## Lund University

# Mirror symmetry at mass $\mathrm{A}=54$ : E4 effective charges near doubly magic ${ }^{56} \mathrm{Ni}$ 

Rudolph, D.; Blank, B.; Giovinazzo, J.; Roger, T.; Alvarez-Pol, H.; Arokia Raj, A.; Ascher, P.; Caamaño-Fresco, M.; Caceres, L.; Cox, D.M.; Fernández-Domínguez, B.; Lois-Fuentes, J.; Gerbaux, M.; Grévy, S; Grinyer, G.F.; Kamalou, O.; Mauss, B.; Mentana, A.; Pancin, J.; Pibernat, J.; Piot, J.; Sorlin, Olivier; Stodel, C.; Thomas, J.-C.; Versteegen, M.<br>Published in:<br>Physics Letters B

DOI:
10.1016/j.physletb.2022.137144

2022

Document Version:
Publisher's PDF, also known as Version of record
Link to publication

Citation for published version (APA):
Rudolph, D., Blank, B., Giovinazzo, J., Roger, T., Alvarez-Pol, H., Arokia Raj, A., Ascher, P., Caamaño-Fresco, M., Caceres, L., Cox, D. M., Fernández-Domínguez, B., Lois-Fuentes, J., Gerbaux, M., Grévy, S., Grinyer, G. F., Kamalou, O., Mauss, B., Mentana, A ${ }_{56}$ Pancin, J., ... Versteegen, M. (2022). Mirror symmetry at mass A=54: E4 effective charges near doubly magic ${ }^{56}$ Ni. Physics Letters B, 830, Article 137144.
https://doi.org/10.1016/j.physletb.2022.137144
Total number of authors:
25

Creative Commons License:
CC BY

## General rights

Unless other specific re-use rights are stated the following general rights apply:
Copyright and moral rights for the publications made accessible in the public portal are retained by the authors
and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the
legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal

Read more about Creative commons licenses: https://creativecommons.org/licenses/

## Take down policy

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

# Mirror symmetry at mass $A=54$ : $E 4$ effective charges near doubly magic ${ }^{56} \mathrm{Ni}$ 

D. Rudolph ${ }^{\text {a,* }, ~ B . ~ B l a n k ~}{ }^{\text {b }}$, J. Giovinazzo ${ }^{\text {b }}$, T. Roger ${ }^{\text {c }}$, H. Alvarez-Pol ${ }^{\text {d }}$, A. Arokia Raj ${ }^{\text {e }}$, P. Ascher ${ }^{\text {b }}$,<br>M. Caamaño-Fresco ${ }^{\text {d }}$, L. Caceres ${ }^{\text {c }}$, D.M. Cox ${ }^{\text {a }}$, B. Fernández-Domínguez ${ }^{\text {d }}$, J. Lois-Fuentes ${ }^{\text {d }}$, M. Gerbaux ${ }^{\text {b }}$,<br>S. Grévy ${ }^{\text {b }}$, G.F. Grinyer ${ }^{\mathrm{f}}$, O. Kamalou ${ }^{\text {c }}$, B. Mauss ${ }^{\text { }}$, A. Mentana ${ }^{\text {e }}$, J. Pancin ${ }^{\text {c }}$, J. Pibernat ${ }^{\text {b }}$, J. Piot ${ }^{\text {c }}$, O. Sorlin ${ }^{\text {c }}$,<br>C. Stodel ${ }^{\text {c }}$, J.-C. Thomas ${ }^{\text {c }}$, M. Versteegen ${ }^{\text {b }}$<br>${ }^{a}$ Department of Physics, Lund University, SE-22100 Lund, Sweden<br>${ }^{b}$ Centre d'Etudes Nucléaires de Bordeaux Gradignan, UMR 5797 CNRS/IN2P3 - Université de Bordeaux, F-33175 Gradignan Cedex, France<br>${ }^{c}$ Grand Accélérateur National d'Ions Lourds, CEA/DRF-CNRS/IN2P3, F-14076 Caen Cedex, France<br>${ }^{d}$ IGFAE and Dpt. de Física de Partículas, Universidade de Santiago de Compostela, E-15758 Santiago de Compostela, Spain<br>${ }^{e}$ Instituut voor Kern- en Stralingsfysica, KU Leuven, B-3001 Leuven, Belgium<br>${ }^{f}$ Department of Physics, University of Regina, Regina, Saskatchewan S4S 0A2, Canada<br>${ }^{g}$ RIKEN Nishina Center, Wako, Saitama 351-0198, Japan

