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PO Box 117 221 00 Lund +46 46-222 00 00

Attosecond photoionization dynamics with stimulated core-valence transitions

Jhih-An You,^{1,2,3} Nina Rohringer,^{1,2,3,*} and Jan Marcus Dahlström^{1,2,4,†}

¹Center for Free-Electron Laser Science, Luruper Chaussee 149, 22761 Hamburg, Germany

²Max Planck Institute for the Physics of Complex Systems, Noethnitzerstrasse 38, 01187 Dresden, Germany

³Max Planck Institute for the Structure and Dynamics of Matter, Luruper Chaussee 149, 22761 Hamburg, Germany

⁴Department of Physics, Stockholm University, AlbaNova University Center, SE-106 91 Stockholm, Sweden

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We investigate ionization of neon atoms by an isolated attosecond pump pulse in the presence of two coherent extreme ultraviolet or x-ray probe fields. The probe fields are tuned to a core-valence transition in the residual ion and induce spectral shearing of the photoelectron distributions. We show that the photoelectron-ion coincidence signal contains an interference pattern that depends on the temporal structure of the attosecond pump pulse and the stimulated core-valence transition. Many-body perturbation theory is used to compute "atomic response times" for the processes and we find strikingly different behavior for stimulation to the outer-core hole $(2p \leftrightarrow 2s)$ and stimulation to the inner-core hole $(2p \leftrightarrow 1s)$. The response time of the inner-core transition is found to be comparable to that of state-of-the-art laser-based characterization techniques for attosecond pulses.

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I. INTRODUCTION

Atoms and molecules are today routinely probed and controlled on the atomic time scale in various branches of attophysics [1]. Tailored laser fields are used to control electron trajectories and to probe high-order harmonic generation (HHG) [2,3]. The combination of phase-locked attosecond (as) extreme ultraviolet (XUV) pulses and femtosecond (fs) infrared (IR) laser fields has found numerous applications: The IR-field can act as an intense probe to break chemical bonds [4] or map time into frequency space by the so-called attosecond streaking techniques [5-8]. Alternatively, the XUV pulse can act as a probe to study electron-hole dynamics by transient absorption techniques [9-11]. XUV and x-ray freeelectron lasers (FELs) [12–15] are accelerator-based sources that provide pulses of fs duration with peak powers reaching the gigawatt (GW) range. The capabilities of these new sources are rapidly evolving, including the demonstration of wavelength-tunable pulse pairs [16–18] and spectral-temporal pulse shaping by seeded FELs [19], with possible production of GW-as pulses [20-23]. Diverse fs pump-probe schemes at FELs led to groundbreaking experiments in chemical-reaction dynamics [24-27] and the extension of these techniques to the as time scale could open new avenues for the observation and control of electron dynamics. Attosecond pulses have mainly been characterized using streak-camera techniques [5-7], or interferometric techniques [28-30], where photoelectrons are treated as "replicas" of the corresponding attosecond pulses that are controlled by a phase-locked optical laser field. The implementation of such techniques at FELs is cumbersome due to challenges of synchronization of FEL pulses to optical lasers [31,32]. Furthermore, recent difference measurements of photoelectrons resulting from different atomic initial states have evidenced that such XUV-IR schemes, which rely on laser-driven photoelectron dynamics, suffer from uncertainties on the order of tens of attoseconds [8,33].

This article explores the possibilities to exert control of a photoelectron without laser-electron continuum interaction. To this end, we study a process where an isolated XUV-as pulse ejects an electron from neon, while a pair of XUV (or x-ray) probe fields drives a transition in the ion. The probe fields are tuned to predominately stimulate hole transitions rather than electron continuum dynamics. A small red and blue detuning of the probe fields relative to the resonant hole transition is used to induce spectral shearing of the photoelectron replica to lower and higher kinetic energies, respectively. The shearing process is illustrated under pathway (S+) in Fig. 1(a) relative to (1), the unshifted one-photon ionization process. This opens the way for a different control scheme of the final electron energy by *indirect* interaction with the probe fields via the hole in the remaining ion Interestingly, we show that correlation between the electron and the hole is not required to explain the mechanism and that the process can be described within the independent-particle approximation.

The paper is organized as follows. In Sec. II we introduce the proposed scheme and outline our primary theoretical method for the study, which is based on a one-dimensional model of the neon atom. In Sec. III we present our main results for the time-dependent one-dimensional model (Sec. III A) and give an interpretation of the result using three-dimensional perturbation theory (Sec. III B). In Sec. IV we discuss our results and give an outlook for experimental realization of the scheme. Finally, in Sec. V we present our conclusions.

II. METHOD

As illustrated in Fig. 1(a), we consider photoionization by an isolated XUV-as pulse in the presence of two coherent XUV (or x-ray) probe fields. The complex XUV amplitude of the incoming field on the neon atom written as (atomic units, $\hbar = e = m = 4\pi\epsilon_0 = 1$, are used unless otherwise stated)

$$E(\omega) = E_1(\omega) + E_2\delta(\omega - \omega_2) + E_3\delta(\omega - \omega_3), \qquad (1)$$

where the pump amplitude is $E_1(\omega) = |E_1(\omega)| \exp[i\phi_1(\omega)]$, with a central frequency ω_1 and a spectral bandwidth $\Delta \omega_1$. The peak intensity of the pump pulse is set to $I_1 = 7 \times$

^{*}nina.rohringer@mpsd.mpg.de

[†]marcus.dahlstrom@fysik.su.se



FIG. 1. (a) Photoionization processes in neon: (1) photoelectron replica of attosecond pulse by one-photon absorption from 2pstate; (S+) nonsequential two-photon processes generating spectrally sheared replicas by stimulated ionic transitions with a final hole in the 2s state. (b) Sketch of the proposed experiment where an IR laser field is split into two parts for generation of the XUV pump (1) and XUV probe (2,3) fields by HHG. Photoionization of neon atoms is then studied with electron-ion coincidence detection. (c) Photoelectron spectrum with residual hole in 2p state and (d) photoelectron spectrum with residual hole in 2s state, both computed by one-dimensional time-dependent configuration interaction singles (within an independent-particle model). See main text for the labeled spectroscopic structures.

 10^{12} W/cm², with a Fourier-limited pulse duration of 244 as. The group delay,

$$\tau_1(\omega) = \frac{d\phi_1}{d\omega},\tag{2}$$

describes the arrival time of a particular frequency component ω of the pump pulse at the target. We consider probe frequencies, $\omega_{f=2,3}$, that are symmetrically red- and blueshifted relative to the $2p \leftrightarrow 2s$ hole transition,

$$\omega_2 = \epsilon_{2p} - \epsilon_{2s} - \delta\omega,$$

$$\omega_3 = \epsilon_{2p} - \epsilon_{2s} + \delta\omega,$$

where the outer hole energy is $\epsilon_{2p} = -21.56 \text{ eV}$ and the inner hole energy is $\epsilon_{2s} = -48.47 \text{ eV}$ [34]. The peak intensity of the probe fields is set to $I_f = 3.5 \times 10^{12} \text{ W/cm}^2$. The detuning is supposed small compared to the bandwidth of the pump field, $\delta \omega \ll \Delta \omega_1$, and the probe fields are quasimonochromatic with a bandwidth much smaller than the detuning, $\Delta \omega_{2,3} \ll \delta \omega$, as indicated by the δ functions in Eq. (1). The group delay of the probe fields is defined as $\tau_{32} = (\phi_3 - \phi_2)/2\delta\omega$ using the spectral phase of the probe fields, $\phi_{2,3} = \arg\{E_{2,3}\}$. In Fig. 1(b) we propose an experimental setup where the pump (1) is generated by HHG from an ultrashort IR pulse and the probe fields (2,3) are odd HHG harmonics from a longer IR pulse. The group delay of the probe fields is then locked to the phase of the IR laser field due to the nonlinear HHG process, $\tau_{32} \propto \phi_{IR}$, and can be accurately controlled by an IR laser-delay stage. Implementation of this probe technique at FEL sources would require two-color pulse pairs [16–18] and accurate temporal and phase control [19].

