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# THE BISMUTH ABUNDANCE IN THE HgMn STARS $\chi$ LUPI AND HR 7775 AND IMPROVED ATOMIC DATA FOR SELECTED TRANSITIONS OF Bi i, Bi iI, AND Bi $\mathrm{m}^{1}$ 

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#### Abstract

High-resolution spectra of the chemically peculiar HgMn stars $\chi$ Lupi and HR 7775, obtained with the Hubble Space Telescope/Goddard High Resolution Spectrograph, are investigated for their abundance of bismuth by comparison with LTE synthetic spectrum modeling. HR 7775, previously known from International Ultraviolet Explorer spectra to display strong lines of Bi II, is determined to have bismuth present at an enhancement level of nearly 5 orders of magnitude from the lines Bi if $\lambda \lambda 1436,1902$ and Bi III $\lambda 1423$. The bismuth enhancement for $\chi$ Lupi is found to be near a level of 1.5 dex, and an ionization anomaly between $\mathrm{Bi}^{+}$and $\mathrm{Bi}^{++}$is apparent. HR 7775 abundance enhancements of the heavy elements platinum, $[\mathrm{Pt} / \mathrm{H}]=4.7$ dex, and gold, $[\mathrm{Au} / \mathrm{H}]=3.8$ dex, have also been determined. New laboratory measurements for wavelengths and hyperfine structure patterns of $\mathrm{Bi} \frac{\mathrm{I}}{\mathrm{L}} \mathrm{Bi} I / \mathrm{Bi}$ iII lines are presented, as well as the results of calculations for hyperfine structure constants and oscillator strengths for selected lines of Bi II and Bi III.


Subject headings: atomic data - stars: abundances - stars: chemically peculiar -
stars: individual ( $\chi$ Lupi, HR 7775) - ultraviolet: stars
On-line material: machine-readable tables

## 1. INTRODUCTION

The chemically peculiar (CP) stars of the upper main sequence are renowned for displaying anomalous spectral line strengths for a variety of elements. Of particular note are the enhanced strengths of the rare earth elements in the spectra of the magnetic A-type stars and the very heavy elements $\mathrm{Pt}, \mathrm{Au}, \mathrm{Hg}$, and Tl in the spectra of the nonmagnetic, late $\mathrm{B}, \mathrm{HgMn}$ stars. While radiative diffusion theory (Michaud 1970) has provided a basic framework for study into the origins of anomalous line strengths, additional work must be undertaken to account for the diversity of elemental abundance and isotopic mixture anomalies that are observed in HgMn stars. Recent theoretical work by Seaton $(1997,1999)$ has addressed the behavior of iron group elements in unevolving models. Other modeling

[^0]efforts (Proffitt et al. 1999; Leckrone et al. 1996) have been unable to maintain the great line enhancements over extended periods of time. Thus, temporal evolution may enter into the problem in presently unknown ways.
$\chi$ Lupi (=HD 141556, B9.5p HgMn + A2Vm) has been the subject of extensive study at visible and ultraviolet wavelengths. As part of the $\chi$ Lupi Pathfinder Project (Leckrone et al. 1998, 1999) the ultraviolet high spectral resolution capabilities available on the Hubble Space Telescope (HST) have been exploited. The project goals have included the study of elemental abundances and isotopic mixtures in the atmosphere of one HgMn star in order to provide constraints for the diffusion paradigm or any other theory that proposes to explain the spectral anomalies of late B-type chemically peculiar stars. The choice of $\chi$ Lupi for such a target is predicated upon its extremely sharp-lined spectrum and the anomalous isotopic composition observed at optical wavelengths for the heavy elements platinum and mercury. Its brightness ( $m_{v}=3.95$ ) has also allowed for rather high signal-to-noise ratio ( $\mathrm{S} / \mathrm{N}$ ) levels to be attained with reasonable exposure durations using the Goddard High Resolution Spectrograph (GHRS) on board HST.

