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PO Box 117
221 00 Lund
+46 46-222 00 00

Inhomogeneous spin excitations in weakly coupled spin- $\frac{1}{2}$ chains

L. Shen ^{1,*}, E. Campillo ¹, O. Zaharko,² P. Steffens ³, M. Boehm,³ K. Beauvois,³ B. Ouladdiaf,³ Z. He,⁴ D. Prabhakaran,⁵ A. T. Boothroyd ⁵ and E. Blackburn ^{1,†}

¹*Division of Synchrotron Radiation Research, Lund University, SE-22100 Lund, Sweden*

²*Laboratory for Neutron Scattering and Imaging, Paul Scherrer Institut, CH-5232 Villigen PSI, Switzerland*

³*Institut Laue-Langevin, 71 Avenue des Martyrs, 38042 Grenoble Cedex 9, France*

⁴*State Key Laboratory of Structural Chemistry, Fujian Institute of Research on the Structure of Matter, Chinese Academy of Sciences, Fuzhou, Fujian 350002, China*

⁵*Department of Physics, University of Oxford, Clarendon Laboratory, Oxford, OX1 3PU, United Kingdom*



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We present a systematic inelastic neutron scattering and neutron diffraction study on the magnetic structure of the quasi-one-dimensional spin- $\frac{1}{2}$ magnet $\text{SrCo}_2\text{V}_2\text{O}_8$, where the interchain coupling in the Néel-type antiferromagnetic ground state breaks the static spin lattice into two independent domains. At zero magnetic field, we have observed two new spin excitations with small spectral weights inside the gapped region defined by the spinon bound states. In an external magnetic field along the chain axis, the Néel order gets partially destabilized at $\mu_0 H^* = 2.0$ T and completely suppressed at $\mu_0 H_p = 3.9$ T, above which a quantum disordered Tomonaga–Luttinger liquid (TLL) prevails. The low-energy spin excitations between $\mu_0 H^*$ and $\mu_0 H_p$ are not homogeneous, containing the dispersionless (or weakly dispersive) spinon bound states excited in the Néel phase and the highly dispersive psinon-antipsinon mode characteristic of a TLL. We propose that the two new modes at zero field are spinon excitations inside the domain walls. Since they have a smaller gap than those excited in the Néel domains, the underlying spin chains enter the TLL state via a local quantum phase transition at $\mu_0 H^*$, making the Néel/TLL coexistence a stable configuration until the excitation gap in the Néel domains closes at $\mu_0 H_p$.

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I. INTRODUCTION

At the absolute zero of temperature, a continuous quantum phase transition (QPT) can occur on variation of a non-thermal control parameter—pressure, chemical substitution, magnetic field and so on—because of the fluctuations inherent in Heisenberg’s uncertainty principle, exposing a singularity called a quantum critical point (QCP) that separates the two phases involved [1]. A $T > 0$ K nonthermal phase transition can also be approximated as a QPT as long as the quantum fluctuations overwhelm the thermal fluctuations. This renders experimental assessment of quantum criticality possible [2,3]. There are, however, exceptional cases where a QCP is avoided, suppressing the otherwise prominent quantum critical dynamics near the QCP. Notably, masked quantum criticality arises in some of the most studied correlated electron systems, including the heavy-fermion metals [4,5], itinerant-electron magnets [6–8], and arguably also the high-

temperature superconductors [9,10]. As a result, classification of the phase formation in the vicinity of a QCP is at the heart of understanding the rich complexity in these materials.

A novel magnetic-field-induced QPT has been predicted to occur in the one-dimensional (1D) spin- $\frac{1}{2}$ Heisenberg–Ising XXZ model [11–13],

$$H_{XXZ} = J \sum_i (S_i^x S_{i+1}^x + S_i^y S_{i+1}^y + \Delta S_i^z S_{i+1}^z) - g_z \mu_0 \mu_B H \sum_i S_i^z, \quad (1)$$

where J is the nearest-neighbor antiferromagnetic (AFM) intrachain exchange constant, Δ is the anisotropy parameter, and g_z is the component of the Landé g tensor along the chain direction (z axis). In the Heisenberg–Ising regime ($\Delta > 1$), this model has a gapped AFM ground state of Néel type with the spins lying along the z axis [Fig. 1(a)]. An external magnetic field ($\mathbf{H} \parallel z$ axis) tunes the density of the elementary excitations (spinons [14]), acting like a chemical potential to close the gap in the excitation spectrum at a QCP that separates the Néel state from a quantum disordered Tomonaga–Luttinger liquid (TLL). A similar concept has been extensively explored in the dimerized AFMs, where the QPT is the Bose–Einstein condensation (BEC) of triplons [15,16].

Recently, the quasi-1D quantum magnet family $M\text{Co}_2\text{V}_2\text{O}_8$ ($M = \text{Sr}, \text{Ba}$), where the intrachain spin–spin interactions can be approximated by the Heisenberg–Ising

*lingjia.shen@sljus.lu.se.

†elizabeth.blackburn@sljus.lu.se.

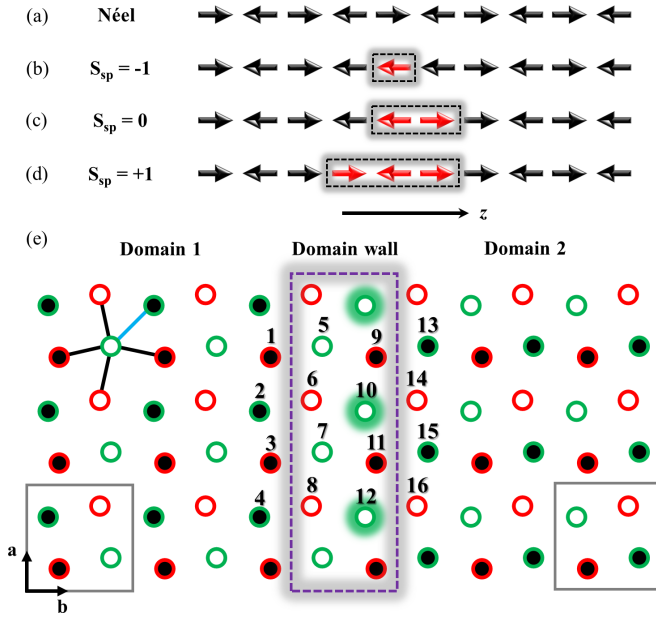


FIG. 1. Magnetic structure and spinon excitations. (a) Néel-type AFM order predicted by Eq. (1). (b–d) Spinon pairs created by spin flips (red arrows) with $S_{sp} = -1, 0, +1$, respectively. (e) In-plane magnetic structure of $\text{SrCo}_2\text{V}_2\text{O}_8$ at zero-field. There are two independent Co spin screw chains denoted by the green and red circles [25]. The filling colors (black or white) denote spin direction (up or down). Gray boxes enclose inequivalent magnetic unit cells in the two domains present, which are separated by the domain wall enclosed by the dashed purple box. The solid lines between Co sites denote the different interchain exchange paths that contribute to the local molecular field h_i at each site (blue = $\pm h_1$, black = $\pm h_2$). The glowing circles highlight spins that have been flipped by domain-wall formation. Sixteen spin sites are labeled for the $|h_s|$ analysis in Table I.