As depicted in Fig. 1(a), the proposed probe process can be cast in terms of single-particle transitions. An appropriate numerical method is therefore time-dependent configuration interaction singles (TDCIS) [35]. For the calculation of the photoelectron spectrum we implemented the coupled surface flux method [36], similar to the approach used in Ref. [37]. To discuss the basic process, we opt for a one-dimensional (1D) description of the considered process. In Figs. 1(c) and 1(d) we show simulated ionic channel resolved photoelectron spectra for a 1D model of the neon atom. Surprisingly, we have found that it was important to account for stimulated ion dynamics by the probe fields after the electron has escaped the inner region, as explained in the Appendix. Electron-electron correlation effects do not influence the ionization process significantly and this allows us to further approximate the system by an independent-particle model, where the correlation coupling terms in TDCIS are neglected. This makes the interpretation of the numerical results more tractable but also helps to speed up the computational time.

III. RESULTS

In Sec. III A we present our numerical results for the timedependent 1D model of neon. To interpret our results and to make quantitative estimates, we then turn to perturbation theory in Sec. III B, where we first consider the stimulated $2p \leftrightarrow 2s$ (XUV) transition in Sec. III B 1 and then the $2p \leftrightarrow$ 1s (x-ray) transition in Sec. III B 2.

A. Time-dependent 1D model

Photoelectrons leaving the residual ion with a hole in the 2p state [Figs. 1(c)] exhibit one broad peak (1) due to absorption of one pump photon (with $\omega_1 = 68 \text{ eV}$ and $\Delta \omega_1 = 7.5 \text{ eV}$) and two narrow peaks (2, 3) due to absorption of either probe field (with $\omega_{2,3} = 26.9 \mp 1 \text{ eV}$ and $\Delta \omega_{2,3} = 0.125 \text{ eV}$). The broad peak (S-) is due to absorption of one pump photon and stimulated emission of one probe photon. Weaker peaks labeled with (P²) and (P³) denote two and three probe-photon processes, respectively. Photoelectrons leaving the residual ion with a hole in the 2*s* state [Fig. 1(d)] exhibit a peak (1') from the pump field and a peak (S+) due to absorption of one pump photon and one probe photon.

In Fig. 2 we show the behavior of the (S+) structure as a function of relative probe phase $\phi_{32} = \phi_3 - \phi_2$, for (a) a Fourier-limited pump pulse, $\phi_1(\omega) = 0$; (b) a quadratic phase dependence, $\phi_1(\omega) = \alpha(\omega - \omega_1)^2$, with $\alpha = 100$; and (c) a cubic phase dependence, $\phi_1(\omega) = \beta(\omega - \omega_1)^3$, with $\beta = 100$.



FIG. 2. (a)–(c) Normalized photoelectron distribution of the (S+) peak in Fig. 1(d) as a function of phase difference between probe fields, ϕ_{32} . Data are computed using 1D-TDCIS (within an independent-particle model). (a) Fourier-limited pump pulse; (b) linear chirp; and (c) quadratic chirp of pump pulse. (d)–(f) Same as (a)–(c), but with normalization at each individual kinetic energy. The left vertical axis labels the relative phase in radians, while the right axis labels the extracted group delay of the attosecond pulse in femtoseconds defined in Eq. (2), shown by the dashed white curve.

In Fig. 2(a) the (S+) peak vanishes for $\phi_{32} \approx 0$, while the peak is maximized for $\phi_{32} \approx \pi$. As derived in Sec. III B, this is due to a relative π shift between the two-photon paths that have positive and negative detuning with respect to the hole resonance, respectively. In Figs. 2(d)–2(f) we show more clearly the ϕ_{32} dependence of the (S+) structure by dividing every phase-dependent curve, at a fixed energy of Figs. 2(a)–2(c), by its maximal value. In analogy with spectral shearing interferometry, the modulations (indicated by white dashed curves) are expected to depend on the group delays of the attosecond pump pulse with (d) constant value, (e) linear chirp, and (f) quadratic chirp, respectively. By direct fit to the unchirped case ($\alpha = \beta = 0$) we obtain an extracted α value of -0.288, corresponding to a drift of -0.5 as/eV. Where does this "response time" come from?

Further, our simulations show that the (S-) peak [Fig. 1(c)] has a similar ϕ_{32} dependence as (S+). The one-photon peaks (1) and (1') also modulate with ϕ_{32} , but the variation is opposite to that of (S+) and (S-). Physically, this is because the probe fields are effectively shifting the ionic channel of the photoelectrons, e.g., by redistribution of population from peak (1) to peak (S+). The total photoelectron spectrum, unresolved for the residual ionic state, does not show clear ϕ_{23} dependence. Unfortunately, this makes the experimental measurement of the (S+) modulations challenging, because it must rely on coincidence detection, as we discuss in Sec. IV.

In Fig. 3 we show the "response time" for the case of an unchirped pump pulse, i.e., by zooming in on the dashed curve in Fig. 2(d), for three different symmetric detuning of the probe fields, $\delta \omega = 1, 1.5$, and 2 eV. All detunings show qualitatively the same result with a response time in the range 40–55 as. All curves exhibit a negative slope



FIG. 3. Detailed study of the "response time" of the (S+) peak for three different detuning of the probe field given an unchirped pump pulse ($\alpha = \beta = 0$). In accordance with Eq. (5), the response time, τ_{pb} , is extracted by making a cosine fit to the phase-dependent oscillations of the photoelectron probability, e.g., the modulations shown in Fig. 2(d) (where $\delta \omega = 1 \text{ eV}$). The raw data (not shown) has been fitted to a line in order to extract the α parameter of the pump pulse. Standard deviation of the linear fit is indicated by the error bars. The data were computed by the 1D time-dependent independentparticle model discussed in the Appendix.