HR 7775 (=HD 193452, B9.5p HgMn) represents a logical next step in the overall process of testing the diffusion paradigm since its effective temperature is essentially identical to that of $\chi$ Lupi A, and the spectra of these two stars are similar overall. HR 7775 also displays extremely narrow spectral lines, indicative of low rotational velocity and small atmospheric turbulence. Its surface gravity is, however, slightly greater than that of $\chi$ Lupi A. This may indicate a somewhat less advanced stage of evolution for HR 7775, but the singular trait that has brought attention to HR 7775 is the great enhancement of bismuth lines in its spectrum. Using ultraviolet spectra obtained with the International Ultraviolet Explorer (IUE) satellite, Jacobs \&

TABLE 1
Wavelengths for Bi I

| $\begin{gathered} \lambda_{\mathrm{va}} \mathrm{a}^{\mathrm{a}} \\ (\mathrm{~A}) \end{gathered}$ | Int. | $\underset{\left(\mathrm{cm}^{-1}\right)}{\sigma}$ | Odd Level ${ }^{\text {b }}$ ( $\mathrm{cm}^{-1}$ ) | $J_{\text {odd }}$ | Even Level ${ }^{\text {b }}$ ( $\mathrm{cm}^{-1}$ ) | $J_{\text {even }}$ | $\underset{\substack{\text { calc } \\(\AA) \\(A)}}{ }$ | Comment ${ }^{\text {d }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1685.698. | 70 | 59322.61 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| 1687.055. | 50 | 59274.89 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| 1716.049. | 30 | 58273.39 | 0 | 3/2 | $58273^{\text {e }}$ | $3 / 2^{\text {f }}$ | $\ldots$ |  |
| 1731.050 . | 3 | 57768.41 | 0 | 3/2 | $57767^{\text {e }}$ | 3/2 | $\ldots$ | $\ldots$ |
| 1735.928. | 25 | 57606.08 | 0 | 3/2 | $57607^{\text {e }}$ | 1/2 | $\ldots$ | $\ldots$ |
| 1743.760 . | 50 | 57347.34 |  |  |  |  |  |  |
| 1752.065. | 5000 | 57075.51 | 0 | 3/2 | 57075 | 5/2 | 1752.0757(15) | $\ldots$ |
| 1756.414. | 20 | 56934.19 | 0 | 3/2 | 56934 | 5/2 | 1756.4145(2) | $\ldots$ |
| 1757.587... | 75 | 56896.19 | 0 | 3/2 | 56896 | 3/2 | 1757.5879(16) | $\ldots$ |
| 1767.023... | 1 | 56592.36 | 0 | 3/2 | $56591{ }^{\text {e }}$ | 1/2 | ... | $\ldots$ |
| 1767.737... | 9000 | 56569.50 | 0 | 3/2 | 56569 | 3/2 | 1767.7383(16) | $\ldots$ |
| 1775.254. | 10 | 56329.97 | 0 | 3/2 | 56329 | 3/2 | 1775.2538(2) | $\ldots$ |
| 1788.606 . | 2 | 55909.46 | 11419 | 3/2 | $67327^{8}$ | ? | ... | $\ldots$ |
| 1791.328. | 20 | 55824.51 | 0 | 3/2 | 55824 | 1/2 | 1791.3273(2) | $\ldots$ |
| 1802.626. | 300 | 55474.62 | 0 | 3/2 | 55474 | 5/2 | 1802.6231(2) | $\ldots$ |
| 1804.233. | 20 | 55425.21 | 0 | 3/2 | 55425 | 3/2 | 1804.2302(2) | $\ldots$ |
| 1832.824. | 300 | 54560.61 | 0 | 3/2 | 54560 | 1/2 | 1832.8232(2) | $\ldots$ |
| 1849.498. | 20 | 54068.73 | 11419 | 3/2 | $65483{ }^{\text {e }}$ | 3/2 |  |  |
| 1852.638. | 2000 | 53977.09 | 0 | 3/2 | 53977 | 5/2 | 1852.6392(2) | $\ldots$ |
| 1856.017. | 350 | 53878.82 | 0 | 3/2 | 53878 | 3/2 | 1856.0165(2) | $\ldots$ |
| 1913.666. | 1500 | 52255.72 | 0 | 3/2 | 52255 | 1/2 | 1913.6662(3) | $\ldots$ |
| 1954.706. | 15000 | 51158.59 | 0 | 3/2 | 51158 | 5/2 | 1954.7096(3) | $\ldots$ |
| 1960.049. | 6000 | 51019.13 | 0 | 3/2 | 51019 | 3/2 | 1960.0506(3) | $\ldots$ |
| 2021.801. | 4000 | 49460.85 | 0 | 3/2 | 49460 | 3/2 | 2021.7986(3) | Flag; -0.06; 2021.772 |
| 2062.293. | 150000 | 48489.72 | 0 | 3/2 | 48489 | 5/2 | 2062.2865(3) | Flag; -0.14; 2062.228 |
| 2110.886 | 25000 | 47373.47 | 0 | 3/2 | 47373 | 1/2 | 2110.8858(3) |  |