## Abstract

## Supplemental Material

Reference numbers relate to the main article

End of June 2022 we realized that the convergence of a subset of KB3GR-based ANTOINE calculations for solely the yrast $I^{\pi}=8^{+}$state was incorrect. This implies that the following four modifications were implemented in this updated version of the Supplemental Material, which was made available online about July 10, 2022:

1. KB3GR-entry for the $B\left(E 2 ; 10^{+} \rightarrow 8^{+}\right)$value in Table 1 changed from 0.001 to 1.92 W.u.
2. The level energy predicted for the $I^{\pi}=8^{+}$state in the KB3GR-column in Fig. 1 was changed from 6949 to 6715 keV .
3. In Fig. 2(b), the data point for the $I^{\pi}=8^{+}$state of the $V_{C M}+V_{C \ell s}+V_{C \ell \ell}+V_{B: J}+V_{C p 3}$ parametrization (dot dashed, red) changed from -182 to +117 keV .
4. In Fig. 2(b), the data point for the $I^{\pi}=8^{+}$state of the $V_{C M}+V_{C \ell s}+V_{C \ell \ell}+V_{B: 4 x 0}+V_{C p}$ parametrization (dot-dot dashed, green) changed from -191 to +116 keV .

Clearly, a more consistent picture arises when comparing the KB3GR predictions with those of the other interactions. We apologize for any inconvience or headache caused by the four faulty values presented earlier.

Note that neither text nor Fig. 2(e) of the main article are concerned.

DR would like to thank Silvia M. Lenzi for detailed discussions.

[^0]Table 1: Reduced transition strengths, $B(E 2)$, in W.u., for decays of states in ${ }^{54} \mathrm{Fe}$ calculated with several $f p$-shell interactions and for various restricted numbers, $t$, of particles allowed to cross the shell gap at particle numbers $N, Z=28$. The electric quadrupole and magnetic dipole moments of the $I^{\pi}=10^{+}$isomer are listed as well. For all calculations, $\varepsilon_{\pi}=1.15$ and $\varepsilon_{v}=0.80[11]$ and free $g$ factors were used.

| observable | exp |  | GXPF1A [34] |  |  |  |  |  |  | FPD6 | KB3G | KB3 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $[15]$ |  |  |  |  |  | KB3GR |  |  |  |  |  |
|  |  | $t=2$ | $t=4$ | $t=8$ | $t=10$ | full | $t=6$ | $t=6$ | $t=6$ | $t=6$ | $t=6$ |  |
| $B\left(E 2 ; 2^{+} \rightarrow 0^{+}\right)$ | $11.1(3)$ | 5.13 | 7.56 | 9.49 | 9.75 | 9.56 | 9.14 | 11.8 | 7.57 | 6.76 | 9.29 |  |
| $B\left(E 2 ; 6^{+} \rightarrow 4^{+}\right)$ | $3.25(5)$ | 2.38 | 2.88 | 3.06 | 3.05 | 3.04 | 2.99 | 3.50 | 2.83 | 2.67 | 3.42 |  |
| $B\left(E 2 ; 10^{+} \rightarrow 8^{+}\right)$ | $1.70(3)$ | 1.99 | 2.05 | 2.05 | 2.01 | 2.00 | 1.98 | 2.31 | 2.05 | 2.16 | 1.92 |  |
| $Q\left(10^{+}\right)\left(\mathrm{efm}^{2}\right)$ | $52(8)$ | 45.9 | 56.6 | 59.3 | 59.6 | 59.6 | 59.3 | 59.9 | 54.5 | 54.8 | 56.6 |  |
| $\mu\left(10^{+}\right)\left(\mu_{N}^{2}\right)$ | $7.281(10)$ | 6.98 | 7.14 | 7.19 | 7.19 | 7.19 | 7.19 | 7.54 | 6.77 | 6.68 | 6.92 |  |