with extracted α values for detuning 1, 1.5, and 2 eV equal to -0.288, -0.239, and -0.160, respectively. In order to interpret this behavior we have additionally performed simulations where the photoelectron does not interact with the probe field. In Fig. 3 we label this result as "no ATI" (no above-threshold ionization) because the electron cannot absorb probe photons after it has been ejected within this model (see also the Appendix). Interestingly, the extracted α parameter is -0.00294, which is much closer to the expected zero value. This shows that XUV-driven electron continuum dynamics must be responsible for the finite response time. The discrepancy in recovering the parameters of the pump pulse is attributed to an "atomic response time" and a derivation of how the group delay, $\tau_1(\omega)$, is mapped to the (S+) structure is given by perturbation theory in the next section. In the case of a chirped pump pulse, e.g., $\alpha \neq 0$ case, the finite duration of the probe fields will also affect the extracted values. In the simplified case of Gaussian pulses (with linear chirp given by α) and by considering the "no ATI case," we have found that this effect can be approximated as

$$\tilde{\alpha} = \alpha \left[1 - \frac{2\Delta\omega_f^2}{\Delta\omega_1^2} - \frac{\Delta\omega_f^2}{4\ln(2)\delta\omega^2} \right],\tag{3}$$

where $\tilde{\alpha}$ is the extracted value for the α parameter of the pulse. The bandwidths of the pump and probe pulses are labeled as $\Delta \omega_1$ and $\Delta \omega_{f=2,3}$, respectively, and defined as the fullwidth at half-maximum (FWHM), $E_i(\omega) \sim \exp[-2\ln(2)(\omega - \omega_i)^2/\Delta \omega_i^2]$. In Table I we show the reasonable agreement between this simple analytical estimate ($\tilde{\alpha}$) and the numerical simulations (without ATI). Further, we note that the difference between the case with ATI and without ATI (rightmost column)

α	$\delta\omega$ (eV)	$\Delta \omega_1 ({ m eV})$	$\Delta \omega_f$ (eV)	ã	Numerical		
					With ATI	Without ATI	Difference
-100	1	7.5	0.0625	- 99.79	- 100.127	- 99.85	-0.277
100	1	7.5	0.0625	99.79	99.55	99.86	-0.31
100	1	7.5	0.125	99.5	99.058	99.39	-0.332
10	1	7.5	0.125	9.953	9.646	9.943	-0.297
100	0.5	7.5	0.125	97.69	97.149	97.57	-0.421

TABLE I. Comparison of the retrieved α from numerical calculations and analytical estimate ($\tilde{\alpha}$).

with $\delta \omega = 1$ eV is approximately -0.3, in agreement with our finding for the $\alpha = 0$ case. This indicates that the electron contribution does not depend strongly on the chirp of the pump pulse. Finally, the difference between the numerical simulations with $\alpha = 100$ and $\delta \omega = 0.5$ eV (in Table I) shows a larger negative slope than the $\delta \omega = 1$ eV case, in agreement with the trend found for the $\alpha = 0$ case (in Fig. 3). In the following we do not focus on these detailed pulse convolution effects that occur due to the finite bandwidth of the probe fields $\Delta \omega_f$, but rather explain the fundamental reason for why electron continuum dynamics leads to a nonzero response time.

B. Time-independent perturbation theory

In order to better understand the physical mechanism of the atomic response time, we now turn to perturbation theory. The dominant complex amplitudes that give rise to ϕ_{32} -dependent modulations of the (S+) structure are given by

$$S_{pb,f} = \frac{1}{i} E_1(\omega_{pb} - \omega_f) E_f M_{pb,f}, \quad f = 2,3,$$
 (4)

corresponding to absorption of one photon from the pump field with energy $\omega'_1 = \omega_{pb} - \omega_f$, followed by one from either probe field with energy ω_f .

1. Stimulation of $2p \rightarrow 2s$ hole transition

In Eq. (4), the two-photon matrix element, $M_{pb,f} = M_{pb}(\omega_{pb} - \omega_f, \omega_f)$, describes a transition from the ground state to a final state with one electron in the continuum state p = ks, kd (with energy $\epsilon_p > 0$) and a hole in the atomic orbital b = 2s ($\epsilon_b < 0$). Energy conservation is imposed as $\omega_{pb} = \epsilon_p - \epsilon_b = \omega'_1 + \omega_f$. The probability density for electrons in the (S+) structure is computed as the square of the two complex amplitudes with f = 2,3 leading to an interference pattern over $\phi_{32} \propto \tau_{32}$,

$$W_{pb} \approx |S_{pb,2} + S_{pb,3}|^2 = |A_{pb}| - |B_{pb}| \cos[2\delta\omega(\tau_1 - \tau_{32} + \tau_{pb})], \quad (5)$$

where $|A_{pb}|$ is the incoherent sum of the transition strengths, while $|B_{pb}|$ relates to the cross term of the amplitudes. We note that the group delays of the pump τ_1 and the probe fields τ_{32} enter with opposite signs in Eq. (5), which must be the case because if the pump field is delayed by a certain amount the probe field must also be delayed by the same amount to recover same outcome. Besides the group-velocity delays τ_1 and τ_{32} , the interference pattern is delayed by

$$\tau_{pb} = [\arg(M_{pb,2}M_{pb,3}^*) - \pi]/2\delta\omega,$$
(6)

which depends on the phase difference between the twophoton matrix elements and can be interpreted as an atomic response time for creating the (S+) peak. Because it is convenient to define the response time as a small number, we have included a $-\pi$ inside the square bracket in Eq. (6) to remove the relative π shift between the two-photon transitions due to the resonance. It follows from this definition that there is a minus sign on the cosine in Eq. (5). While τ_{pb} may be regarded as a limiting factor for determining the unknown τ_1 , explaining the modest error in the extracted α value above for the 1D model, the response time is an interesting quantity to study further, as it contains information about the stimulated core-valence transition; in particular, it contains information about the phase difference of the two-photon (XUV-XUV) matrix elements.

In order to make a quantitative estimate of τ_{pb} , we now turn to many-body perturbation theory to describe neon in 3D and include correlation effects. Following Ref. [38], our calculations are based on single-particle states that are expanded on a spherical basis $\phi_i(\mathbf{r}) = R_{n_i,l_i}(r)Y_{l_i,m_i}(\hat{\mathbf{r}})$. The radial wave functions, $R_i(r)$, are eigenstates to the restricted Hartree-Fock (HF) equation for occupied states, while the unoccupied (virtual) states are additionally attracted by an effective spherical potential to model the long-range Coulomb interaction between electron and ion.