| 2134.273. | 700 | 46854.36 | 11419 | 3/2 | $58273^{\text {e }}$ | $3 / 2^{\text {f }}$ | ... | $\ldots$ |
| 2165.064 . | 70 | 46188.01 | 11419 | 3/2 | $57607^{\text {e }}$ | 1/2 | $\ldots$ | $\ldots$ |
| 2177.882 . | 450 | 45916.17 | 0 | 3/2 | 45915 | 1/2 | ... |  |
| $2177.895^{\text {h }}$ | 950 | 45915.90 | 0 | 3/2 | 45915 | 1/2 | 2177.8956(3) | $\ldots$ |
| 2177.907. | 500 | 45915.64 | 0 | 3/2 | 45915 | 1/2 | ... | $\ldots$ |
| 2214.820 . | 100 | 45150.40 | 11419 | 3/2 | 56569 | 3/2 | 2214.8188(25) |  |
| 2228.902 . | 900000 | 44865.14 | 0 | 3/2 | 44865 | 3/2 | 2228.9052(4) | $\ldots$ |
| 2231.302 . | 350000 | 44816.88 | 0 | 3/2 | 44816 | 5/2 | 2231.3041(4) | $\ldots$ |
| 2277.261. | 400000 | 43912.40 | 0 | 3/2 | 43912 | 3/2 | 2277.2624(4) |  |
| 2317.946 . | 15 | 43141.64 | 11419 | 3/2 | 54560 | 1/2 | 2317.9484(4) |  |
| 2349.734. | 15 | 42558.01 | 11419 | 3/2 | 53977 | 5/2 | 2349.7338(4) | $\ldots$ |
| 2355.170 . | 100 | 42459.78 | 11419 | 3/2 | 53878 | 3/2 | 2355.1694(4) |  |
| 2401.61. | 400 | 41638.7 | 15437 | 5/2 | 57075 | 5/2 | 2401.6720(29) | Flag; 0.17; 2401.704 |
| 2431.19 ... | 70 | 41132.1 | 15437 | 5/2 | 56569 | 3/2 | 2431.1995(30) | Flag; 0.15; 2431.268 |
| 2448.778 . | 150 | 40836.69 | 11419 | 3/2 | 52255 | 1/2 | 2448.7790(4) | Flag; -0.04 |
| 2497.67 | 5 | 40037.3 | 15437 | 5/2 | 55474 | 5/2 | 2497.6763(4) | Flag; 0.13; 2497.736 |
| 2516.390. | 1500 | 39739.47 | 11419 | 3/2 | 51158 | 5/2 | 2516.3908(4) | Complex; narrow |
| 2525.250. | 4000 | 39600.04 | 11419 | 3/2 | 51019 | 3/2 | 2525.2493(5) | Complex; narrow |
| 2594.73 ... | 40 | 38539.7 | 15437 | 5/2 | 53977 | 5/2 | 2594.7371(5) | Flag; 0.14; 2594.800 |
| 2601.36 .. | 20 | 38441.4 | 15437 | 5/2 | 53878 | 3/2 | 2601.3669(5) | Flag; 0.14; 2601.430 |
| 2628.688. | 150000 | 38041.79 | 11419 | 3/2 | 49460 | 3/2 | 2628.6825(5) | Complex; 0.14 |
| 2697.55. | 40000 | 37070.7 | 11419 | 3/2 | 48489 | 5/2 | 2697.5387(5) | Flag; -0.27; 2697.418 |
| 2731.223. | 20 | 36613.63 | 21660 | 1/2 | $58273^{\text {e }}$ | $3 / 2^{\text {f }}$ | ... | ... |
| $2731.300^{\text {h }}$. | 40 | 36612.60 | 21660 | 1/2 | $58273^{\text {e }}$ | $3 / 2^{\text {f }}$ | $\ldots$ |  |
| 2731.376. | 20 | 36611.58 | 21660 | 1/2 | $58273^{\text {e }}$ | $3 / 2^{\text {f }}$ |  |  |
| 2781.297. | 35000 | 35954.45 | 11419 | 3/2 | 47373 | 1/2 | 2781.2978(5) | Complex; narrow |
| 2781.929. | 5 | 35946.28 | 21660 | 1/2 | $57607^{\text {e }}$ | 1/2 | ... | ... |
| $2782.010^{\text {h }}$ | 10 | 35945.24 | 21660 | 1/2 | $57607^{\text {e }}$ | 1/2 | $\ldots$ | $\ldots$ |
| 2782.090 . | 5 | 35944.20 | 21660 | 1/2 | $57607^{\text {e }}$ | 1/2 | ... |  |
| 2799.47 ... | 100 | 35721.0 | 15437 | 5/2 | 51158 | 5/2 | 2799.4742(5) | Flag; 0.16; 2799.547 |
| 2810.443. | 10000 | 35581.58 | 15437 | 5/2 | 51019 | 3/2 | 2810.4422(6) | Flag; 0.15; 2810.511 |
| 2864.532. | 250 | 34909.72 | 21660 | 1/2 | 56569 | 3/2 | ... |  |
| $2864.628^{\text {h }}$ | 550 | 34908.55 | 21660 | 1/2 | 56569 | 3/2 | 2864.6280(41) |  |
| 2864.708. | 300 | 34907.57 | 21660 | 1/2 | 56569 | 3/2 | ... | $\ldots$ |
| 2884.327. | 3 | 34670.13 | 21660 | 1/2 | 56329 | 3/2 | $\ldots$ |  |
| $2884.427^{\text {h }}$ | 8 | 34668.93 | 21660 | 1/2 | 56329 | 3/2 | 2884.4162(6) | $\ldots$ |
| 2884.487 . | 5 | 34668.21 | 21660 | 1/2 | 56329 | 3/2 | ... | $\ldots$ |
| 2898.814. | 150000 | 34496.87 | 11419 | 3/2 | 45915 | 1/2 | 2898.8159(6) | $\ldots$ |

