k)}{1.09(\nu_{o}/c - \beta(0.19 + 0.25 \cdot k) + 1000 \cdot 1_o/c)}
\]  
(25)

Where \( k \) expresses the amount of non freezable water content as multiple of the amount of non evaporable water (15).
\[
K = k \cdot \frac{0.25 \cdot \beta}{\nu_{o}/c - 0.19 \cdot \beta + 1000 \cdot 1_o/c}
\]  
(26)

\( S_{CR} \) calculated from this equation adjusted to \( (S_o)_{CR} \) is marked out in fig 1. The agreement with measured values is excellent. The same good agreement have been measured for cement mortars (7).

Strength--The strength of a porous material is intimately coupled to its porosity, its pore size distribution, its grain size distribution and also to its age at constant porosity (for instance different strength-porosity connections must be valid for concretes at different degrees of hydration). For a heterogenous material like concrete it can easily be proved that the amount of dispersed particles (aggregates), size of the particles, affinity between the particles and the matrix and the elastic properties of the matrix and particles highly influence the strength-porosity relationship. All those parameters have been extensively discussed in (14).

Equations which express the strength-porosity relatively good are (14).

In the neighbourhood of the critical porosity, (for instance as a measure of effect of hydration on strength) it is valid.
\[
\sigma = \sigma_o (1 - \left( \frac{P}{P_{CR}} \right)^n) \quad \text{where } n = 1.0
\]  
(27)

or 
\[
\sigma = \sigma_o \cdot \ln \frac{P_{CR}}{P}
\]  
(28)

Where \( P_{CR} \) for a concrete is a function of the mix proportions (14): For an ordinary concrete or cement paste \( P_{CR} \) is:
\[
P_{CR} = 0.913 \cdot C \cdot \nu_{o}/c + 1 \cdot 1000
\]  
(29)
σ₀ or q is a fictive value. It is determined by the amount of aggregate, size of aggregate etc. Normally σ₀ is reduced with increasing amount of aggregate.

For concretes with the same degree of hydration, the same type and amount of aggregate the following equation can be used over a greater porosity range:

\[ \sigma = \sigma_0 (1 - p)^k \]  

(30)

More nuanced expressions are given in (14).

Theoretically it is the strength of the water saturated material that should be inserted in eq (21). Besides it is the residual strength after reduction because of an eventual exploited part that should be used.

**Ductility**—The ductility of a material can be expressed:

\[ \varepsilon_B = \frac{\sigma_B}{E_B} \]  

(31)

\[ \sigma_B \]  as well as \[ E_B \] are functions of the porosity and pore structure. \[ \sigma_B \] is even a function of pore size and general structure of the material.

A simple connection between porosity and ductility is:

\[ \varepsilon_B = \frac{\sigma_0 (1 - p)^{k_1}}{E_0 (1 - p)^{k_2}} = \varepsilon_0 (1 - p)^{k_1-k_2} \]  

(32)

Where \[ k_2 = \frac{4}{5} \] for a well curved concrete (14) and \[ k_2 = 3 \] for a cement paste (14).

\[ k_1 \] is quite dependent on the pore structure etc. However normally \[ k_1 > k_2 \]. \[ k_1 = 6 \] is not impossible for a concrete (14). Hence the ductility is increased with decreasing porosity. Increasing degree of hydration and decreasing water cement ratio are therefore favourable as regards ductility and \( S_{CR} \). This is also confirmed by experiments (14).

**Poissons ratio**—Poissons ratio is almost independent on porosity as far as this adopts normal values.

**Non freezable water content**—The freezing point of water in a pore is a function of the pore radius. On basis of the theory of capillary condensation the following simplified equation can be derived (19). It is valid for a material in equilibrium with a high relative humidity

\[ r = - \omega \cdot \frac{2 \cdot \sigma_G \cdot M_{G}}{\rho_L \cdot \Delta H} \cdot \frac{1}{T-T_0} + 28.5 \cdot 10^{-18} \cdot \frac{3}{\ln\left(\frac{\sigma_0}{T_0}\right)} \]  

(33)
Where the second term is the thickness of the adsorbed layer and the first term is the "Kelvin radius". $\Delta H$ is a function of temperature (19). Thus the smaller the pore, the lower the freezing point. In fig 18 is shown the pore size distribution calculated from freezing point depressions determined by adiabatic calorimeter thawing experiments and two determinations by mercury porosimeter. The material is sand lime brick. The disagreement could be an effect of hysteresis absorption-desorption since mercury porosimeter is an absorption process.

Since the adsorption isotherm is a function of the pore size distribution there must be some connection between the isotherm and the non-freezable water content. Such an approximate expression is:

$$\Delta T = \frac{R \cdot T \cdot (T - T)}{\Delta H} \cdot \ln \frac{p}{p_0}$$

Thus by knowledge of the amount of water absorbed at different relative humidities, the non freezable water content at different temperatures can be determined (19), (20).

In fig 19 is shown the upper part of the absorption and desorption isotherm determined by experiments (21), and calculated by use of eq (33). The material is the same sand lime brick as in fig 18. The agreement between the adsorption isotherm is satisfactory. However, since it is very difficult to experimentally obtain the isotherm in the high pressure range in question it is easier to make the determinations of non-freezable water content via special experiments. (Perhaps the knowledge of non-freezable water contents could even be used as a very easy means of calculating the isotherm in the high pressure range).