The two-photon matrix elements are separated into two terms using second quantization,

$$M_{pb,f} \approx M_{pb,f}^{\text{(hole)}} + M_{pb,f}^{\text{(elec.)}},\tag{7}$$

because the probe field can either stimulate a hole transition or a continuum electron transition, as illustrated in Figs. 5(a)and 5(b), respectively. The stimulated hole term

$$M_{pb,f}^{\text{(hole)}} = \sum_{a'} \frac{z_{a'b} z_{pa'}}{(\omega_f - \epsilon_{a'} + \epsilon_b)}$$
(8)

describes a dipole transition of an electron from any occupied single-particle state $\phi_{a'}$ to the final electron state ϕ_p , followed by a dipole transition of the hole to the final state ϕ_b . The radial orbitals are chosen to be real, which implies a real transition to a given final partial wave state, $\phi_p = ks, kd$ for $\phi_b = 2s$. In contrast, the stimulated electron term is complex,

$$\mathcal{M}_{pb,f}^{(\text{elec.})} = \lim_{\xi \to 0^+} \sum_{p'}^{f} \frac{z_{pp'} z_{p'b}}{(\omega_1' - \epsilon_{p'} + \epsilon_b + i\xi)}$$
$$= \text{p.v.} \int_{p'} \frac{z_{pp'} z_{p'b}}{(\omega_1' - \epsilon_{p'} + \epsilon_b)} - i\pi z_{pr} z_{rb}, \qquad (9)$$

1



FIG. 4. (a) Squared matrix elements, $|M_{pb,f}|^2$, for final *s*-wave (dotted) and *d*-wave (dashed), including both stimulated hole and electron paths in the bold lines and only electron paths in the thin lines. (b) Response time for photoemission along polarization axis, *s*-wave and *d*-wave. Data presented in (a) and (b) are computed by a 3D independent-particle model of neon. (c) Response time for photoemission along the polarization axis (within a correlated model including both time orderings) for the stimulated valence hole $(2p \rightarrow 2s)$ and core hole $(2p \rightarrow 1s)$ transitions. The streak-camera delay from the initial 2p (2s) state [38] is shown for reference.

and it describes an initial dipole interaction that excites an electron from the occupied state $\phi_b = 2s$, to the unoccupied states, $\phi_{p'} = n'p$ and k'p. The second dipole interaction then stimulates an electron transition in the continuum $[\omega'_1 + \epsilon_b >$ 0 as shown in Fig. 5(c)] to the final state $\phi_p = ks, kd$. In Eq. (9) we write the matrix element as real nonresonant contributions (principal-value sum integrals over p' = k'p) and an imaginary resonant contribution (via the intermediate state $\phi_r = k_r p$ with $\epsilon_r = \epsilon_b + \omega'_1$). If the probe field is in the IR range the stimulated electron transition is a good approximation for the total two-photon matrix element $M_{pb,f} \approx M_{pb,f}^{(\text{elec.})}$ but this is not the case for the processes studied here with nearly resonant XUV transitions. In Fig. 4(a) we show that stimulated electron contributions $|M_{pb,f}^{(\text{elec.})}|^2$ are 2–3 orders of magnitude smaller than the total contributions $|M_{pb,f}|^2$ that are dominated by the strong resonant coupling in the residual ion. Here, the total matrix element is better approximated as a hole transition plus a small imaginary electron transition $M_{pb,f} \approx M_{pb,f}^{(hole)} + i \text{Im} M_{pb,f}^{(elec.)}$. If we note that $M_{pb,2}^{(hole)} = -M_{pb,3}^{(hole)}$ and assume that $M_{pb,2}^{(elec.)} \approx M_{pb,3}^{(elec.)}$, then

$$\tau_{pb} \approx -\frac{\arg[M_{pb,3}]}{\delta\omega} \\ = \frac{1}{\delta\omega} \arctan\left[\frac{\pi z_{pr} z_{rb}}{z_{ab} z_{pa}/\delta\omega}\right] \approx \frac{\pi z_{pr} z_{rb}}{z_{ab} z_{pa}}, \quad (10)$$

where $z_{ij} > 0$ are dipole matrix elements between between the real single-particle states ϕ_i and ϕ_j . The last step in Eq. (10) is valid for small detuning, $\delta \omega \ll |z_{ab}z_{pa}/\pi z_{pr}z_{rb}|$. Interestingly, Eq. (10) shows that τ_{pb} does not depend strongly on $\delta \omega$ but rather gives direct information about the ratio between dipole matrix elements of the stimulated electron and hole transitions. In other words, decreasing the detuning to further stimulate the hole transitions will not alter the response time. This has been verified by many-body perturbation theory for $\delta \omega = 1$ and 1.5 eV, where we found that the response time changed by less than 1 as.

In Fig. 4(b) we present τ_{pb} from Eq. (6) using the 3D independent-particle model given by Eq. (7). A positive linear drift is found on both final partial waves, ks and kd, which we attribute to an increasing relative contribution from the resonant electron path, i.e., the numerator on the right side of Eq. (10). We also show τ_{pb} for photoelectrons with momentum $\mathbf{k} = k\hat{\mathbf{z}}$ along the polarization axis, computed by the complex final state

$$\phi_{\mathbf{k}}(\mathbf{r}) \propto \sum_{L,M} i^L e^{-i\eta_L(k)} Y^*_{L,M}(\hat{\mathbf{k}}) R_{k,L}(r) Y_{L,M}(\hat{\mathbf{r}}), \qquad (11)$$

where $\eta_L(k)$ are scattering phases of the real radial functions, $R_{k,L}(r)$. The angle-resolved emissions has a linear drift of 0.634 as/eV, quite close to the dominant *d*-wave. Over a large energy range, from 65 to 120 eV, the deviation from this linear fit is less than 1 as. The response times of the 3D calculation are in qualitative agreement with those of the 1D case, with a delay on the order of tens of attoseconds. Surprisingly, we find that the slopes of the response times are different in the 1D and 3D case. It remains an open question if this discrepancy is entirely due to pulse convolution effects or if the different electronic structure between 1D and 3D plays a role. In order to answer this question, it would be beneficial to perform 3D TDCIS calculations [37], but this remains an endeavor beyond the scope of the present paper.

Next, we add correlation effects by implementing the random phase approximation with exchange (RPAE) on the first dipole interaction [38], which increases the linear slope to 0.733 as/eV (not shown). Including also the nonresonant, reversed time-order (TO) processes, where the probe photon is absorbed before the pump photon changes the slope marginally to 0.724 as/eV. Although the contribution from the reversed-TO is rather small, we stress that the $\delta\omega$ dependence reported for the 1D model in Fig. 3 cannot be explained without taking this effect into account.

Finally, we note that the ratio of the two-photon (pump + probe) and one-photon (pump) transition rates

$$R \approx \left| \frac{E_f z_{ba}}{\delta \omega} \right|^2, \tag{12}$$

scales inversely with the squared detuning of the probe field. This implies a boost of the two-photon transition by tuning the probe fields closer to the resonance. Assuming $\delta \omega = 1 \text{ eV} = 0.0358$ au, $z_{ab} \approx 1$ au, and R = 1%, we estimate that the required probe field intensity is $I_f|_{R=1\%} = 7.4 \times 10^{-5}$ au = $2.6 \times 10^{12} \text{ W/cm}^2$. In the case studied here with one short pump pulse and two long probe fields it is only the temporal overlap of the two pulses that will contribute to the two-photon transition. Using the time-dependent model, discussed in Sec. III A, we have verified that the probability for the two-photon transition does not depend on the duration of the probe fields, but rather on the instantaneous intensity and detuning of the probe fields. We refer the interested reader to Ref. [39] for an insightful discussion about pump-probe schemes on the attosecond time scale.