TABLE 1-Continued

| $\lambda_{\mathrm{vac}}{ }^{\mathrm{a}}$ <br> (A) | Int. | $\begin{gathered} \sigma \\ \left(\mathrm{cm}^{-1}\right) \end{gathered}$ | Odd Level ${ }^{\text {b }}$ $\left(\mathrm{cm}^{-1}\right)$ | $J_{\text {odd }}$ | Even Level ${ }^{\text {b }}$ $\left(\mathrm{cm}^{-1}\right)$ | $J_{\text {even }}$ | $\begin{gathered} \lambda_{\text {calc }^{c}}{ }^{\text {( } \AA)} \end{gathered}$ | Comment ${ }^{\text {d }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2939.136...... | 100000 | 34023.60 | 15437 | 5/2 | 49460 | 3/2 | $\ldots$ | $\ldots$ |
| 2939.156 ${ }^{\text {h }} \ldots \ldots$. | 200000 | 34023.37 | 15437 | 5/2 | 49460 | 3/2 | 2939.1529(6) | $\ldots$ |
| 2939.176....... | 100000 | 34023.14 | 15437 | 5/2 | 49460 | 3/2 | ... | $\ldots$ |
| 2989.88 ........ | 150000 | 33446.2 | 11419 | 3/2 | 44865 | 3/2 | 2989.8909(6) | Flag; -0.05 |
| 2994.20 ........ | 6000 | 33397.9 | 11419 | 3/2 | 44816 | 5/2 | 2994.2090(6) | Flag; -0.05 |
| 3025.50 ........ | 150000 | 33052.4 | 15437 | 5/2 | 48489 | 5/2 | 3025.5018(6) | Complex |
| 3068.557...... | 900000 | 32588.61 | 0 | 3/2 | 32588 | 1/2 | ... | ... |
| $3068.591^{\text {h }} \ldots \ldots$. | 1500000 | 32588.25 | 0 | 3/2 | 32588 | 1/2 | 3068.5934(7) | $\ldots$ |
| 3068.643...... | 600000 | 32587.69 | 0 | 3/2 | 32588 | 1/2 | ... |  |
| $3077.55 \ldots . .$. | 15000 | 32493.4 | 11419 | 3/2 | 43912 | 3/2 | 3077.5542(7) | Flag;-0.06; 3077.527 |
| 3112.996...... | 70 | 32123.39 | $64711^{\text {i }}$ | ? | 32588 | 1/2 | ... | ... |
| $3113.042^{\text {h }} \ldots \ldots$. | 140 | 32122.92 | $64711^{\text {i }}$ | ? | 32588 | 1/2 | $\ldots$ | $\cdots$ |
| 3113.087...... | 70 | 32122.46 | $64711^{\text {i }}$ | ? | 32588 | 1/2 | . | ... |