Owing to pore size restrictions on ice formation, pore water in isolated capillaries could be unfrozen at low temperatures because of supercooling (22). This is confirmed by thawing experiments on specimens frozen to -25°C and -6°C. Fig 20 shows an example of this. Eq (33) is therefore somewhat limited especially for dense concretes where the waterfilled cement gel could not freeze until ice formation is nucleated in the pore at temperatures lower than the normal freezing temperature. If the surrounding pores are very narrow the ice in these isolated pores could be formed by homogeneous nucleation at -40°C (23). Then at this temperature a large amount of ice would be formed almost simultaneously and the specimen destructed since its permeability is low at this stage.

**Rate of ice formation**—The ice formation can be divided in two or three stages:

**Stage 1**—Rapid ice formation when supercooled water is nucleated. The temperature of the specimen is then normally raised if the amount of large pores is great. If the process is adiabatic the following mean rate of ice formation is obtained:
Where $\Delta t$ is the time needed in order to raise the temperature of the specimen. Date of ice formation is however greatest close to the spot of nucleation. The mean rate of ice formation is therefore dependent on the size of specimen. According to (22) the rate of ice front propagation at nucleation is about $10 \text{mm\cdot s}^{-1}$. The interval $\Delta t$ can therefore be expressed as a function of size of specimen (15).

$$\Delta t = \frac{R}{v_{\text{ice}}} = 100 \cdot R = 300 \cdot \frac{V}{A}$$

(36)

It seems logical not to take the whole specimen in consideration when $\Delta t$ is calculated but only the critical sphere of the material eq (14). By use of eqs (14) and (36) eq (35) is changed to;

$$\frac{d\phi}{dt} \cdot v_f = \frac{\Delta T_o \cdot 2}{\rho_w \cdot \Delta h \cdot 100 \sqrt{3} \cdot D_{CR}} \left( y_p \cdot c_p + S_e \cdot P \cdot \rho_w \cdot c_w \right)$$

(37)

Note: the permeability at this early freezing is considerably greater than at the subsequent freezing. This influences the value of $D_{CR}$.

Stage 2—Normal ice formation. The rate of ice formation in this stage is proportional to the temperature difference between ambient air and specimen surface (8).

$$v_f \cdot \frac{d\phi}{dt} = k (\theta_{\text{SPEC}} - \theta_{\text{AIR}})$$

(38)

Where the constant $k$ is dependent on convection of the air and of the surface-volume ratio of the specimen.

A heat balance equation for the already frozen zone like the one leading to eq (15) leads to:

$$v_f \cdot \frac{d\phi}{dt} = \frac{1}{\Delta h \cdot \rho_w} \left\{ y_p \cdot c_p + c_v \cdot K \cdot c_v + \rho_w \cdot P (S_e - K) \cdot c_l \right\} \frac{d\phi}{dt}$$

(39)

In this expression $y_p$ and $c_p$ both decrease proportional to porosity.

Calculations show that ice formation in stage 1 is 4000 to 6000 times greater than in stage 2 if $d\phi/dt = 6^\circ C/h$. However in this latter stage permeability is gradually decreased.

Stage 3—This stage is the eventual homogeneous nucleation of supercooled water in isolated capillaries at $=-40^\circ C$.

Eq (35) can be used if consideration is taken to earlier transformation of some water into ice. In this stage permeability can be almost zero.
**Permeability**—The following simplified expression for coefficient of permeability can be derived: (15).

\[ B = \frac{P^3}{T^2 \cdot \eta^2 \cdot \mu} \]  \hspace{1cm} (40)

Where \( P \) is the "waterfilled" porosity.

According to eq (33) and fig 18 the amount of ice at each temperature is dependent on the pore size distribution. Hence it is suitable to modify eq (40) by dividing the porosity in different pore size classes:

\[ B = \sum \frac{P_n^3}{T_n^2 \cdot \eta_n^2 \cdot \mu_n} \]  \hspace{1cm} (41)

Where \( P_n \) for instance corresponds to pores with freezing points between 0°C and -1°C. The viscosity of ice is negligible to that of water which means that an ice filled pore does not contribute to the permeability. Hence the following simplified expression for the variation of coefficient of absorption with temperature can be derived.

\[ B_\theta = (\frac{\eta'}{\eta_f})^3 \cdot \frac{1}{T_\theta^2 \cdot \eta_f^2 \cdot \mu_f^2} \cdot \text{const} \]  \hspace{1cm} (42)

Where also \( T, \eta, \) and \( \eta_f \) are functions of temperature since they are dependent on \( n_f^f \). \( \eta' \) is increasing substantially with decreasing temperature.

Eq (42) is only valid for a material where all the water-filled pores are "permeable". In reality it is however possible that the frozen water blocks the pores so that water at low temperatures is frozen as in a closed container. The blocking may eventually be caused by the first small amount of ice formed. In such a case the variation of permeability with temperature is dependent on the amount of ice formed but also on the degree of saturation in the specimen. A possible equation is:

\[ B_\theta = B_\theta^0 - \beta \cdot \eta_f \cdot \eta' \cdot f(S) \]  \hspace{1cm} (43)

The function \( f(S) \) is determined by the shape of the pore system. In special cases \( B_\theta^0 = 0 \) when a certain amount of ice is formed. Then the continued freezing occurs in an almost sealed container.