2. Stimulation of $2p \rightarrow 1s$ hole transition

The squared two-photon matrix element for the $2p \rightarrow 1s$ stimulated hole transition is roughly two orders of magnitude smaller than that of the $2p \rightarrow 2s$, shown in Fig. 4(a), but the trend is otherwise similar. This is easy to understand because the dipole coupling from the 2p valence state to the 1s inner-core state is smaller than that of 2p to 2s. In Fig. 4(c) we compare τ_{pb} , including correlation and both time orders (RPAE + TO), for XUV-stimulated outer-core-valence transition $(2p \rightarrow 2s)$ and x-ray inner-core-valence transition $(2p \rightarrow 1s)$. Evidently, the core transition has a much shorter



FIG. 5. (a) Two-photon diagram for stimulated hole transition, $2p \rightarrow 2s$, after photoemission from outer state, $2p \rightarrow ks, kd$. (b) Two-photon diagram for stimulated electron continuum transition from an inner valence state, $2s \rightarrow k'p \rightarrow ks, kd$. (c) Two-photon diagram for stimulated virtual electron transition from a core state, $1s \rightarrow n'p \rightarrow ks, kd$.

response time. This can be explained by the fact that the (main) electron path no longer goes through the continuum, but instead on a virtual bound excitation,

$$M_{pb,f}^{(\text{elec.})} = \sum_{n'} \frac{z_{pn'} z_{n'b}}{(\omega_1' - \epsilon_{n'} + \epsilon_b)},$$
(13)

where $\omega'_1 + \epsilon_b < 0$ for b = 1s, as illustrated in Fig. 5(c). In the present calculation we used the real HF energy for the 1s orbital $\epsilon_{1s}^{(HF)} = -891.70$ eV, which should be valid provided that the pump pulse is sufficiently short. Nonetheless, we have also tested to give the 1s energy an imaginary part (equal to 0.27 eV) to mimic the decay of the core hole, but this did not change the response time by more than 1 as.

IV. DISCUSSION

In this paper we have explored an idea to perform spectral shearing interferometry of photoelectrons using two coherent XUV (or x-ray) probe fields. Due to the excess or shortage of photon energy for a given ionic transition, the photoelectron will shift up or down in coincidence with the transition in the ion. The idea is closely related to the attosecond streak-camera method [5-7], where a strong IR field is used to drive the electron in the continuum and to the PROOF method [29,40] where a single IR photon is absorbed or emitted to shear the photoelectron distribution. The corresponding atomic response times of the attosecond streak camera are shown for reference in Fig. 4(c) [38]. As can be observed, the response time from the outer-core method $(2p \rightarrow 2s \text{ transition})$ is larger than the response time of the streak camera from the 2p state in neon. As we explained, the relatively large response of the outer-core method comes from stimulated continuum electron transitions by the probe field. In contrast, the response time of the inner-core method $(2p \rightarrow 1s)$ is found to be comparable to that of the streak-camera method. In this case the response time of the inner-core method comes from correlation effects and possibly field-convolution effects. In theory, this establishes the proposed scheme as an all-XUV or x-ray method for direct group-delay determination of attosecond pulses. Assuming that the attosecond pulse has been readily characterized, e.g., by the streak-camera method, the new method can be used to study the phase difference of two-photon (XUV-XUV or XUV-x-ray) processes. However, in order to extract the desired signal, i.e., the ϕ_{32} -dependent modulations of the (S+) peak in Fig. 2, we need to study channel-resolved photoelectrons. More precisely, we need to distinguish between electrons from the unexcited ion (with a 2p hole) and the excited ion (with a 1s or 2s hole). In practice, this is a major drawback of the method because the streak camera does not require any form of coincidence detection. The first coincidence detection schemes combined with attosecond pulses have been reported recently [41-43], but so far no experiments have been reported where the state of the ion has been determined separately from the electron. Nonetheless, let us now speculate as to how this type of measurement can be performed in future experiments, inspired by the existing technology, such as reaction microscopes [44] and photoelectron-fluorescence coincidence detection [45]. First, for the case of a 1s hole, high-energy Auger emission will occur on a femtosecond time scale and efficiently convert the singly charged ion to

the doubly charged ion. A reaction microscope can be used to separate the photoelectron and the ion in space; then the ionic charge can be determined by accelerating the ions in an electric field. Since Auger emission is the dominant decay mechanism for the 1s hole, this Auger-based method is deemed more feasible than fluorescence-based detection. In contrast, the decay occurs exclusively by fluorescence for the case of a 2s hole and it may appear that the only way to probe the state of the ion would be to detect florescence photons on a nanosecond time scale. However, recent experimental work has shown that it is possible to laser enable Auger decay of the 2s hole by hitting the excited ion with an intense IR laser field [41]. This opens up for both ion-acceleration technique and electron-coincidence detection of the highenergy primary electron and the low-energy Auger electron to determine the state of the ion. Clearly, all these ideas are more challenging to implement experimentally than the conventional attosecond streak camera, but we believe that these are technical challenges that can be overcome in the future. Finally, we stress that the issue of photoelectrons with the same final energy from different states of the ion is inherent to the broad bandwidth of the pump pulse. If our aim is to study the phase of the two-photon matrix elements, it is more efficient to replace the isolated pump pulse [(1) in Fig. 1] by an attosecond pulse train that translates to a comblike photoelectron spectrum with spacing $2\delta\omega$. In this case the (S+) signal then resides on peaks in between the comblike peaks of the pump field, which means that the ϕ_{32} dependence can also be studied without coincidence detection, but only at discrete energy intervals determined by the comb structure. This setup bears great resemblance with and could be used together with the RABBITT method [28].

V. CONCLUSIONS

In conclusion, we have proposed a new type of pump-probe scheme that relies on stimulated core-valence transitions by two narrow-band detuned XUV or x-ray probe fields and a short XUV pump pulse. Here we applied the method to the characterization of isolated attosecond pulses and we demonstrated the existence of an atomic response time that gives insight into the nature of the stimulated core-valence transitions. In particular, for the stimulated $2p \rightarrow 2s$ hole transition in neon, we found that the response time can be approximated by a ratio between electron continuum transitions and the stimulated hole transition. In practice, the method relies on coincidence detection of electron and ion, which makes it less efficient than existing techniques based on IR sources for pulse characterization. Nonetheless, the method is a natural candidate for future XUV-XUV experiments on tabletop HHG sources and at FEL facilities, as it presents a way to study XUV-XUV/x-ray processes with short pump pulse probed by the sharp frequency bandwidth of the probe fields.