XXZ model (Eq. 1), has attracted tremendous attention [17–26]. While a magnetic-field-induced Néel to TLL phase transition has been observed at low temperatures, the magnetic structure in the QPT region has never been evaluated. This issue is important for understanding the quantum criticality in this material because Eq. (1) is not a comprehensive description for the interactions in materials of this class. In particular, it does not account for the effect of dimensional crossover that becomes energetically relevant while approaching $T = 0$ K. In this study, we used neutron diffraction and inelastic neutron scattering (INS) to measure the magnetic structure of $\text{SrCo}_2\text{V}_2\text{O}_8$ in the zero-field Néel state and across the field-induced Néel to TLL QPT. The spinon excitations in both regions are found to be inhomogeneous. Earlier neutron diffraction work has shown that in the Néel phase, there are two magnetic domains with approximately equal populations [25]. We present a model that takes this into account to interpret our observations.

II. METHODS

Two INS experiments were performed on the cold-neutron triple-axis spectrometer, ThALES, at the Institut Laue-Langevin (ILL). A cylindrical $\text{SrCo}_2\text{V}_2\text{O}_8$ single crystal

(height: 22 mm, diameter 6 mm, mass: 2.699 g) grown in Oxford (UK) by the floating zone method [27] was used. In the first experiment [28], it was mounted in a dilution refrigerator inside a 6 T horizontal cryomagnet. The initial and final neutron wave vectors were selected using a Si (111) monochromator and analyzer, respectively. The INS spectra at momentum transfers with a finite out-of-plane component were collected in this setup with a fixed final wave vector of 1.5 \AA^{-1} . In the second experiment [29], it was mounted in a dilution refrigerator inside a 10 T vertical cryomagnet. The initial and final neutron wave vectors were selected using a PG (002) monochromator and analyzer, respectively. The INS spectra in the reciprocal $(H, K, 0)$ plane were collected in this setup with a fixed final wave vector of 1.3 \AA^{-1} . All of the INS data presented here were measured with the c axis aligned along the magnetic field.

The single-crystal neutron diffraction measurements for the magnetic structure refinement at 3.0 T and 50 mK were performed on the thermal neutron diffractometer ZEBRA at the Swiss Spallation Neutron Source (SINQ) at the Paul Scherrer Institute. A $\text{SrCo}_2\text{V}_2\text{O}_8$ single crystal ($\sim 3 \times 3 \times 6 \text{ mm}^3$) grown in Fujian (China) by the spontaneous nucleation method [30] was measured with a lifted detector (normal beam geometry). It was mounted in a dilution refrigerator inside a 6 T vertical cryomagnet with the c axis aligned along the magnetic field. For the magnetic structure determination, a set of magnetic and nuclear reflections were collected at neutron wavelength $\lambda = 1.178 \text{ \AA}$ using a Ge (311) monochromator. We have also performed additional measurements on the same crystal on the D10 diffractometer (ILL) [31] in order to search for the possible emergent spin modulation between 2.0 and 3.9 T (see Section V and Supplemental Material [32]). The sample was mounted in a dilution refrigerator inside a 6 T horizontal cryomagnet. A vertically focusing graphite monochromator was used, fixing the wavelength of the incoming neutrons to $\lambda = 2.36 \text{ \AA}$.

The quality of the two single crystals was checked by neutron Laue diffraction; no impurity could be resolved. In addition, they share identical magnetic field versus temperature phase diagram within the detection limit {see Fig. S1(a) in the Supplemental Material [32]}. Unless otherwise stated, the data presented in the main text below are based on the measurements on the sample grown by floating zone [27].

III. MAGNETIC DIMENSIONAL CROSSOVER IN $\text{SrCo}_2\text{V}_2\text{O}_8$

In this section, we discuss the impact of dimensional crossover on the spin excitations based on a minimal model that approximates the interchain exchange interactions in $\text{SrCo}_2\text{V}_2\text{O}_8$. This model will be used to understand the experimental observations presented in the following sections.

The elementary excitations in a spin- $\frac{1}{2}$ AFM chain are spin- $\frac{1}{2}$ spinons [14], which can be thought of as quasiparticles that are always created or annihilated in pairs by spin flips. Consequently, each spinon pair has a bosonic quantum spin number of $S_{sp} = +1, -1$ or 0, depending on the number and direction of spin flips [Figs. 1(b)–1(d)]. Fundamentally, the zero-field excitation gap in the Néel state is determined by the doubly degenerate $S_{sp} = \pm 1$ spinon pairs; the condensation of

the $S_{\text{sp}} = +1$ branch at the QCP drives the Néel to TLL QPT in Eq. 1. As a result, the spinon dynamics are pivotal to the location of a QCP.

The dimensional crossover brought about by lowering the temperature in a quasi-1D magnet introduces additional interchain couplings. Unlike the intrachain counterparts, these terms are perturbative and can be treated in a mean-field approximation [33–35]. Specifically, their contributions can be modeled by adding an effective staggered magnetic-field $h_s(-1)^j$ to the ij spin in a single XXZ chain [Eq. (1)]. In the absence of interchain couplings, it costs the same energy to flip an arbitrary number of spins, meaning that spinon pairs propagate freely along the chain, giving a continuous excitation spectrum. When h_s is nonzero, flipping n spins in one chain leads to an additional energy gain that is proportional to nh_s . This is equivalent to putting the spinon pairs in an attractive potential, confining them spatially [36]. Confinement replaces the free spinon continuum with a series of discrete modes, i.e., spinon bound states [33]. In the $M\text{Co}_2\text{V}_2\text{O}_8$ ($M = \text{Sr}, \text{Ba}$) family, this confinement is well described by a 1D Schrödinger equation with linear potential [19–21], the solutions of which are:

$$E_j = 2E_0 + \zeta_j h_s \left(\frac{\hbar^2}{\mu} \right)^{\frac{1}{3}}, \quad (j = 1, 2, 3\dots), \quad (2)$$

where E_0 is the free spinon excitation gap, E_j is the energy of the j th bound state, ζ_j is the j th negative zero of the Airy function, and μ is the reduced spinon mass [37,38]. Based on this equation, the zero-field $S_{\text{sp}} = \pm 1$ spinon excitation gap E_1 is proportional to h_s .