**Test of the hydraulic pressure theory**

Eq (21) assumes that the mechanism of frost deterioration is mainly hydraulic pressure for all materials. This has been criticized, since in this case a highly permeable material like clay brick could not be destructed by frost (24). The fact is however, that critical thicknesses as those predicted by eq (11) have been found even for clay bricks. Eq (42) brings an explanation for this. Even if \( T \) and \( \eta \)
are considered constant, the amount of non-freezable water is so low in clay brick that the permeability is enormously reduced.

For the well-burnt clay brick mentioned earlier \( \frac{V_{nf}}{V_0} < 0.062 \) at the final freezing. Then \( B \) is reduced to at least: \( 0.0625^3 = 2.4 \times 10^{-8} \) of its original value. This in turn is not the permeability of the material but the permeability of the water-filled part of the material which can be considerably lower.

If the hydraulic pressure theory is valid, the expansion of a specimen ought to follow an expression of type

\[
\varepsilon = \text{const} \cdot \frac{d\beta}{dt}
\]

(44)

\( \varepsilon \) is however limited to a value correspondent to the water expansion at ice formation. This limitation is essential at low permeabilities, "closed container":

\[
\varepsilon \leq \frac{1}{3(1-2v)} \cdot \frac{\Delta V}{V} = \frac{1}{3(1-2v)} \cdot 0.09 \cdot V_{nf} \cdot \beta
\]

(45)

Hence, by experiments where the expansion, the rate of ice formation and the permeability are measured, the validity of the hydraulic pressure theory might be confirmed through eq (44).

Such experiments are done at our institution. The apparatus is a calorimeter-extensometer, the principle of which is shown in fig 21. A similar apparatus have been described in (25). The specimen, size 30 x 30 x 120 mm³, is adapted to a certain degree of saturation, and mounted in the specimen chamber. The total assembly is immersed in a kerosene bath with constant low temperature. The length changes, heat flow and specimen temperature are measured automatically. By knowledge of the calorimeter constant and the heat capacity of the assembly, the amount of ice formed can be measured.

An apparatus for permeability measurements at low temperatures has been built. Reliable experiments have however not been performed so far.

Cement. Fig 22 shows such a freezing experiment for a non air entrained very porous paste. The degree of saturation in the specimen, is less than the critical value calculated from an equation of type (25).

Fig 23 shows the same specimen after 2 months prolonged curing in lime water which makes the degree of hydration somewhat higher. Besides in this experiment \( S > \text{calculated } S_{cr} \).

Fig 24 shows the result of freezing of a clay brick with a degree of saturation exceeding the critical, which has been determined in the normal way mentioned earlier.

In all three experiments the pore-water is supercooled to \(-4 \to -5^\circ C\). Then freezing is initiated and the specimen temperature rises. The specimens expand because of hydraulic pressure arising when the
Then, for both the specimens where $S > S_{cr}$, the expansion continues as long as ice is formed. Hence the cement paste expands all the time while the clay brick begins to contract when almost all ice is formed at -5°C.

The dryer cement paste contracts all the time despite the amount of ice formed is as high as in the case where $S > S_{cr}$. The contraction for the cement paste as well as for the clay brick exceeds the normal thermal contraction (broken line). At melting the slope of the line length-change-temperature is about the same as for freezing. Since the melting is not accompanied by any hydraulic pressure expansion, it seems reasonable to assume that the measured slope at melting is the real thermal expansion for the mixture porous material-ice. The coefficient of thermal expansion for a two phase material can be expressed.

$$\alpha = \frac{a_1 \cdot V_1 \cdot K_1 + a_2 \cdot V_2 \cdot K_2}{V_1 \cdot K_1 + V_2 \cdot K_2} \quad (46)$$

Where $K$ is bulk modulus and the indices 1 and 2 represents ice and solid material.

$a_1$, for ice, is about $52 \cdot 10^{-6}$ at $0^\circ C$ but decreases with decreasing temperature. $a_1$ (solid phase) is about $5 \cdot 10^{-5}$ for a ceramic material. $K_1 = 10^5$ kp/cm$^2$ for poly-crystalline ice at $-5^\circ C$ (22). $K_2 = K_o(1-P)^3$ for a porous material (14) where $K_o = 600,000$ kp/cm$^2$.

$P$ is the total porosity since there is no adherence between the ice body and the pore wall.

$V_1$ is the volume of ice after freezing. Then according to eq (46) the following ratios of coefficients of thermal expansions at freezing temperatures and at ordinary temperatures are valid.

For clay brick: $\alpha < -5^\circ C$ and $\alpha > 0^\circ C$.

For cement paste: $\alpha = 5^\circ C \rightarrow -10^\circ C = 2.4$; $\alpha = 10^\circ C \rightarrow -20^\circ C = 2.7$ (measured values = 3.0).