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APPENDIX

Time-dependent configuration interaction singles (TD-CIS) [35] includes the Hartree-Fock ground state $|\Phi_0\rangle$ and its single excitations $|\Phi_a^p\rangle$ based on the one-particle Fock operator \hat{H}_0 and its eigenstate $|\varphi_i\rangle$ with energy ϵ_i . Generally, indices a, b, c, \ldots are used for spatial orbitals that are occupied in $|\Phi_0\rangle$, for unoccupied (virtual) orbitals indices p, q, r, \ldots are employed, and the indices i, j, k, \ldots are for general orbitals (occupied or unoccupied). Spin-orbit interaction is not considered in this work. The many-body wave packet in the CIS basis is given by

$$|\Psi,t\rangle = \alpha_0(t)|\Phi_0\rangle + \sum_p \sum_a \alpha_a^p(t) |\Phi_a^p\rangle, \tag{A1}$$

with initial conditions $\alpha_0(t_0) = 1$ and $\alpha_a^p(t_0) = 0$. To describe the hole dynamics and the corresponding electron wave packet propagating in the real space, we introduce time-dependent orbitals that collect all single excitations originating from the occupied orbitals $|\varphi_a\rangle$,

$$|\chi_a(t)\rangle = \sum_p \alpha_a^p(t) |\varphi_p\rangle.$$
 (A2)

For the atomic system interacting with laser field E(t) linearly polarized along the *z* axis, the TDCIS equations of motion can be written as

$$i\dot{\alpha_0} = -E(t)\sum_a \langle \varphi_a | \hat{z} | \chi_a(t) \rangle,$$
 (A3)

$$i\frac{\partial}{\partial t}|\chi_{a}(t)\rangle = (\hat{H}_{0} - \varepsilon_{a})|\chi_{a}(t)\rangle + \sum_{b}\hat{P}\{\hat{K}_{ba} - \hat{J}_{ba}\}|\chi_{b}(t)\rangle - E(t)\hat{P}\hat{z}\{\alpha_{0}|\varphi_{a}\rangle + |\chi_{a}(t)\rangle\} + E(t)\sum_{b}z_{ba}|\chi_{b}(t)\rangle,$$
(A4)

where $z_{ba} = \langle \varphi_b | z | \varphi_a \rangle$, \hat{P} is the projection operator acting on the subspace composed of the virtual orbitals,

$$\hat{P} = \sum_{p} |\phi_{p}\rangle\langle\phi_{p}| = 1 - \sum_{a} |\phi_{a}\rangle\langle\phi_{a}|, \qquad (A5)$$

and \hat{J}_{ba} and \hat{K}_{ba} are, respectively, generalized Coulomb and exchange operators associated with the direct Coulomb matrix elements v_{pbqa} and the exchange matrix elements v_{pbqa} :

$$\begin{aligned}
\nu_{pbqa} &\equiv \langle \varphi_p | J_{ba} | \varphi_q \rangle, \\
\nu_{pbaq} &\equiv \langle \varphi_p | \hat{K}_{ba} | \varphi_q \rangle.
\end{aligned} \tag{A6}$$

This procedure establishes a system of linear, coupled oneparticle Schrödinger-like equations in Eq. (A4) for the orbitals $|\chi_a(t)\rangle$ with initial condition $|\chi_a(t_0)\rangle = 0$. To calculate photoelectron spectra, we need to evaluate with the transition amplitude between a modified Volkov state and the outgoing multichannel wave packet, $\langle \chi_{\mathbf{k},a}(t) | \chi_a(t) \rangle$, at a time, *t*, long after all interactions have ceased. The modified Volkov state in length gauge, $|\chi_{\mathbf{k},a}(t)\rangle$, with momentum **k** includes an additional phase factor for a hole at the orbital $|\varphi_a\rangle$, and it satisfies the equation

$$i\frac{\partial}{\partial t}|\chi_{\mathbf{k},a}(t)\rangle = \left(-\frac{1}{2}\hat{\nabla}^{2} - \varepsilon_{a} - E(t)\hat{z}\right)|\chi_{\mathbf{k},a}(t)\rangle$$

$$\equiv \hat{H}_{a}(t)|\chi_{\mathbf{k},a}(t)\rangle, \qquad (A7)$$

where $\hat{H}_a(t)$ represents the modified Volkov Hamiltonian for the electron moving in the external laser field with a hole fixed at the orbital $|\varphi_a\rangle$. To overcome the difficulty of the calculation with a large box, we adapt the time-dependent surface flux (t-SURFF) [36] method to the multichannel TDCIS formalism. First, we define the overlap from a large distance R_c to infinity between the modified Volkov state and the wave packet in a given channel, *a*, by a stepfunction,

$$A_{\mathbf{k},a}(R_c,t) \equiv \langle \chi_{\mathbf{k},a}(t)|\theta(R_c)|\chi_a(t)\rangle = \int_{|\mathbf{r}|>R_c} d^{(3)}r \ \chi^*_{\mathbf{k},a}(r,t)\chi_a(r,t), \tag{A8}$$

that converges to the transition amplitude after some sufficiently large time T_c . Equation (A8) can also be written as

$$A_{\mathbf{k},a}(R_c, T_c) = \int_{t_0}^{T_c} dt \frac{d}{dt} \langle \chi_{\mathbf{k},a}(t) | \theta(R_c) | \chi_a(t) \rangle$$

=
$$\int_{t_0}^{T_c} dt \left\{ \left[\frac{d}{dt} \langle \chi_{\mathbf{k},a}(t) | \right] \theta(R_c) | \chi_a(t) \rangle + \langle \chi_{\mathbf{k},a}(t) | \theta(R_c) \frac{d}{dt} | \chi_a(t) \rangle \right\}.$$
 (A9)

If we neglect correlation effects and ionic potential outside R_c , then the time-dependent wave packet $|\chi_a(t)\rangle$ follows the equation of motion

$$i\frac{\partial}{\partial t}|\chi_a(t)\rangle = \hat{H}_a(t)|\chi_a(t)\rangle + E(t)\sum_b z_{ba}|\chi_b(t)\rangle.$$
(A10)

In addition to the modified Volkov Hamiltonian, there is other term which makes different channels coupled to each other by laser field. With Eqs. (A7), (A9), and (A10), we can convert $A_{k,a}(R_c, T_c)$ from the spatial integration at T_c to the temporal integration:

$$A_{\mathbf{k},a}(R_{c},T_{c}) = i \int_{t_{0}}^{T_{c}} dt \left\{ \langle \chi_{\mathbf{k},a}(t) | \hat{H}_{a}(t) \theta(R_{c}) | \chi_{a}(t) \rangle - \sum_{b} \langle \chi_{\mathbf{k},a}(t) | \theta(R_{c}) \Big[\hat{H}_{a}(t) \delta_{ab} + E(t) z_{ab} \Big] | \chi_{b}(t) \rangle \right\}$$

$$= i \int_{t_{0}}^{T_{c}} dt \langle \chi_{\mathbf{k},a}(t) | [\hat{H}_{a}(t), \theta(R_{c})] | \chi_{a}(t) \rangle - i \sum_{b} z_{ab} \int_{t_{0}}^{T_{c}} dt E(t) \langle \chi_{\mathbf{k},a}(t) | \theta(R_{c}) | \chi_{b}(t) \rangle$$

$$= - \int_{t_{0}}^{T_{c}} dt J_{\mathbf{k},a}(R_{c},t) - \int_{t_{0}}^{T_{c}} dt K_{\mathbf{k},a}(R_{c},t). \tag{A11}$$