$\text{SrCo}_2\text{V}_2\text{O}_8$ possesses screw chains of Co^{2+} ions with effective spin $\frac{1}{2}$ running along the crystallographic c axis. The validity of the XXZ model [Eq. (1)] in describing the intrachain interactions in this system has been confirmed by multiple experimental studies [21,22,26]. On cooling, the Co^{2+} spins develop a 3D ordered AFM structure at $T_N = 5.0$ K [25]. In the ground state, the spin configuration within each chain agrees well with the easy-axis Néel order depicted in Fig. 1(a). The relative spin alignment between two neighboring chains is not trivial. This is due to the symmetry reduction associated with the bulk AFM phase transition at T_N , which decouples half of the spin chains from the rest. The resulting spin arrangements in a given ab plane are shown in Fig. 1(e). Each in-plane magnetic unit cell hosts two diagonal AFM spin pairs that are independent of each other. This generates two types of domains, distinguished by their magnetic unit cell configurations, which are almost equally populated in space [25]. We note that this two-domain configuration in $\text{SrCo}_2\text{V}_2\text{O}_8$ is exclusively caused by the symmetry reduction in the Néel state, not by the minimization of magnetostatic energy. The latter is responsible for the formation of conventional domains.

The inhomogeneous spin lattice discussed above is not thermally activated and therefore can persist down to zero temperature. We now analyze its influence on the spinon excitations. Based on a structural analysis [39], the interchain exchange network in $\text{SrCo}_2\text{V}_2\text{O}_8$ contains four independent paths: Two in the skewing direction and the other two in the ab plane. For simplicity, we only consider the two in-plane

TABLE I. Spatial distribution of the effective staggered magnetic field h_s in the bulk Néel state. Only the in-plane interchain couplings marked in Fig. 1(e) are considered.

$ h_s $	$ h_1 $	$ h_1 - 2h_2 $	$ h_1 + 2h_2 $
Site label	1-4, 5, 7, 10, 12, 13-16	6, 8	9, 11

interchain couplings, the effective molecular fields of which are denoted as $\pm h_1$ and $\pm h_2$. Their signs depend on whether the relevant spin pairs are antiferromagnetically (minus) or ferromagnetically (plus) aligned. For a given Co site, five neighboring spins are involved [Fig. 1(e)]. The total effective staggered magnetic-field h_s is obtained by summing up these individual molecular fields [34,35].

We have calculated the $|h_s|$ values for the 16 spin sites labeled in Fig. 1(e); their spatial distribution is summarized in Table I. For any given spin inside the domains, e.g. spin # 1-4, $|h_s|$ is always equal to h_1 . However, inside the domain walls, which are formed by planes of spin chains in three dimensions, h_s is nonuniform. For example, for spin # 5 it is h_1 , for spin # 6 it is $|h_1 - 2h_2|$, and for spin # 9 it is $|h_1 + 2h_2|$. Moreover, even after the two skewing paths are included for a comprehensive analysis on the interchain exchange network [39], we find that the nonuniformity of h_s is still discrete. In other words, there exists well-defined spinon bound states corresponding to a finite set of $|h_s|$ values [34]. Accordingly, our simplified model captures the essential information: The spinon excitations in the domain walls have distinct gap values [Eq. (2)] from those in the domains because of variations in the confining potential.

IV. RESULTS

A. Domain-wall spinon excitations in $\text{SrCo}_2\text{V}_2\text{O}_8$

In Fig. 2, INS spectra as a function of momentum transfer \mathbf{Q} and neutron energy loss E are presented. As expected [33], a series of discrete modes—the spinon bound states—are seen. Figures 2(a)–2(c) show the behavior at the in-plane nuclear zone center $\mathbf{Q}_1 = (2, 2, 0)$, the AFM zone center ($\text{H} + \text{K} + \text{L} = \text{odd integer}$) $\mathbf{Q}_2 = (2, 3, 0)$, and a dispersion map of the magnetic excitations in the reciprocal $(2, \text{K}, 0)$ plane. A series of peaks are observed. To quantitatively analyze our data, we fit them numerically. The instrumental resolution function, which has a full width at half maximum (FWHM) of $88(3) \mu\text{eV}$, has been deconvolved. We have also evaluated the detection noise by conducting measurements at several momentum transfer points where there are negligible sample contributions; these calibrations show that the background may be modeled as a constant term. In the literature, a Gaussian model, where all peaks share a common width, has been used to describe the lineshape of the spinon bound states [19,21,26]. For our high-energy resolution data, we find that modeling the peaks with a damped harmonic oscillator (DHO), the width of which depends on whether the corresponding spinon bound state has $S_{\text{sp}} = \pm 1$ or 0, provides considerably better fitting quality [Figs. 2(a) and 2(b)]. This high-energy resolution is necessary to resolve these subtle features because once we relax the resolution FWHM to $160(8) \mu\text{eV}$, the DHO / 2-width and Gaussian / 1-width