Table 2: Modifications of proton, $\pi$, and neutron, $v$, single-particle energies, $\varepsilon$, due to isospin-symmetry breaking terms. See main text for definitions and Refs. [1,3,4] for further details. Values used in the KB3G (and KB3G56) shell-model calculations are provided for reference. All numbers are

| in keV . |  |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| term | $\Delta \varepsilon_{v}\left(f_{7 / 2}\right)$ | $\Delta \varepsilon_{v}\left(p_{3 / 2}\right)$ | $\Delta \varepsilon_{v}\left(p_{1 / 2}\right)$ | $\Delta \varepsilon_{v}\left(f_{5 / 2}\right)$ | $\Delta \varepsilon_{\pi}\left(f_{7 / 2}\right)$ | $\Delta \varepsilon_{\pi}\left(p_{3 / 2}\right)$ | $\Delta \varepsilon_{\pi}\left(p_{1 / 2}\right)$ | $\Delta \varepsilon_{\pi}\left(f_{5 / 2}\right)$ |
| $V_{C \ell s}[4]$ | +49 | +16 | -31 | -65 | -59 | -19 | +37 | +78 |
| $V_{C C}[4]$ | 0 | 0 | 0 | 0 | 0 | -300 | -475 | -210 |
| $V_{C r}^{\prime}$ | 0 | 0 | 0 | 0 | 0 | -400 | -575 | -210 |
| $V_{C \ell \ell}[3]$ | 0 | 0 | 0 | 0 | -45 | +105 | +105 | -45 |
| interaction | $\varepsilon_{v}\left(f_{7 / 2}\right)$ | $\varepsilon_{v}\left(p_{3 / 2}\right)$ | $\varepsilon_{v}\left(p_{1 / 2}\right)$ | $\varepsilon_{v}\left(f_{5 / 2}\right)$ | $\varepsilon_{\pi}\left(f_{7 / 2}\right)$ | $\varepsilon_{\pi}\left(p_{3 / 2}\right)$ | $\varepsilon_{\pi}\left(p_{1 / 2}\right)$ | $\varepsilon_{\pi}\left(f_{5 / 2}\right)$ |
| KB3G | 0 | 2000 | 4000 | 6500 | 0 | 2000 | 4000 | 6500 |
| $\quad+V_{C \ell s}$ | 49 | 2016 | 3969 | 6435 | -59 | 1981 | 4037 | 6578 |
| $\quad+V_{C C s}+V_{C r}$ | 49 | 2016 | 3969 | 6435 | -59 | 1681 | 3562 | 6368 |
| $\quad+V_{C \ell s}+V_{C \ell \ell}$ | 49 | 2016 | 3969 | 6435 | -104 | 2086 | 4142 | 6533 |
| $\quad+V_{C \not s}+V_{C \ell \ell}+V_{C r}^{\prime}$ | 49 | 2016 | 3969 | 6435 | -104 | 1686 | 3567 | 6323 |
| KB3G56 | 300 | 2000 | 4000 | 6500 | 300 | 2000 | 4000 | 6500 |
| $\quad+V_{C \ell s}+V_{C r}$ | 349 | 2016 | 3969 | 6435 | 241 | 1681 | 3562 | 6368 |



Figure 1: Calculated level energies of selected yrast states of ${ }^{54} \mathrm{Fe}$ for several common $f p$-space interactions. On the left, they are shown as a function of truncation of the full $f p$ model space exemplified for GXPF1A [34]; $t=2,4,6,8,10$ particles are allowed to cross the shell gap at particle number $N=Z=28$, as well as an unrestricted calculation. Truncated at the $t=6$ level, predictions of FPD6 [40], KB3G [35,36], KB3 [37,38], KB3GR [39], and the present KB3G56 are shown on the right.


Figure 2: Mirror-energy differences (MED) between excited states in ${ }^{54} \mathrm{Ni}$ and ${ }^{54} \mathrm{Fe}$. The selection of sums of isospin-breaking terms is identical to Fig. 2(d) (KB3G [35,36]) of the main article, but for three other underlying $f p$ shell-model interactions: KB3G56 in panel (a), KB3GR [39] in panel (b), and GXPF1A [34] in panel (c), always compared with the experimental values (filled circles, cf. Fig. 1 main article). As pointed out in the main article, rather independent of the specific interaction, the sums $V_{C M}+V_{C \ell s}+V_{C r}+V_{B: 2}$ (solid, indigo) and $V_{C M}+V_{C \ell s}+V_{C \ell \ell}+V_{C r}^{\prime}+V_{B: 2}$ (dashed, magenta) provide good to very good descriptions of the observed MED. At variance, attempts using ISB corrections based on $p$--orbital occupation numbers fail; $V_{C M}+V_{C \ell s}+V_{C \ell \ell}+V_{B: 4 x 0}+V_{C p}$ (dot-dot dashed, green) or $V_{C M}+$ $V_{C \ell s}+V_{C \ell \ell}+V_{B: J}+V_{C p 3}$ (dot dashed, red). See main article for details and definitions.


[^0]:    ${ }^{*}$ Corresponding author.
    E-mail address: Dirk.Rudolph@nuclear.lu.se