We get two terms and the first term is the time integration of the flux

$$J_{\mathbf{k},a}(R_{c},t) = \frac{1}{2i} [-\chi_{\mathbf{k},a}^{*}(r,t)\partial_{r}\chi_{a}(r,t) + \chi_{a}(r,t)\partial_{r}\chi_{\mathbf{k},a}^{*}(r,t)]|_{R_{c}}$$
(A12)

through the boundary R_c from t_0 to T_c as indicated in [36,37]. Compared with the previous work [37], the second term is new and its integrand,

$$K_{\mathbf{k},a}(R_c,t) = i \sum_{b} z_{ab} E(t) \langle \chi_{\mathbf{k},b}(t) | \theta(R_c) | \chi_b(t) \rangle e^{-i(\varepsilon_a - \varepsilon_b)t},$$
(A13)

represents the channel coupling of the TDCIS via laser field after the electronic wave packets pass though R_c . This contribution is missing in the integration of the flux at R_c , so this channel-coupling term can be viewed as an external source from other channels as the states of the ion makes transition. In other words, if the field-driven transition between two different ionic states plays the role in the physical process, this channel-coupling term cannot be neglected. This term is especially important if the photoelectron spectrum is measured in coincidence with parent ions. The t-SURFF integral equation,

$$A_{\mathbf{k},a}(R_c, T_c) = -\int_{t_0}^{T_c} dt J_{\mathbf{k},a}(R_c, t) - \int_{t_0}^{T_c} dt K_{\mathbf{k},a}(R_c, t),$$
(A14)

is numerically evaluated with $\chi_a(r,t)$ determined by TDCIS under the initial condition $A_{\mathbf{k},a}(R_c,t_0) = 0$. Finally, the momentum spectrum $\sigma_{\mathbf{k},a}(\mathbf{k})$ and energy spectrum $\sigma_{E,a}(E)$ for the channel *a* are given by

$$\sigma_{\mathbf{k},a}(\mathbf{k}) \equiv |A_{\mathbf{k},a}(R_c, T_c)|^2, \qquad (A15)$$

$$\sigma_{E,a}(E) \equiv \sum_{|\mathbf{k}| = \sqrt{2E}} \frac{\sigma_{\mathbf{k}}(\mathbf{k})}{|\mathbf{k}|}.$$
 (A16)

The numerical results presented in the main text are obtained using an 1D effective central potential and effective electronelectron repulsive potential,

$$V_{\rm eff}(z) = \frac{Z_{\rm eff}}{\sqrt{z^2 + z_c^2}}, \quad V_{\rm ee}(z_1, z_2) = \frac{Z_{\rm ee}}{\sqrt{(z_1 - z_2)^2 + z_e^2}},$$
 (A17)

with parameters Z_{eff} , Z_{ee} , z_c , and z_e that reproduce the experimental ionization energies of the 2s and 2p orbitals in

neon. We considered two models. First, the parameters of the effective potential were chosen such that the electron-electron interaction was zero, which corresponds to the independent-particle approximation (IPA), by parametrization as $Z_{ee} = 0$, $Z_{eff} = 1.795$, and $z_c = 0.7$. Second, we studied the correlated

- F. Krausz and M. Ivanov, Attosecond physics, Rev. Mod. Phys. 81, 163 (2009).
- [2] D. Shafir, H. Soifer, B. D. Bruner, M. Dagan, Y. Mairesse, S. Patchkovskii, M. Yu. Ivanov, O. Smirnova, and N. Dudovich, Resolving the time when an electron exits a tunneling barrier, Nature (London) 485, 343 (2012).
- [3] K. T. Kim, C. Zhang, A. D. Shiner, S. E. Kirkwood, E. Frumker, G. Gariepy, A. Naumov, D. M. Villeneuve, and P. B. Corkum, Manipulation of quantum paths for space-time characterization of attosecond pulses, Nat. Phys. 9, 159 (2013).
- [4] F. Calegari, D. Ayuso, A. Trabattoni, L. Belshaw, S. De Camillis, S. Anumula, F. Frassetto, L. Poletto, A. Palacios, P. Decleva, J. B. Greenwood, F. Martín, and M. Nisoli, Ultrafast electron dynamics in phenylalanine initiated by attosecond pulses, Science 346, 336 (2014).
- [5] M. Hentschel, R. Kienberger, Ch. Spielmann, G. A. Reider, N. Milosevic, T. Brabec, P. Corkum, U. Heinzmann, M. Drescher, and F. Krausz, Attosecond metrology, Nature (London) 414, 509 (2001).
- [6] J. Itatani, F. Quéré, G. L. Yudin, M. Yu. Ivanov, F. Krausz, and P. B. Corkum, Attosecond Streak Camera, Phys. Rev. Lett. 88, 173903 (2002).
- [7] R. Kienberger, E. Goulielmakis, M. Uiberacker, A. Baltuska, V. Yakovlev, F. Bammer, A. Scrinzi, Th. Westerwalbesloh, U. Kleineberg, U. Heinzmann, M. Drescher, and F. Krausz, Atomic transient recorder, Nature (London) 427, 817 (2004).
- [8] M. Schultze *et al.*, Delay in photoemission, Science 328, 1658 (2010).
- [9] Z.-H. Loh, M. Khalil, R. E. Correa, R. Santra, C. Buth, and S. R. Leone, Quantum State-Resolved Probing of Strong-Field-Ionized Xenon Atoms Using Femtosecond High-Order Harmonic Transient Absorption Spectroscopy, Phys. Rev. Lett. 98, 143601 (2007).
- [10] E. Goulielmakis, Z.-H. Loh, A. Wirth, R. Santra, N. Rohringer, V. S. Yakovlev, S. Zherebtsov, T. Pfeifer, A. M. Azzeer, M. F. Kling, S. R. Leone, and F. Krausz, Real-time observation of valence electron motion, Nature 466, 739 (2010).
- [11] C. Ott, A. Kaldun, L. Argenti, P. Raith, K. Meyer, M. Laux, Y. Zhang, A. Blattermann, S. Hagstotz, T. Ding, R. Heck, J. Madronero, F. Martin, and T. Pfeifer, Reconstruction and control of a time-dependent two-electron wave packet, Nature (London) 516, 374 (2014).
- [12] W. Ackermann *et al.*, Operation of a free-electron laser from the extreme ultraviolet to the water window, Nat. Photon. 1, 336 (2007).
- [13] P. Emma *et al.*, First lasing and operation of an angstromwavelength free-electron laser, Nat. Photon. 4, 641 (2010).
- [14] T. Ishikawa *et al.*, A compact X-ray free-electron laser emitting in the sub-angstrom region, Nat. Photon. 6, 540 (2012).
- [15] E. Allaria *et al.*, Highly coherent and stable pulses from the FERMI seeded free-electron laser in the extreme ultraviolet, Nat. Photon. **6**, 699 (2012).

TDCIS model, parametrized by $Z_{ee} = 1$, $Z_{eff} = 9$, and $z_c = 0.755$. The IPA and TDCIS agree remarkably well for our field parameters, with only slightly different extracted phase parameters for the proposed method that depend on the detailed correlated interactions.