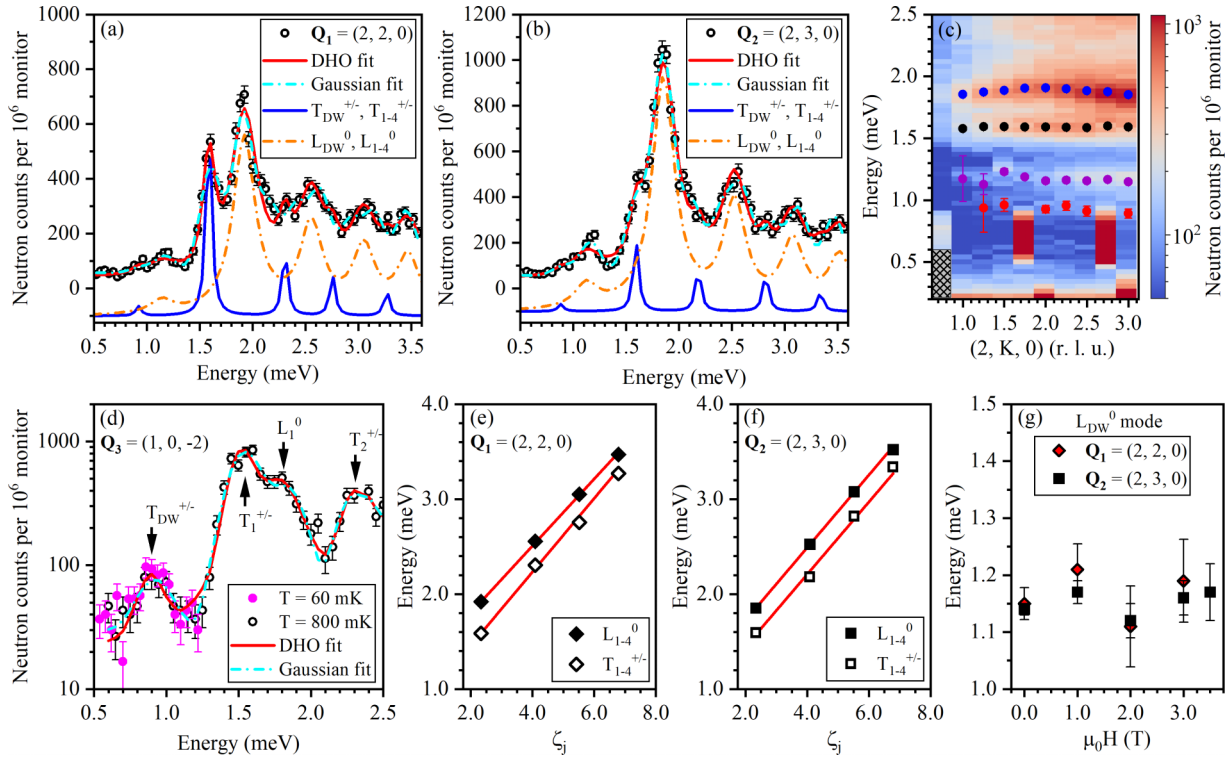


FIG. 2. Spinon confinement in $\text{SrCo}_2\text{V}_2\text{O}_8$. (a–c) Spinon bound states at 50 mK measured by INS at the momentum transfers $\mathbf{Q}_1 = (2, 2, 0)$ and $\mathbf{Q}_2 = (2, 3, 0)$ and their dispersion in the reciprocal $(2, K, 0)$ plane. In the $T_{\text{DW}}^{+/-} / T_{1-4}^{+/-}$ (blue solid line) and $L_{\text{DW}}^0 / L_{1-4}^0$ (orange dash-dotted line) plots, the instrumental resolution profile has been deconvolved to show the intrinsic damping of these modes. The $T_{\text{DW}}^{+/-}$ (red circles), L_{DW}^0 (purple circles), $T_{1-4}^{+/-}$ (black circles), and L_{1-4}^0 (blue circles) mode energies are plotted in (c), where the right” areas around 0.75 meV and at $K = 0.75, 1.75,$ and 2.75 r.l.u. are spurious leaks through the analyzer; they were excluded in our data analysis. (d) Spinon bound states at 60 mK (800 mK) and $\mathbf{Q}_3 = (1, 0, 2)$, displayed on a logarithmic scale to highlight the $T_{\text{DW}}^{+/-}$ mode. (e, f) Comparing the central energies of the domain spinon bound states with the linear confinement theory described by Eq. (2). (g) Magnetic-field dependence of the L_{DW}^0 mode energy at \mathbf{Q}_1 and \mathbf{Q}_2 . The numerical fits are described in the main text.

models produce similar fitting quality; a typical example is demonstrated in Fig. 2(d) for the spectrum collected at another AFM zone center $\mathbf{Q}_3 = (1, 0, 2)$.

In Figs. 2(a) and 2(b), the four pairs of spinon bound states above 1.40 meV with strong spectral weights, which are excited inside the Néel domains, have been reported in the literature [21,22,26]. The $S_{\text{sp}} = 0$ and ± 1 modes account for the magnetic moment fluctuations along the c axis (longitudinal, or L , mode) and in the ab plane (transverse, or T , modes), respectively [40,41]. Since neutron scattering is only sensitive to the spin configuration perpendicular to \mathbf{Q} and the Néel order is dominated by the Ising-like easy axis anisotropy along the c axis [25], the four strong peaks (orange dash-dotted line) detected in this in-plane geometry are the $S_{\text{sp}} = 0$ spinon bound states, while the four weaker ones (blue solid line) are the $S_{\text{sp}} = \pm 1$ spinon bound states. These modes are either weakly dispersive with a bandwidth of about 0.05 meV or dispersionless, supporting the hypothesis of insignificant interchain spinon correlations.

We also observe a previously unreported pair of peaks with small spectral weights at about 0.88 and 1.15 meV [Figs. 2(a)–2(c)]. Their central energies lie in the gapped region of the aforementioned bulk spinon spectrum. Their evolution in the \mathbf{Q} - E space is reminiscent of the other spinon modes at higher energies: (1) They are nondispersive in the

transverse direction, and (2) the peak at 0.88 meV is less intense than that at 1.15 meV. We interpret these peaks as another $S_{\text{sp}} = \pm 1$ (~ 0.88 meV) and 0 (~ 1.15 meV) pair. In Fig. 2(g) we track the ~ 1.15 meV mode as a function of magnetic field and see no shift, indicating that it behaves like a $S_{\text{sp}} = 0$ longitudinal mode. Due to the small spectral weight we were not able to track the ~ 0.88 meV mode in a magnetic field; if it is an $S_{\text{sp}} = \pm 1$ mode, it should show a Zeeman splitting. As an alternate way of testing this assignment, we also measured the same energy range at $\mathbf{Q}_3 = (1, 0, 2)$. In this out-of-plane geometry, we should be more sensitive to the $S_{\text{sp}} = \pm 1$ modes than to the $S_{\text{sp}} = 0$ mode [19,21]. As Fig. 2(d) shows, this is exactly what is seen both for the new peaks at 0.88 and 1.15 meV (below the detection limit in this geometry) and for the well-studied modes between 1.40 and 1.95 meV. This measurement strongly supports the $S_{\text{sp}} = \pm 1$ nature of the peak at 0.88 meV.

Trivial explanations for the two weak peaks below 1.40 meV include crystalline mosaicity and impurity. The first can be easily ruled out because the zone centers probed (\mathbf{Q}_1 , \mathbf{Q}_2 and \mathbf{Q}_3) correspond to the energy minima of the spinon spectrum [21,26]. In the absence of strong in-plane dispersion [Fig. 2(c)] [21], any secondary misaligned crystal of $\text{SrCo}_2\text{V}_2\text{O}_8$ can only add spectral weights to higher energies. On the other hand, given that only a few compounds have been

experimentally confirmed to host a well-defined $S_{sp} = 0$ mode [19,21], it is very difficult to reconcile with the presence of such mode in a random impurity phase.

In theory, the lowest-lying spinon bound state should mostly consist of one-spin flips [Fig. 1(b)] and should always have the largest spectral weight [21,33]. Accordingly, the peaks at 0.88 and 1.15 meV do not come from the bulk Néel domains, which give rise to the stronger peaks at higher energies [21]. Following the discussion in Section III and given that INS is a powerful technique for detecting solitonlike excitations with a small volume fraction [42,43], we therefore propose that they are in fact the lowest-lying spinon bound states in the domain walls. This naturally explains their much smaller spectral weights compared with those excited in the domains, as the domain walls occupy only a small portion of the sample. One necessary condition for any spinon bound state to rise in the sample is that it must be above the confinement threshold $2E_0$ (Eq. 2). We have calculated this parameter for different S_{sp} values in $\text{SrCo}_2\text{V}_2\text{O}_8$ using the spinon bound state energies in the domains. As shown in Figs. 2(e) and 2(f), the linear confinement theory fits the data well. We obtain $2E_0 \simeq 0.68$ meV for $S_{sp} = \pm 1$ and $2E_0 \simeq 1.02$ meV for $S_{sp} = 0$. Based on this calculation, the necessary condition for spinon confinement in the domain walls is fulfilled. According to Eq. (2) and Table I, there exist multiple sets of domain-wall spinon bound states above $2E_0$ due to the nonuniformity of h_s . However, experimental detection of any of these modes above 1.4 meV is challenging due to the small spectral weights and dominant contributions from domain spinons.