Hence, the often noticed increased thermal contraction at a freezing can also be explained theoretically as a purely mechanical effect. The usual explanation is shrinkage caused by migration of unfrozen water to ice bodies in the pores (12). The experiment with the clay brick shows however the same characteristics as the paste experiment despite the brick has almost no unfrozen water ($K_{10} = 0.05$) while the paste has considerable amounts ($K_{10} = 0.51$). Besides a clay
brick shows almost no shrinkage at water loss.

The thermal contraction at freezing is however somewhat smaller than the expansion at thawing. This can eventually be explained by hydraulic pressure acting during freezing.

The clay brick and the paste at high degree of saturation show great expansions as long as ice is formed. Those expansions can not be explained as in situ freezing in a closed container. viz expansions calculated from (45) are up to 15 times greater than the measured. Hence water must be forced through the specimen from the freezing site. A hydraulic pressure must occur. The question is whether this pressure is big enough to expand the specimen in the observed way. If not, the expansion must be a consequence of some other phenomenon, ice lens segregation (1,12) or some other mechanism (24,26).

Since the very rapid freezing caused by supercooling expands the specimen less than the continued freezing which occurs with considerably lower rate, the permeability must be enormously reduced if the mechanism should be hydraulic pressure.

In the following an attempt is made to in a very simplified way calculate in which way the permeability is changed when the temperature is lowered.

If the tortuosity is constant the permeability at 0°C compared to that at 0°C is:

\[
\frac{B_0}{B_e} = \left(\frac{w_{nf}}{w_e}\right)^3 \left(\frac{Y_0}{Y_e}\right)^2
\]

(47)

But for spherical pores the specific surface can be expressed.

\[
Y_0 = 3 \cdot \frac{w_{nf}}{r}
\]

(48)

Where \( r \) is the radius of permeable pores.

\( r \) is coupled to the freezing point depression according to eq (33) which can be simplified to (19).

\[
r = \frac{1}{8.061 \cdot 10^6 \Delta T - 6.12 \cdot 10^4 (\Delta T)^2 + 2 \cdot 10^2 (\Delta T)^3}
\]

(49)

But \( w_{nf} \) is a function of \( \Delta T \).

\[
w_{nf} = f(\Delta T)
\]

(50)

Then by use of eqs (47) - (50) the change of permeability with temperature can be calculated.
For the cement paste eq (50) is: (see fig 23)
\[ v_{nf} = 5 \cdot \Delta T^{-1/2} \]  
(51)
Hence eq (49) gets approximately:
\[ r = k \cdot v_{nf}^2 \]  
(52)
By use of eq (52) and eq (48) eq (47) is changed to:
\[ \frac{B_0}{B_e} = \left( \frac{v_{nf}}{v_e} \right)^5 \]  
(53)

The measured rate of ice formation can be divided by the calculated permeability which according to eq (44) gives the expansion. This theoretical expansion have been calculated and is indicated in fig 25 where the experiment in fig 23 is rewritten with time as independent variable. The constant in eq (44) is chosen so that calculated and measured expansion coincide at \(-19^\circ C\). The agreement between the two expansions is fair bearing in mind the approximate calculation of permeability. The expansion around \(0^\circ C\) is very difficult to calculate since the rate of ice formation is uncertain. It must be observed that no consideration is taken to thermal contraction in the calculated curve.

In the brick almost all ice is formed around \(0^\circ C\). Hence the specific surface is considered constant and the relative permeability gets the form:
\[ \frac{B_0}{B_e} = \left( \frac{v_{nf}}{v_e} \right)^k \]  
(54)
Where \(k = 2,0\)

This equation have been used for calculation of expansion in the same way as above. The result together with experimental curves is shown in fig 26. The agreement down to \(-5^\circ C\) is excellent. The same good agreement is obtained even when the exponent \(k\) in eq (54) is 3 or 4. At temperatures lower than \(-5^\circ C\) the specimen contracts thermally from the expanded state. The hydraulic pressure theory at use of eq (54) indicates however that the specimen ought to contract drastically because ice formation is almost finished. See \(e_{CAlC}\) eq (44) in fig 26. However the permeability gets very low for which reason it is possible that the late freezing is a freezing in a closed container. Eq (45) shows however that this would mean a substantial expansion. See \(e_{CAlC}\) eq (45) in fig 26. Hence it seems as if the expansion caused by hydraulic pressure in the range \(0 - -5^\circ C\) is locked by ice formed in the expanded specimen. Then at the continued freezing the expanded specimen contracts thermally according to eq (46) from its expanded state. The thermal contraction is however reduced by the continued hydraulic pressure according to eqs (44) and (54). This can be the explanation...
of the discrepancy between thermal contraction and expansion in fig 24.

The maximum reduction in permeability for the cement paste is $1,3 \times 10^{-3}$ according to eq (53). For the clay brick it is $4,8 \times 10^{-3}$ according to eq (54) at maximum expansion. With the perhaps more reasonable exponents 3 or 4 in eq (54) it is however $3,4 \times 10^{-4}$ or $2,3 \times 10^{-5}$. In this case the effect on permeability of blocking the pores with ice is 25 to 175 times greater for clay brick than for cement paste which is reasonable.