- [16] A. A. Lutman, R. Coffee, Y. Ding, Z. Huang, J. Krzywinski, T. Maxwell, M. Messerschmidt, and H.-D. Nuhn, Experimental Demonstration of Femtosecond Two-Color X-ray Free-Electron Lasers, Phys. Rev. Lett. **110**, 134801 (2013).
- [17] E. Allaria *et al.*, Two-colour pump-probe experiments with a twin-pulse-seed extreme ultraviolet free-electron laser, Nat. Commun. 4, 2476 (2013).
- [18] A. A. Lutman, F.-J. Decker, J. Arthur, M. Chollet, Y. Feng, J. Hastings, Z. Huang, H. Lemke, H.-D. Nuhn, A. Marinelli, J. L. Turner, S. Wakatsuki, J. Welch, and D. Zhu, Demonstration of Single-Crystal Self-Seeded Two-Color X-ray Free-Electron Lasers, Phys. Rev. Lett. **113**, 254801 (2014).
- [19] D. Gauthier, P. R. Ribič, G. De Ninno, E. Allaria, P. Cinquegrana, M. B. Danailov, A. Demidovich, E. Ferrari, L. Giannessi, B. Mahieu, and G. Penco, Spectrotemporal Shaping of Seeded Free-Electron Laser Pulses, Phys. Rev. Lett. **115**, 114801 (2015).
- [20] A. A. Zholents and W. M. Fawley, Proposal for Intense Attosecond Radiation from an X-ray Free-Electron Laser, Phys. Rev. Lett. 92, 224801 (2004).
- [21] A. A. Zholents and G. Penn, Obtaining attosecond x-ray pulses using a self-amplified spontaneous emission free electron laser, Phys. Rev. Spec. Top. Accel. Beams 8, 050704 (2005).
- [22] E. Prat and S. Reiche, Simple Method to Generate Terawatt-Attosecond X-ray Free-Electron-Laser Pulses, Phys. Rev. Lett. 114, 244801 (2015).
- [23] G. Marcus, G. Penn, and A. A. Zholents, Free-Electron Laser Design for Four-Wave Mixing Experiments with Soft-X-Ray Pulses, Phys. Rev. Lett. 113, 024801 (2014).
- [24] Benjamin Erk *et al.*, Imaging charge transfer in iodomethane upon x-ray photoabsorption, Science 345, 288 (2014).
- [25] B. K. McFarland *et al.*, Ultrafast X-ray Auger probing of photoexcited molecular dynamics, Nat. Commun. 5, 4235 (2014).
- [26] Ph. Wernet *et al.*, Orbital-specific mapping of the ligand exchange dynamics of Fe(CO)₅ in solution, Nature (London) 520, 78 (2015).
- [27] Thomas R. M. Barends *et al.*, Direct observation of ultrafast collective motions in co myoglobin upon ligand dissociation, Science 350, 445 (2015).
- [28] P. M. Paul, E. S. Toma, P. Breger, G. Mullot, F. Augé, Ph. Balcou, H. G. Muller, and P. Agostini, Observation of a train of attosecond pulses from high harmonic generation, Science 292, 1689 (2001).
- [29] M. Chini, S. Gilbertson, S. D. Khan, and Z. Chang, Characterizing ultrabroadband attosecond lasers, Opt. Express 18, 13006 (2010).
- [30] M. Chini, K. Zhao, and Z. Chang, The generation, characterization and applications of broadband isolated attosecond pulses, Nat. Photon. 8, 178 (2014).
- [31] S. Schulz, I. Grguraš, C. Behrens, H. Bromberger, J. T. Costello, M. K. Czwalinna, M. Felber, M. C. Hoffmann, M. Ilchen, H. Y. Liu, T. Mazza, M. Meyer, S. Pfeiffer, P. Prędki,

S. Schefer, C. Schmidt, U. Wegner, H. Schlarb, and A. L. Cavalieri, Femtosecond all-optical synchronization of an X-ray free-electron laser, Nat. Commun. **6**, 5938 (2015).

- [32] I. Grguras, A. R. Maier, C. Behrens, T. Mazza, T. J. Kelly, P. Radcliffe, S. Dusterer, A. K. Kazansky, N. M. Kabachnik, Th. Tschentscher, J. T. Costello, M. Meyer, M. C. Hoffmann, H. Schlarb, and A. L. Cavalieri, Ultrafast X-ray pulse characterization at free-electron lasers, Nat. Photon. 6, 852 (2012).
- [33] K. Klünder, J. M. Dahlström, M. Gisselbrecht, T. Fordell, M. Swoboda, D. Guénot, P. Johnsson, J. Caillat, J. Mauritsson, A. Maquet, R. Taïeb, and A. L'Huillier, Probing Single-Photon Ionization on the Attosecond Time Scale, Phys. Rev. Lett. 106, 143002 (2011).
- [34] A. Kramida, Yu. Ralchenko, J. Reader, and and NIST ASD Team, NIST Atomic Spectra Database (ver. 5.2), http://physics.nist.gov/asd (National Institute of Standards and Technology, Gaithersburg, MD, 2014).
- [35] N. Rohringer, A. Gordon, and R. Santra, Configurationinteraction-based time-dependent orbital approach for *ab initio* treatment of electronic dynamics in a strong optical laser field, Phys. Rev. A 74, 043420 (2006).
- [36] L. Tao and A. Scrinzi, Photo-electron momentum spectra from minimal volumes: The time-dependent surface flux method, New J. Phys. 14, 013021 (2012).
- [37] A. Karamatskou, S. Pabst, Y.-J. Chen, and R. Santra, Calculation of photoelectron spectra within the time-dependent configuration-interaction singles scheme, Phys. Rev. A 89, 033415 (2014).

- [38] J. M. Dahlström, T. Carette, and E. Lindroth, Diagrammatic approach to attosecond delays in photoionization, Phys. Rev. A 86, 061402 (2012).
- [39] Á Jiménez-Galán, F. Martín, and L. Argenti, Two-photon finitepulse model for resonant transitions in attosecond experiments, Phys. Rev. A 93, 023429 (2016).
- [40] G. Laurent, W. Cao, I. Ben-Itzhak, and C. L. Cocke, Attosecond pulse characterization, Opt. Express 21, 16914 (2013).
- [41] P. Ranitovic, X. M. Tong, C. W. Hogle, X. Zhou, Y. Liu, N. Toshima, M. M. Murnane, and H. C. Kapteyn, Laser-Enabled Auger Decay in Rare-Gas Atoms, Phys. Rev. Lett. **106**, 053002 (2011).
- [42] M. Sabbar, S. Heuser, R. Boge, M. Lucchini, L. Gallmann, C. Cirelli, and U. Keller, Combining attosecond xuv pulses with coincidence spectroscopy, Rev. Sci. Instrum. 85, 103113 (2014).
- [43] E. P. Mansson, D. Guenot, C. L. Arnold, D. Kroon, S. Kasper, J. M. Dahlström, E. Lindroth, A. S. Kheifets, A. L'Huillier, S. L. Sorensen, and M. Gisselbrecht, Double ionization probed on the attosecond timescale, Nat. Phys. 10, 207 (2014).
- [44] J. Ullrich, R. Moshammer, A. Dorn, R. Dörner, L. Ph. H. Schmidt, and H. Schmidt-Böcking, Recoil-ion and electron momentum spectroscopy: Reaction-microscopes, Rep. Prog. Phys. 66, 1463 (2003).
- [45] J.-E. Rubensson, J. Lüning, M. Neeb, B. Küpper, S. Eisebitt, and W. Eberhardt, Photoelectron Soft X-ray Fluorescence Coincidence Spectroscopy on Free Molecules, Phys. Rev. Lett. 76, 3919 (1996).