[^1]Dworetsky (1982) identified seven lines of Bi II and determined an abundance enhancement of nearly 6 orders of magnitude relative to the solar system value. For only one other star, the magnetic chemically peculiar star HR 465 (Cowley 1987), had the detection of bismuth lines been reasonably well grounded prior to the launch of HST.

Guaranteed Time Observer (GTO) GHRS observations were designed to provide spectral data that would address the issues of the bismuth abundance for the ionization stages $\mathrm{Bi}^{+}$and $\mathrm{Bi}^{++}$and line blending in the vicinity of the strongest bismuth lines at ultraviolet wavelengths. The knowledge gained from these observations would then lay the groundwork for future study of bismuth in chemically normal and peculiar stars at ultraviolet wavelengths at lower spectral resolution (i.e., high-dispersion IUE data). However, in order to identify and model properly the bismuth features at the spectral resolution of the GHRS echelle mode, it was deemed necessary to obtain more accurate and extensive atomic data than were previously available. In this paper we present new laboratory wavelengths and hyperfine structures for strong lines of the first three ionization stages of bismuth at satellite ultraviolet wavelengths ( $1200-3300 \AA$ ) along with oscillator strengths calculated under the assumption of core-valence (CV) interaction. We apply these data to the determination of the bismuth abundance for the HgMn stars $\chi$ Lupi and HR 7775.

## 2. WAVELENGTH MEASUREMENTS AND HYPERFINE STRUCTURE

Spectra of Bi I, Bi II, and Bi III were obtained with the 10.7 m normal-incidence vacuum spectrograph at the National Institute of Standards and Technology. The grating was ruled with 1200 lines $\mathrm{mm}^{-1}$ and was blazed at $1200 \AA$ in the first order. The plate factor in the first order was $0.78 \AA$
$\mathrm{mm}^{-1}$. A copper hollow cathode light source containing remnants of sputtered platinum from an earlier experiment and chips of metallic bismuth was operated at a direct current of 400 mA . The carrier gas consisted of a flowing mixture of four parts helium and one part neon at a total pressure of 320 Pa ( 2.4 torr). Photographic exposures ranging in time from 15 s to 60 minutes were made on 101-05 type plates in the region $380-3370 \AA$. Observations were made in the first order with filters to eliminate lines from higher grating orders. Lines of Cu II (Ross 1970) and Pt I, Pt II (Sansonetti et al. 1992) were used as the wavelength standards.

Tables 1-3 present our measured wavelengths and wavenumbers for the lines of $\mathrm{Bi} \mathrm{I}, \mathrm{Bi}$ II, and Bi III, respectively, along with the energy and angular momentum of the combining levels for each classified transition. From the standard deviation of the fits to the standard lines we estimate the uncertainty of the wavelengths (one standard uncertainty level) to be $\pm 0.002 \AA$. The centers of gravity for some complex lines have larger uncertainties and are given with only two decimal places in the tables. The intensities are visual estimates of plate blackening.

The results for Bi i are complicated by the fact that many of the lines appear as partially resolved hyperfine structure (hfs) patterns. In Tables 1-3 we describe the lines as they appear at our laboratory resolving power $(R=\lambda / \Delta \lambda=150$, 000 ). Since the resolving power of the GHRS is somewhat lower ( $R=90,000$ ), the hyperfine structure will appear slightly less well resolved in the stellar spectrum. For lines that appear as flag patterns we give the wavelength of the center of gravity in the main part of the table. In the comments column we note the appearance of the line as a flag and give the total width of the pattern in $\AA$ as well as the wavelength of the leading hyperfine component. Lines with negative widths are degraded to the red. Further details of