Thus it seems as if the hydraulic pressure theory can explain all the phenomena seen at a freezing even for two so different materials as cement paste and clay brick. This is very essential since in this case connections between materials properties and critical degrees of saturation can be derived in the way indicated above.

Influence of materials properties on the actual degree of saturation

This subject will be treated very briefly.

Rate of water uptake and drying—The rate of water uptake as well as the rate of drying increases with increasing pore radius.

For a material with tubular pores of different sizes the degree of saturation on a critical depth, $D_{CR}/2$ from the surface at a water uptake is (15).

$$S_e^* \cdot X = \frac{2}{P \cdot D_{CR}} \cdot \sum_{n} \frac{P}{n} \cdot \frac{\sqrt{r \cdot n \cdot g \cdot \cos \beta}}{2 \cdot \mu} \cdot \frac{1}{D_{CR}} \cdot \frac{13}{t} \cdot \frac{s}{F} \quad (55)$$

Where $P$ is the amount of pores of a certain size. $F$ is a mean pore radius.

Hence, at a certain $D_{CR}$ and a certain time, $t$, $S_{CR}$ on the critical depth increases with increasing pore size. The equation is however very simplified since it takes no consideration to bifurcations between different pores which means that $S_e^* = 1,0$ at long enough time.

The drying can be divided into two parts. The first part corresponds to a saturated water flow from the interior of the material to the surface. The second part is a combination of liquid water and diffusion process when there is no longer a continuous water phase in the material. The second part is a considerably slower process than the first.

The first transport has a permeability of type (40). However, the pore properties are of no importance in this stage as long as rate of transport is great enough to keep a free water surface on the materials surface. Then the rate of drying is constant. Of course there is a need of faster water transport within the specimen when the ambient air gets drier or is forced to move along the materials surface.

The diffusion process increases its rate with increasing porosity and pore size. Dependent on the pore size Hagen-Poiseulles law or Knudsen's law is predominant.
Total water uptake

The total water uptake in the wet part of a specimen when the waterfront has reached a distance, \( x \), from a free water surface, can be calculated from a combination of the "coefficient of water uptake" \( k_w \) and the "coefficient of capillarity" \( k_c \), which in turn can be determined experimentally.

\[
k_w = \frac{Q_w}{t^{k_1}}
\]

\[
k_c = \frac{k}{x^{k_2}}
\]

Where \( k_1 \) and \( k_2 \) are constants. Then it is valid,

\[
(S_e)_{MAX} = k_w \cdot k_c \cdot x^{(k_1 \cdot k_2 - 1)}
\]

For a single capillary \( k_1 \cdot k_2 = 1/2 \cdot 2 = 1 \). In this special case \( (S_e)_{MAX} = k_w \cdot I_c^{1/2} \).

For a porous material \( k_1 \cdot k_2 \leq 1 \) which means that \( (S_e)_{MAX} \) as a mean value of the whole wet part of the specimen will decrease with the capillary rise, \( x \). This is an essential result since it means that the surface part of a specimen has a higher \( (S_{ACT})_{MAX} \) than the inner parts. cf fig 12.

The constants \( k_1 \) and \( k_2 \) must be dependent on the pore structure. Perhaps experiments can be designed in order to find out correlations between those constants and the pore properties. Such experiments must be fundamental for the understanding of the second part of the frost resistance problem, viz. the value of \( S_{ACT} \). Many investigators have found correlations between pore size distribution and frost resistance \((27, 28)\). Perhaps this correlation is an effect of the pore size distribution on the constants \( k_1 \) and \( k_2 \), viz. it seems reasonable to assume that more air is entrapped in a specimen when the pore size distribution is wide than when all pores are of the same size.

In \((29)\) the capillary water uptake of a random pore system with bifurcations is treated. It is shown theoretically, that the coarsest pores are filled at first, but they very soon deliver their water to the smaller pores. Then they can not be filled again until all the surrounding smaller pores are filled. If the coarse pore has such a shape that it is surrounded only by smaller pores (air pore in cement paste) it cannot be filled again until the air in the pore can penetrate the waterfilled surrounding pores. The air pressure needed is inversely proportional to the surrounding pore radius.

\[
p = \frac{2 \cdot \sigma \cdot L_0}{r} \cdot \cos \theta
\]

At a pore radius of \( 10u \) the pressure needed is \( 0.15 \) kp/cm\(^2\). Such a pressure can normally only be obtained by artificial means.
(vacuum).

Experiments have however shown that even air bubbles in a cement paste may be filled with water if the specimen is stored for a very long time in water. This is possibly an effect of condensation in the pores.

The locking of pores with water according to eq (59) has very important practical significance for light weight aggregate concretes. cf fig 15. Even if the aggregate particles have a bad durability (their $S_{CR} < S_{ACT}$) when they are single they can be used as aggregate in a durable concrete since their pores are blocked by the dense cement paste. Hence they can not be filled again, once they have dried out.

ACKNOWLEDGEMENTS

The author wants to thank professor S G Bergström, who initiated this research and who has provided many ideas. Another thank is transmitted to the National Swedish Council for Building Research, which has financed this investigation.