We will now use the labels $T_i^{+/-}$ or L_i^0 ($i = 1-4$) to denote the i th $S_{sp} = \pm 1$ or 0 spinon bound state in the domains, and $T_{DW}^{+/-}$ or L_{DW}^0 to denote the observed $S_{sp} = \pm 1$ or 0 spinon bound state in the domain walls. The high-energy resolution INS spectroscopy data allow us to conclude that the zero-field spinon confinement in $\text{SrCo}_2\text{V}_2\text{O}_8$ is not perfect [Figs. 2(a) and 2(b)]. The inverse lifetimes of the $S_{sp} = \pm 1$ and $S_{sp} = 0$ modes extracted from the numerical fits are \mathbf{Q} independent within the errors with FWHMs of 0.06(2) and 0.25(2) meV, respectively.

B. Coexistence of Néel AFM and a TLL

We study the magnetic structure as a function of longitudinal magnetic field. The onset of the TLL state can be understood as the condensation of the spin flips responsible for the $S_{sp} = +1$ spinon pairs [see Fig. 3(a)]. This is induced by the Zeeman splitting of the transverse spinon mode in a longitudinal magnetic field and should lead to the development of a staggered ferromagnetic moment, M_c , along the c axis. We have studied this by measuring the elastic scattering signal using the energy analysis available on the ThALES three-axis cold-neutron spectrometer. Figure 3(e) shows the intensity of the Bragg reflection $\mathbf{Q}_4 = (0, 2, 0)$ as a function of magnetic field. \mathbf{Q}_4 is a nuclear zone center, as well as a ferromagnetic zone center. In Fig. 3(e) the zero-field nuclear contribution has been subtracted to give a clean probe of M_c [18,25] as a function of magnetic field. In the low-field region, the intensity scales almost linearly with magnetic field, deviating upward from $\mu_0 H^* = 1.8$ T.

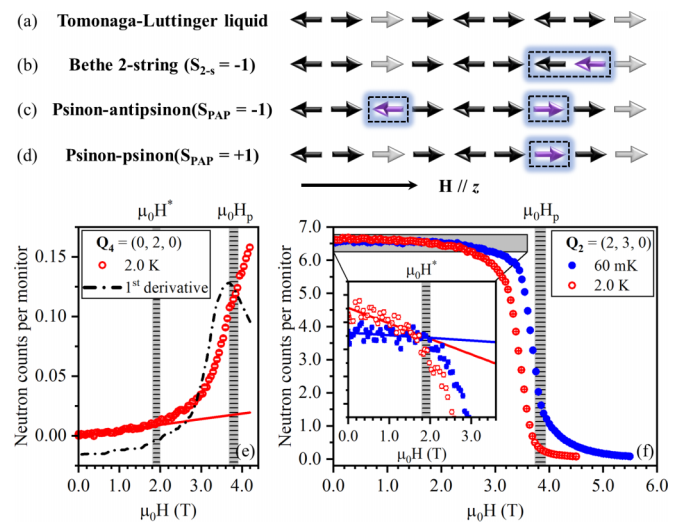


FIG. 3. Spin configurations and static magnetic properties in a field-induced TLL. (a-d) Schematic illustrations of the ground state, Bethe 2-string (2-s), psinon-antipsinon (PAP), and psinon-psinon (PP) excitations of a TLL [22,26,44]. Gray arrows represent the condensed $S_{sp} = +1$ spinon pairs in a longitudinal magnetic field. Purple arrows are spin flips responsible for the excitations. Magnetic-field dependences of the neutron diffraction intensity at (e) $\mathbf{Q}_4 = (0, 2, 0)$ and (f) $\mathbf{Q}_2 = (2, 3, 0)$, which probe the staggered ferromagnetic moment (M_c) along the chain and Néel order, respectively [25]. The nuclear structure contribution in (e) has been subtracted. The inset of (f) is an enlarged view of the shaded area in the main panel. The hatched columns mark the positions of $\mu_0 H^*$ and $\mu_0 H_p$. The dash-dotted line in (e) is the first derivative of the data (red dots). The solid lines in (e, f) are linear fits to the data points below $\mu_0 H^*$.

Figure 3(f) shows similar measurements taken at an AFM zone center, in this case $\mathbf{Q}_2 = (2, 3, 0)$. At 2.0 K and below $\mu_0 H^*$, there is a tiny linear decrease in the diffraction intensity at \mathbf{Q}_2 ; this effect is almost absent at 60 mK. These initial changes are most likely driven by thermal fluctuations. We also observe that the Néel order does not vanish until $\mu_0 H_p$ (~ 3.75 T at 2.0 K); this is the field above which $\text{SrCo}_2\text{V}_2\text{O}_8$ becomes disordered at $1.5 \text{ K} < T < T_N$. Below 1.5 K, $\mu_0 H_p$ becomes temperature independent and sits at 3.9 T. In this temperature range, a spin-density wave develops above $\mu_0 H_p$, splitting the magnetic reflection at the AFM zone centers, e.g., \mathbf{Q}_2 , into a pair of peaks along the reciprocal c^* axis. The tails of these incommensurate reflections are responsible for the remnant intensities at 60 mK and above $\mu_0 H_p$ [Fig. 3(f) and Fig. S1(b) in the Supplemental Material [32]]. These observations are in agreement with our previous study [25].