TABLE 2
Wavelengths for Bi ii

| $\begin{gathered} \lambda_{\mathrm{ya}}{ }^{\mathrm{a}}{ }_{(\mathrm{A}}^{(\mathrm{A})} \end{gathered}$ | Int. | $\underset{\left(\mathrm{cm}^{-1}\right)}{\sigma}$ | Even Level ( $\mathrm{cm}^{-1}$ ) | $J_{\text {even }}$ | Odd Level ( $\mathrm{cm}^{-1}$ ) | $J_{\text {odd }}$ | Comments ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1058.846 \ldots$ | 300 | 94442.44 | 0 | 0 | 94440 | 1 | $\ldots$ |
| 1085.465 . | 100 | 92126.42 | 17030 |  | 109157 | 2 | $\ldots$ |
| 1097.755 | 25 | 91095.01 | 17030 | 2 | 108126 | 1 | $\ldots$ |
| 1099.174 .. | 300 | 90977.41 | 17030 | 2 | 108007 | 3 | ... |
| 1112.523 . | 120 | 89885.78 | 0 | 0 | 89883 | 1 | $\ldots$ |
| 1116.327. | 20 | 89579.49 | 17030 | 2 | 106611 | 1 | $\ldots$ |
| 1123.517. | 250 | 89006.22 | 13324 | 1 | 102330 | 2 | ... |
| 1129.998 . | 18 | 88495.73 | 17030 | 2 | 105526 | 2 | $\ldots$ |
| 1147.190 | 250 | 87169.52 | 13324 | 1 | 100492 | 1 | $\ldots$ |
| 1163.171 . | 700 | 85971.88 | 17030 | 2 | 103003 | 3 | ... |
| 1167.056 . | 800 | 85685.69 | 13324 |  | 99011 | 2 |  |
| 1172.334 . | 120 | 85299.92 | 17030 | 2 | 102330 | 2 | ... |
| 1186.118 . | 30 | 84308.64 | 17030 | 2 | 101341 | 1 | ... |
| 1198.133 ... | 300 | 83463.19 | 17030 | 2 | 100492 | 1 | ... |
| 1219.813. | 40 | 81979.78 | 17030 | 2 | 99011 | 2 | ... |
| 1225.412 . | 800 | 81605.21 | 13324 | 1 | 94928 | 2 | - ${ }^{\text {a }}$ |
| 1232.792 . | 100 | 81116.68 | 13324 | 1 | 94440 | 1 | Complex |
| 1241.045 . | 5000 | 80577.26 | 0 | 0 | 80575 | 1 | ... |
| 1265.331. | 250 | 79030.70 | 17030 | 2 | 96057 | 3 | ... |
| 1283.715 ... | 3000 | 77898.91 | 17030 | 2 | 94298 | 2 | ... |
| 1306.161 . | 400 | 76560.24 | 13324 | 1 | 89883 | 1 | $\ldots$ |
| 1316.943 | 80 | 75933.43 | ... | ... | ... | ... | New line |
| $1317.066 \ldots$ | 60 | 75926.34 | $\ldots$ | $\ldots$ | $\ldots$ | ... | ... |
| $1317.167 .$. | 50 | 75920.52 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| 1325.450 | 900 | 75446.07 | 13324 | 1 | 88769 | 2 | Complex |
| 1329.444 ... | 600 | 75219.42 | 33936 | 2 | 109157 | 2 | Complex |
| 1347.925 ... | 40 | 74188.10 | 33936 | 2 | 108126 | 1 | ... |
| 1350.068 . | 800 | 74070.34 | 33936 | 2 | 108007 | 3 | ... |
| 1372.609 ... | 800 | 72853.96 | 17030 | 2 | 89883 | , | $\ldots$ |
| 1376.036 ... | 80 | 72672.52 | 33936 | 2 | 106611 | 1 | ... |
| 1393.926 . | 1800 | 71739.82 | 17030 | 2 | 88769 | 2 | $\ldots$ |
| 1396.872 . | 50 | 71588.52 | 33936 | 2 | 105526 | 2 | ... |
| $1436.7768^{\text {c }}$. | 2000 | 69600.233 | 0 | 0 | 69598 | 1 | ... |
| $1436.8205^{\circ}$. | 1700 | 69598.116 | 0 | 0 | 69598 | 1 | $\ldots$ |