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SYMBOLS

A = specimen surface (m²)
B = coefficient of permeability (including viscosity of fluid) (m³·s/kg)
C = cement content (kg/m³)
D_CR = critical thickness of saturated slice (m)
E_B = Young's secant modulus at fracture (N/m²)
E_n = Young's modulus after n cycles freezing (N/m²)
K = non freezable water content at lowest temp as fraction of pore-volume, cf eq (10)
K = bulk modulus (N/m²)
L_CR = critical wall thickness of saturated hole sphere (Powers' spacing factor) (m)
M = molecular weight of water (kg/k mole)
P = porosity (m³/m³ material)
P_CR = critical porosity where σ_B=0
Q_dry = weight of dried specimen (kg/m³ material)
Q_e = weight of evaporable water (kg/m³ material)
R = gas constant (Nm/°K·k mole)
R = radius of materials sphere (m)
R_CR = critical radius of saturated sphere (m)
S = degree of saturation, eq (2)
S_a = coefficient of absorption, eq (1)
S_e = degree of saturation, eq (3). Note: S_e ≠ S_a
(S_e)ₓ = degree of saturation on depth x
S_ACT = actual degree of saturation (cf (S_e)ACT; u_ACT)
S_CR = critical degree of saturation (cf (S_e)CR; u_CR)
T = "Tortuosity factor" (m/m)
T_o = ordinary freezing temp (°K)
V = volume in general
specimen volume, eq (36) \( \text{m}^3 \)

specific surface of the waterfilled part of the pore system \( \text{m}^2/\text{m}^3 \) material. Note: \( Y \neq \alpha \)

c = specific heat \( \text{Nm/kg} \cdot ^\circ \text{C} \)

\( \frac{dB}{dt} v_f \) = rate of ice formation \( \text{m}^3/\text{m}^3 \) material \cdot s

k = constant in general

k = non freezable water as multiples of non evaporable water content, eqs (25), (26)

\( k_c \) = "coefficient of capillarity"

\( k_w \) = "coefficient of water uptake"

l = air content before freezing \( \text{m}^3/\text{m}^3 \) material

\( l_{\text{ACT}} \) = actual air content correspondant to \( S_{\text{ACT}} \) \( \text{m}^3/\text{m}^3 \) material

\( l_o \) = air content at mixing \( \text{m}^3/\text{m}^3 \) concrete

n = exponent eq (27)

p = pressure \( \text{N/m}^2 \)

\( p/p_s \) = relative vapour pressure

q = constant eq (28)

r = (Kelvin) radius of capillary \( \text{m} \)

s = Frost resistance, eq (5) \( (\text{cf} s_u, s_e) \)

t = time \( \text{s} \)

u = moisture ratio \( \text{kg/kg} \)

\( u_0 \) = moisture ratio at complete saturation \( \text{kg/kg} \)

\( v_{\text{ice}} \) = rate of propagation of ice front \( \text{m/s} \)

\( w_a \) = max water uptake at capillary water uptake at ordinary pressure and constant temp \( \text{m}^3/\text{m}^3 \) material

\( w_e \) = evaporable water content at lowest temp \( \text{m}^3/\text{m}^3 \) material

\( w_f \) = freezable water content at lowest temp \( \text{m}^3/\text{m}^3 \) material

\( w_f' \) = freezable water content in a completely saturated slice within a materials volume \( \text{m}^3/\text{m}^3 \) watersaturated material. Note \( w_f' \neq w_f \).
\( w_{nf} \) = non freezeable water content at lowest temp \((m^3/m^3 \text{ material})\)

\( w_{o/c} \) = water cement ratio \((kg/kg)\)

\( x \) = distance from materials surface to ice front or water front \((m)\)

\( x_{us} \) = unsaturated depth; depth from surface to a place where expelled water can be taken care of \((m)\)

\( (x_{us} - x)_{CR} \) = "critical depth of unsaturation", eq (15) \((m)\)

\( \alpha \) = specific surface of air filled pores, eq (13) \((m^2/m^3 \text{ pore-volume})\)

\( \alpha \) = thermal expansion coefficient \((m/m^0\text{C})\)

\( \beta \) = fraction of \( w_f \) actually frozen

\( \beta \) = degree of hydration = fraction hydrated cement. eqs (25), (26) \((kg/kg)\)

\( \beta_o \) = fraction of \( w_f \) freezing at ceasing of supercooling

\( \gamma_p \) = density of dried specimen \((kg/m^3)\)

\( \Delta h \) = heat of fusion \((Nm/kg)\)

\( \Delta H \) = molar heat of fusion \((Nm/k \text{ mole})\)

\( \Delta t \) = time needed in order to raise temperature \( \Delta T \) at ceasing of supercooling \((s)\)

\( \Delta T \) = freezing point depression \((^0\text{C})\)

\( \Delta T_o \) = temperature rise at ceasing of supercooling \((^0\text{C})\)

\( \Delta V \) = relative volume change

\( \epsilon \) = linear strain at hydrostatic tension

\( \epsilon_B \) = fracture linear strain at hydrostatic tension

\( \epsilon_o \) = fracture strain of solid phase

\( \mu \) = viscosity \((Ns/m^2)\)

\( v \) = poisson's ratio

\( \omega \) = shape factor of ice crystal

\( \rho \) = density \((kg/m^3)\)
\( \sigma_o \) = theoretical strength of solid phase (N/m\(^2\))
\( \sigma_B \) = tensile strength of material (N/m\(^2\))
\( \sigma_{LG} \) = surface tension liquid-gas (N/m)
\( \theta \) = temperature (°C)
\( \theta \) = wetting angle

Indici

L = liquid
LG = liquid-gas
i = ice
p = dry specimen
w = water
### TABLE 1 Analysis of data from (9).