In the intermediate field region, our measurements detect a response of the \mathbf{Q}_2 reflection to $\mu_0 H^*$, above which the intensity loss accelerates [inset of Fig. 3(f)]. The $\mu_0 H^*$ value also slightly increases to 2.0 T as the temperature is lowered to 60 mK. Since the Néel order in $\text{SrCo}_2\text{V}_2\text{O}_8$ involves two unequally populated magnetic domains [25], the suppression of the \mathbf{Q}_2 reflection could be caused by a change in the domain volume fractions. A misalignment between the magnetic field and c axis [18] or equilibration difficulty at very low temperatures could also be responsible for such changes. We dismiss this possibility based on magnetic structure refinements

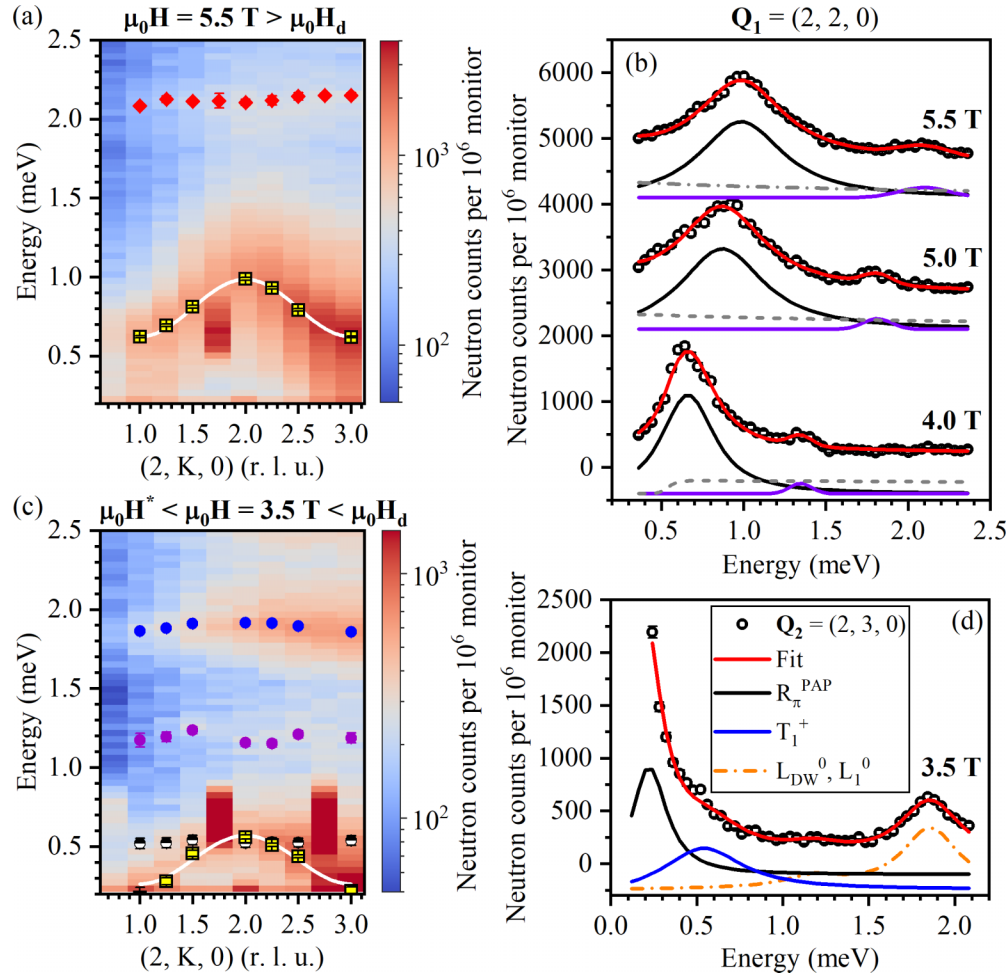


FIG. 4. Magnetic excitations in a longitudinal magnetic field. (a) Dispersion of the TLL spin dynamics in the reciprocal $(2, K, 0)$ plane at 5.5 T. The red diamonds and yellow squares mark the positions of the Bethe 2-strings (χ_{π}^{2-s}) and psinon-antipsinons (R_{π}^{PAP}), respectively. (b) Magnetic excitation spectrum at $\mathbf{Q}_1 = (2, 2, 0)$ as a function of magnetic field. The black solid, gray dashed, and violet solid lines are the numerical fits to the R_{π}^{PAP} , continuum (see the main text) and χ_{π}^{2-s} modes, respectively. (c) Dispersion of the magnetic excitations at 3.5 T, which shows the coexistence of spinon bound states [T_1^+ (black circles), L_{DW}^0 (purple solids), and L_1^0 (blue solids)] and R_{π}^{PAP} (yellow squares). (d) Magnetic excitation spectrum at $\mathbf{Q}_2 = (2, 3, 0)$ and 3.5 T. The white solid lines in (a) and (c) are sinusoidal fits. The numerical fits in (b) and (d) are described in the main text. The spectral weights at low energies in (b) and (d) contain the contributions from elastic scattering; its lineshape has been omitted for clarity. All measurements were carried out at 50 mK.

carried out on the sample grown by spontaneous nucleation [30] at 3.0 T used in Ref. [25], using 41 magnetic reflections belonging to the Néel phase (see Fig. S2 in the Supplemental Material [32]). These refinements reveal that, besides a reduction in the ordered magnetic moment at each Co site, both the magnetic structure and the volume fractions of the two domains remain unchanged relative to those measured in zero field. This rules out the domain scenario in this sample and confirms that the bulk averaged Néel order is partially suppressed between $\mu_0 H^*$ and $\mu_0 H_p$.

The kink at $\mu_0 H^*$ revealed in Fig. 3(e) supports the emergence of spin chains with a finite M_c before the Néel order is completely suppressed at $\mu_0 H_p$. While a finite M_c fits the description for having a TLL above $\mu_0 H^*$, it is *not* direct evidence. Indeed, since the slope of the diffraction intensity at \mathbf{Q}_4 peaks at $\mu_0 H_p$ [Fig. 3(e)], which probes the suppression of the bulk Néel order [Fig. 3(f)], $\mu_0 H^*$ could simply mark

the starting point of a second-order phase transition or some sort of crossover behavior. However, if we assume that a TLL emerges at $\mu_0 H^*$, the persistence of a partially suppressed Néel order up to a higher field $\mu_0 H_p$ does not agree with the expectation for a continuous QPT in a single XXZ spin- $\frac{1}{2}$ chain [11–13].

To confirm the nature of the magnetic state between $\mu_0 H^*$ and $\mu_0 H_p$, we now consider the changes seen in the INS spectra as a function of magnetic field at 50 mK. A full description of the TLL spin dynamics is now available in both theory and experiment: They consist of multiparticle excitations ranging from psinon-antipsinon and psinon-psinon pairs at low energies to Bethe strings at medium and high energies [22,24,26,44], as illustrated in Figs. 3(a)–3(d). While these modes can still be effectively described by spin flips, i.e., having a quantum spin number +1, -1, or 0 [see Figs. 3(b)–3(d)], they differ from the spinons in the Néel state in that