<table>
<thead>
<tr>
<th>Method</th>
<th>Time in unfrozen water (&gt;0°C) per cycle</th>
<th>Time in air per cycle</th>
<th>Time in air of unfrozen specimen (&gt;−5°C) per cycle</th>
<th>( t_{aw} / t_w )</th>
<th>( t_a / t_w )</th>
</tr>
</thead>
<tbody>
<tr>
<td>C290: Rapid water</td>
<td>1.2</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>C291: Rapid air</td>
<td>0.7</td>
<td>1.3</td>
<td>0.3</td>
<td>0.43</td>
<td>1.85</td>
</tr>
<tr>
<td>C292: Slow water</td>
<td>29</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>C310: Slow air</td>
<td>7</td>
<td>18</td>
<td>1.5</td>
<td>0.21</td>
<td>2.57</td>
</tr>
</tbody>
</table>

### TABLE 2 The frost-resistance of four types of light weight aggregate concrete

<table>
<thead>
<tr>
<th>Material, type and density (kg/m³)</th>
<th>S&lt;sub&gt;e,CR&lt;/sub&gt;</th>
<th>Frost resistance, s&lt;sub&gt;u&lt;/sub&gt; according to eq (7)</th>
<th>At knick-point absorption</th>
<th>At absorption for</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>24 h</td>
<td>240 h</td>
</tr>
<tr>
<td>1 860</td>
<td>0.46</td>
<td>0.243</td>
<td>0.230</td>
<td>0.194</td>
</tr>
<tr>
<td></td>
<td>0.48</td>
<td>0.258</td>
<td>0.246</td>
<td>0.210</td>
</tr>
<tr>
<td>2 785</td>
<td>0.33</td>
<td>0.135</td>
<td>0.120</td>
<td>0.083</td>
</tr>
<tr>
<td></td>
<td>0.34</td>
<td>0.159</td>
<td>0.145</td>
<td>0.107</td>
</tr>
<tr>
<td>3 630</td>
<td>0.22</td>
<td>0.062</td>
<td>0.036</td>
<td>-0.011</td>
</tr>
<tr>
<td></td>
<td>0.28</td>
<td>0.066</td>
<td>0.050</td>
<td>-0.002</td>
</tr>
<tr>
<td>4 1240</td>
<td>0.27</td>
<td>0.049</td>
<td>0.030</td>
<td>-0.016</td>
</tr>
<tr>
<td></td>
<td>0.28</td>
<td>0.075</td>
<td>0.054</td>
<td>+0.005</td>
</tr>
</tbody>
</table>

### TABLE 3 Test of the correctness of equations (17), (18) and (19).

<table>
<thead>
<tr>
<th>Material</th>
<th>S&lt;sub&gt;e,CR&lt;/sub&gt; meas.</th>
<th>l&lt;sub&gt;CR&lt;/sub&gt; meas.</th>
<th>l&lt;sub&gt;CR&lt;/sub&gt; calc. (mm&lt;sup&gt;-1&lt;/sup&gt;)</th>
<th>a&lt;sub&gt;CR&lt;/sub&gt; calc. (mm)</th>
<th>2·L&lt;sub&gt;CR&lt;/sub&gt; calc. (mm)</th>
<th>D&lt;sub&gt;CR&lt;/sub&gt; calc. (mm)</th>
<th>D&lt;sub&gt;CR&lt;/sub&gt; meas. (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cellular concrete, type 1, density =500 kg/m³</td>
<td>0.62</td>
<td>0.309</td>
<td>6.45</td>
<td>0.648</td>
<td>0.783</td>
<td>&lt;1.7</td>
<td>&lt;1.7</td>
</tr>
<tr>
<td>Cellular concrete, type 3, density =500 kg/m³</td>
<td>0.48</td>
<td>0.420</td>
<td>3.57</td>
<td>0.774</td>
<td>0.886</td>
<td>&lt;1.7</td>
<td>&lt;1.7</td>
</tr>
<tr>
<td>Underburnt clay brick</td>
<td>0.85</td>
<td>0.061</td>
<td>5.37</td>
<td>5.78</td>
<td>12.20</td>
<td>12</td>
<td>14</td>
</tr>
<tr>
<td>Well burnt clay brick</td>
<td>0.76</td>
<td>0.076</td>
<td>5.90</td>
<td>4.12</td>
<td>7.90</td>
<td>12 à 14</td>
<td></td>
</tr>
</tbody>
</table>
In = Residual dyn. Young's modulus 
\( \frac{E_n}{E_0} \) after 10 to 13 freezing cycles (%)

Concrete without fibres

\( W_o/C = 0.52 \)
Aggr.cem. = 1:4:1  
Air content = 2%

Capillary water uptake:
24 h
120 h
1200 h

Measured \( S_{CR} = 0.86 \)
Calculated \( S_{CR} = 0.85 \)

Concrete with steel fibres

\( W_o/C = 0.51 \)
Aggr/cem. = 1:4:0  
Air content = 1.2%
Fiber volume: ~ 1.5 vol.%

Capillary water uptake:
24 h
120 h
1200 h

Measured \( S_{CR} = 0.86 \)
Calculated \( S_{CR} = 0.85 \)

FIG 1 Experimental and theoretical critical degrees of saturation of a concrete with or without steel fibres. Capillary water uptake indicated in the figure.

\( E_n/E_o (\%) \)

\( S > S_{CR} \)
\( S \approx S_{CR} \)
\( S < S_{CR} \)

FIG 2 Principles for variation of dynamic Young's modulus with number of cycles when the degree of saturation is constant.
FIG 3 Principles of effect of specimen size on freezing conditions and temperature distribution.

FIG 4 Distribution of water in two specimens of cellular concrete, density 530 kg/m³, size 30 x 30 x 120 mm³, immediately before the first freezing.
FIG 5 The mechanism in obtaining moisture gradients at drying.

FIG 6 Apparatus for adapting specimens to proper degrees of saturation.
FIG 7 Apparatus for cyclic freezing-and-thawing.

FIG 8 Normal freezing and thawing cycle.
FIG 9 Result of a comparison of the four methods according to ASTM of freeze-testing concrete. (9) Each pile is one type of concrete.

FIG 10 Water uptake test.
FIG 11 Determination of capillary water uptake of two concretes. Definition of "knick-point absorption".

Moisture ratio (%)
FIG 12 Effect of specimen thickness on "knick-point absorption".
\( E_n / E_o(\%) \) Residual Young's modulus after 6 to 12 freezing cycles

\[ u_{CR} = 0.361 - 0.373 \]

FIG 13 Critical moisture ratio of a light weight aggregate no fines concrete (Type 1 Table 2).

\[
\frac{S_A}{S_B} = \frac{(SCPA)_A - (SACT)_A}{(SCPB)_B - (SACT)_B} \quad \text{eq}(8)
\]

FIG 14 Frost resistance of the four light weight aggregate concretes in Table 2 related to the frost resistance of type 1 at "knick-point absorption".
a) Materials used single

A: Dense material
$S_{CR}^A = S_{ACT}^A$

B: Permeable material
$S_{CR}^B > S_{ACT}^B$

b) Layered structure

$S_{CR}^B < S_{ACT}^B$
at interphase

S_{CR}^B < S_{ACT}^B at a short distance close to the interphase. If $S_{ACT}$ in B is small this distance is very short and the material combination durable.

c) Particle composite

FIG 15 Principles of use of critical degrees of saturation at materials combinations.

FIG 16 Critical thicknesses of completely saturated clay bricks:
size: $30 \times 30 \times d \text{ mm}^3$. 
FIG 17 Principles of determination of the critical degree of saturation. Determination of effects of strength on critical degree of saturation.

Sum pore volume (%)

- from experimental freezing point depressions and eq (33)
- two determinations with mercury porosimeter

FIG 18 Comparison between pore size distribution determined by experimental freezing point depressions and by mercury porosimeter. Sand lime brick.
FIG 19 Comparison between non freezable water content and sorption isotherm. Same sand lime brick as in Fig's 18 and 20.

\[ K = \frac{W_{nf}}{P} \]

FIG 20 Effect of freezing temperature on non freezable water content. Same sand lime brick as in Fig's 18 and 19.
FIG 21 Schematic view of combined dilatometer and calorimeter for measurements of length changes, amount of ice formed and rate of ice formation.

1. Outer jacket of brass.
2. Strain gauges 1000Ω full bridge.
3. Outer resistance thermometer (copper wire).
4. Inner resistance thermometer (copper wire).
5. Polyurethane foam cast in situ.
6. Screw (support).
7. Specimen 30x30x120 mm³ wrapped in plastics foil with 3 thermocouples and with knobs in the ends.
8. Invar frame.
Measured length change, amount of ice formed and rate of ice formation at freezing.

*FIG 22 Cement paste: Wo/C = 0.83 air content at mixing = 6%.
Wn/C = 0.20 : P = 60.0 %: specimen volume = 100 cm³
Se = 0.83 : calculated (Se)CR = 0.86. Kmin = 0.364*
FIG 23 Cement paste: Wo/C = 0.83; air content at mixing = 6 %; Wn/C = 0.22; P = 58.8 %; specimen volume = 100 cm$^3$; Se = 0.895 calculated (Se)CR = 0.86; Kmin = 0.433

Measured length change, amount of ice formed and rate of ice formation at freezing.
FIG 24 Clay brick, density 1690 kg/m$^3$: P = 39.3 %. specimen volume = 92 cm$^3$: Se = 0.87. (Se)$_{\text{measured}} = 0.85$; $K_{\text{min}} = 0.025$

Measured length change, amount of ice formed and rate of ice formation at freezing.
FIG 25 The cement paste in Fig 23. Measured and calculated length changes at freezing.
FIG 26 The clay brick in Fig 24. Measured and calculated length changes at freezing.
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**Bulletiner**


**Internare rapporter**


**Rapporter**

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