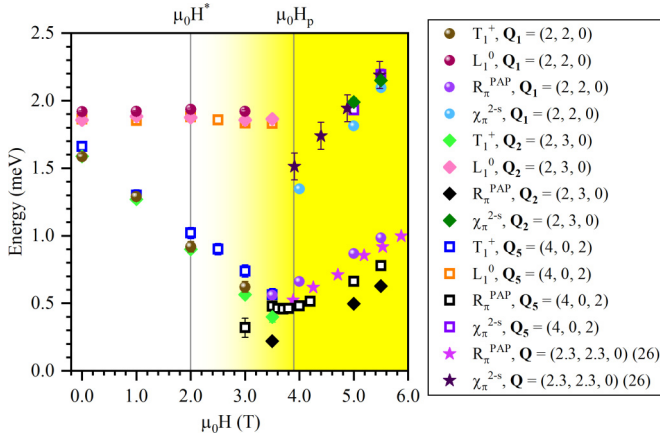


FIG. 5. Evolution of the quasiparticle excitation energies in a longitudinal magnetic field. \mathbf{Q}_1 and \mathbf{Q}_5 are nuclear zone centers; \mathbf{Q}_2 is an AFM zone center. For comparison, the data reported in Ref. [26] are also included.

they correspond to the excitations in a disordered spin- $\frac{1}{2}$ chain with $M_c \neq 0$. Figure 4(a) shows the INS spectrum in the $(2, K, 0)$ direction at 5.5 T, i.e., above $\mu_0 H_p$. All INS spectra in this region can be modeled by combining two DHOs and a product of a Lorentzian and Heaviside step function [Fig. 4(b)]. By comparing our data with the canonical observations of the TLL spin dynamics, the dominant features in the spectrum can be identified. The fourfold screw chain structure in $\text{SrCo}_2\text{V}_2\text{O}_8$ folds the Brillouin zone by a factor of four, meaning that the excitations at $L = 0, \frac{1}{4}, \frac{1}{2}$ and $\frac{3}{4}$ of a single chain can be observed simultaneously at $L = 0$ [26]. Most of the magnetic excitations in a TLL contribute to a continuum, accounting for the broad Lorentzian-Heaviside profile [45]. There are only two relatively well-defined modes that are accessible at $L = 0$ and below 2.5 meV: The psinon-antipsinon pairs at $L = \frac{1}{2}$ (R_π^{PAP}) with a quantum number $S_{\text{PAP}} = 0$ and Bethe 2-strings at $L = \frac{1}{2}$ (χ_π^{2-s}) with a quantum number $S_{2-s} = -1$. By comparing the field dependences of the two DHO centers with those reported in Ref. [26], we confirm that the profile below 1.5 meV is the R_π^{PAP} mode, while the one around 2.1 meV is the χ_π^{2-s} mode (Fig. 5). Our in-plane geometry is optimal for detecting modes with a quantum number of 0, which is consistent with the observed intense spectral weight for the $S_{\text{PAP}} = 0 R_\pi^{\text{PAP}}$ mode. A remarkable feature revealed in Fig. 4(a) is the dispersion of this mode; it is strongly softened at the AFM zone centers with a bandwidth of 0.36(1) meV, contrasting sharply with the dispersionless χ_π^{2-s} mode at higher energies. This strongly suggests that the interchain couplings must be taken into account to understand the low-energy TLL spin dynamics. With the features of the relevant TLL modes established, we now discuss the region between $\mu_0 H^*$ and $\mu_0 H_p$. In Figure 4(c), we present the magnetic excitations and their dispersion at 3.5 T, where the elastic intensity at \mathbf{Q}_2 that characterizes the Néel order is at about 83% of its zero-field value [Fig. 3(f)]. A visual inspection already reveals two strong modes: A weakly dispersive one around 1.85 meV and a strongly dispersive one with a bandwidth of 0.31(3) meV below 0.6 meV. The former is identical with the L_1^0 spinon bound state within

the errors [Fig. 2(c)], revealing the persistence of the spinon confinement in the bulk Néel domains. The latter, however, cannot be explained by any $S_{\text{sp}} = +1$ mode in the system, which is dispersionless [Fig. 2(c)] and approaches the elastic line as the magnetic field increases by gaining Zeeman energy. In fact, these spectra can be numerically reproduced by a minimal model with four modes: L_1^0 , L_{DW}^0 , T_1^+ , and, critically, a dispersive R_π^{PAP} . In these analyses, the contributions from the elastic line, which are not negligible at low energies, have been subtracted by fitting the zero-field spectrum. A typical example is demonstrated in Fig. 4(d) for the spectrum at \mathbf{Q}_2 , while we have also validated this model at \mathbf{Q}_1 and another nuclear zone center $\mathbf{Q}_5 = (4, 0, 2)$ (Fig. 5). The existence of a strongly dispersive mode can be resolved down to 3.0 T in our measurements. By evaluating its evolution as a function of magnetic field, the mode energy seamlessly connects to the $S_{\text{PAP}} = 0 R_\pi^{\text{PAP}}$ one above $\mu_0 H_p$ (Fig. 5). The field dependence and strong dispersion of the new mode below $\mu_0 H_p$ do not fit the characteristics of spinons, but are in strong agreement with the features of a R_π^{PAP} . Consequently, the most likely explanation for our observations at these intermediate magnetic fields is Néel / TLL coexistence with the TLL component accounting for the partial suppression of the bulk Néel order revealed by neutron diffraction.

C. Inhomogeneous Néel to TLL QPT

In Section III, we have argued that the chains in and close to the domain walls may have different excitation gaps from those in the domains based on a minimal model. This possibility is supported by the zero-field INS data presented in Section IV A, which show the presence of a second set of spinon excitations with a smaller gap. We have interpreted these results as the fingerprints of excitations localized inside the domain walls. Now, we use this interpretation to address the Néel / TLL coexistence phenomenon shown in Section IV B.

As noted above, the transition to the TLL state can be related to the condensation of the relevant T_1^+ mode brought about by Zeeman splitting. Figure 5 illustrates that we do not see a clear closure of the gap associated with the T_1^+ mode in the bulk of the domains. As noted earlier, the spinon confinement is not perfect in this material, and the intrinsic damping of the spinon bound states can be extracted from the FWHMs after deconvolving the instrumental resolution. The resulting spinon damping is shown in Fig. 6(a) and is enhanced in both transverse and longitudinal modes by the applied magnetic field. This finite bandwidth will lead to a smaller gap for at least part of the excitations. We have calculated the excitation gap in the domains using three different criteria: $E_1^D, E_1^D - (0.5 \times \text{FWHM})$ and $E_1^D - (1.0 \times \text{FWHM})$, where E_1^D is the central energy of the T_1^+ mode at a given magnetic field. Their magnetic-field dependences are plotted in Fig. 6(b). As in the case of the charge-density wave in NbSe_3 [46] we speculate that once sufficient spectral weight accumulates at zero energy transfer, condensation occurs. It is only by including this magnetic-field-induced spinon damping that this can be achieved at $\mu_0 H_p$ for the T_1^+ mode originating from the domains.

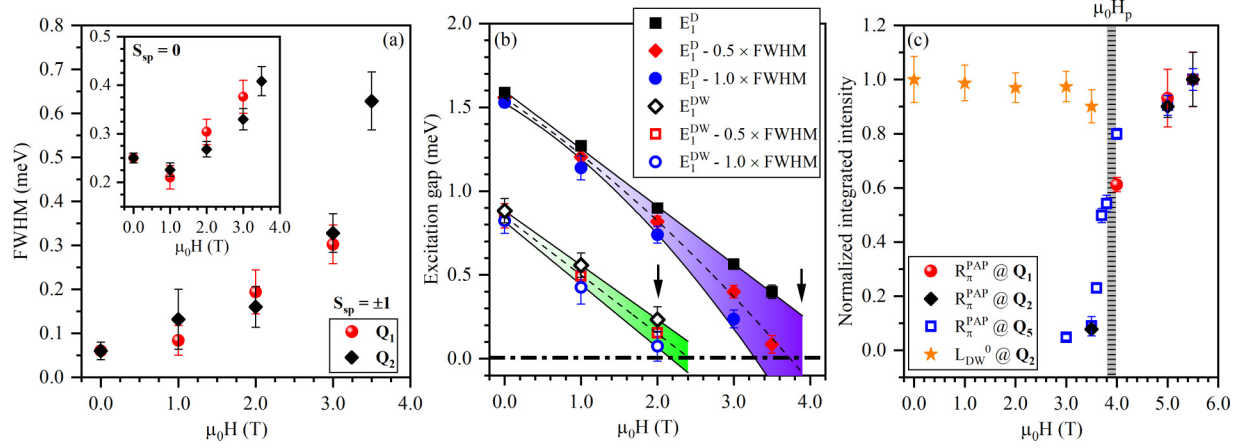


FIG. 6. Spinon damping and spatially inhomogeneous gap closure. (a) Intrinsic FWHMs of the $S_{sp} = \pm 1$ (main panel) and $S_{sp} = 0$ (inset) modes as a function of magnetic field. The instrumental resolution contribution has been deconvolved. $Q_1 = (2, 2, 0)$ and $Q_5 = (4, 0, 2)$ are nuclear zone centers; $Q_2 = (2, 3, 0)$ is an AFM zone center. (b) Estimated spinon excitation gaps in the domains (filled points) and domain walls (open points) at Q_2 as a function of magnetic field. $\mu_0 H^*$ and $\mu_0 H_p$ are marked by black arrows. The shaded areas are guides to the eye. (c) Magnetic-field dependences of the normalized integrated intensity of the R_{π}^{PAP} and L_{DW}^0 modes. The hatched column marks the position of $\mu_0 H_p$. All measurements were performed at 50 mK.

The same methodology can be applied to the transverse spinon bound state in the domain walls, the central energy of which is denoted as E_1^{DW} in Fig. 6(b). While E_1^{DW} can be unambiguously determined at zero field (Fig. 2), we were not able to directly measure its value once the magnetic field is switched on due to its marginal spectral weight. However, we can infer its behavior by invoking the general Zeeman splitting principle: $E_1^{DW}(\mu_0 H) = E_1^{DW}(0 \text{ T}) - g_c \mu_B \mu_0 H$. As shown in Fig. 5, this principle is well obeyed by the other measurable spinon bound states at higher energies. A linear fit to the T_1^+ mode energies at different Q s gives $g_c = 5.6(2)$. By further including the spinon damping effect, we find that the excitation gap of the T_{DW}^+ band at Q_2 closes near $\mu_0 H^*$ [Figs. 6(b)], above which M_c becomes nonzero [Fig. 3(e)]. Combining the elastic and INS results, we believe that the R_{π}^{PAP} mode, which can be resolved down to 3.0 T within our detection limit, originates from the local gap closure in the domain walls near $\mu_0 H^*$.

The spatially inhomogeneous QPT scenario is further backed up by the behavior of the spectral weight of the R_{π}^{PAP} mode [Fig. 6(c)]. At and below 3.5 T, it evolves smoothly and remains small. This is because the TLL at these intermediate fields is only located inside and close to the domain walls. When the excitation gap in the Néel domain begins to close, or the magnetic field approaches $\mu_0 H_p$ [Fig. 5(b)], the spectral weight shows a steplike increase, suggesting the emergence of a Néel to TLL QPT in the domains. The Néel order is completely suppressed at high fields where the spectral weight is flattened again.

V. DISCUSSION AND CONCLUSIONS

The results above support an exotic region between $\mu_0 H^*$ and $\mu_0 H_p$ where a partially suppressed Néel state coexists with the TLL. One possible mechanism for this is masked quantum criticality. This means that the Néel to TLL QPT in $\text{SrCo}_2\text{V}_2\text{O}_8$ is no longer well defined. In correlated elec-

tron systems, masked quantum criticality can occur due to the development of a competing state near the QCP [4,5]. However, after an extensive search in the reciprocal space, no emergent static spin modulation can be resolved in this region in addition to the Néel order (see Fig. S3 in the Supplemental Material [32]). As shown in Figs. 4(c) and 4(d), the dynamical spin properties in the Q - E space can also be well described by the Néel/TLL composite model. Our data therefore do not support the competing state scenario.

The persistence of the L_{DW}^0 mode up to $\mu_0 H_p$ [Figs. 1(g) and 6(c)] would seem to disagree with the domain-wall QPT scenario at $\mu_0 H^*$. This is due to the lack of significant interactions between the different spinon bound states in the low-field region where these states are relatively stable. At high fields, spinon damping becomes profound [Fig. 6(a)] promoting these interactions, such as the decay of a $S_{sp} = 0$ mode into a pair of $S_{sp} = \pm 1$ modes [47]. In fact, this echoes our argument in Section IV C that sufficient spinon damping is necessary for the Néel to TLL QPT to percolate.

In summary, we have presented neutron-scattering evidence for inhomogeneous spin excitations in the the quasi-1D quantum magnet $\text{SrCo}_2\text{V}_2\text{O}_8$, both in the zero-field Néel ground state and during the field-induced Néel to TLL QPT process. What is particularly interesting is the coexistence of partially suppressed Néel antiferromagnetism and a TLL between $\mu_0 H^* = 2.0$ T and $\mu_0 H_p = 3.9$ T, which supports the hypothesis of masked quantum criticality in this system. Masked quantum criticality is an important concept in correlated electron systems, contributing to some of the most intricate states of matter observed therein [4–10]. Spatial confinement, i.e., dimensionality control, of particles is a well-established tool for tuning the quantum phases; paradigmatic examples can be found in systems like ultracold atoms [48,49] and superfluid ^4He in porous media [50]. Unlike these studies where the confining potential is extrinsic, our work

highlights an intrinsic mechanism for confinement, i.e., dimensional crossover, that can be used to explore the quantum magnetism in relevant materials.

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