| $1436.8564^{\text {c }}$. | 1300 | 69596.377 | 0 | 0 | 69598 |  | ... |
| $1447.914 \ldots$ | 100 | 69064.88 | 33936 | 2 | 103003 | 3 | ... |
| 1455.091. | 3500 | 68724.22 | 13324 | 1 | 82047 | 2 | $\ldots$ |
| 1462.138. | 500 | 68393.00 | 33936 | 2 | 102330 | 2 | $\ldots$ |
| 1486.943 ... | 250 | 67252.07 | 13324 | , | 80575 | 1 | ... |
| 1486.963. | 300 | 67251.17 | 13324 | 1 | 80575 | 1 | $\ldots$ |
| 1502.488 . | 90 | 66556.27 | 33936 | 2 | 100492 | 1 |  |
| 1520.549 ... | 600 | 65765.72 | 13324 | , | 79089 | 2 | Flag; -0.06; 1520.520 |
| 1533.139. | 4000 | 65225.66 | 17030 | 2 | 82255 | 3 | ... |
| 1536.745. | 40 | 65072.60 | 33936 | 2 | 99011 | 2 | ... |
| 1538.037 ... | 250 | 65017.94 | 17030 | 2 | 82047 | 2 | $\ldots$ |
| 1563.649 ... | 100 | 63952.97 | 44173 | 0 | 108126 | 1 | ... |
| 1573.632 . | 20 | 63547.26 | 17030 | 2 | 80575 | 1 | ... |
| 1573.673 ... | 30 | 63545.60 | 17030 | 2 | 80575 | 1 | $\ldots$ |
| 1573.721 ... | 50 | 63543.66 | 17030 | 2 | 80575 | 1 | ... |
| 1591.668 . | 1000 | 62827.17 | 13324 | 1 | 76147 | 2 | $\ldots$ |
| 1591.741 ... | 800 | 62824.29 | 13324 | , | 76147 | 2 | ... |
| 1591.803 ... | 600 | 62821.84 | 13324 | 1 | 76147 | 2 | $\ldots$ |
| 1591.853. | 500 | 62819.87 | 13324 | 1 | 76147 | 2 | ... |
| $1591.891 \ldots$ | 300 | 62818.37 | 13324 | , | 76147 | 2 | ... |
| 1601.602 .. | 100 | 62437.48 | 44173 | 0 | 106611 | 1 | ... |
| 1609.629. | 115 | 62126.12 | 33936 | 2 | 96057 | 3 | Flag; -0.14 |
| 1609.665 . | 100 | 62124.73 | 33936 | 2 | 96057 | 3 | ... |
| 1609.696 ... | 85 | 62123.53 | 33936 | 2 | 96057 | 3 | ... |
| 1609.723. | 70 | 62122.49 | 33936 | 2 | 96057 | 3 | $\ldots$ |
| 1609.748 .. | 60 | 62121.52 | 33936 | 2 | 96057 | 3 |  |
| 1609.762 ... | 70 | 62120.98 | 33936 | 2 | 96057 | 3 | Unresolved tail |
| 1611.358 ... | 2000 | 62059.46 | 17030 | 2 | 79089 | 2 | .. |
| 1691.57 .... | 100 | 59116.7 | 17030 | 2 | 76147 | 2 | Complex; 0.17 |
| 1749.232 ... | 25 | 57167.95 | 44173 | 0 | 101341 | 1 | $\ldots$ |
| 1749.279 .. | 15 | 57166.41 | 44173 | 0 | 101341 | 1 | ... |

TABLE 2-Continued

| $\lambda_{\mathrm{vac}}{ }^{\mathrm{a}}$ <br> (A) | Int. | $\begin{gathered} \sigma \\ \left(\mathrm{cm}^{-1}\right) \end{gathered}$ | Even Level $\left(\mathrm{cm}^{-1}\right)$ | $J_{\text {even }}$ | Odd Level $\left(\mathrm{cm}^{-1}\right)$ | $J_{\text {odd }}$ | Comments ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1749.316.. | 10 | 57165.20 | 44173 | 0 | 101341 | 1 | $\ldots$ |
| 1775.54 | 3 | 56320.9 | 44173 | 0 | 100492 | 1 | Complex |
| 1776.991. | 1500 | 56274.91 | 13324 | 1 | 69598 | 1 | ... |
| 1777.057. | 600 | 56272.82 | 13324 | 1 | 69598 | 1 | $\ldots$ |
| 1777.078. | 600 | 56272.15 | 13324 | 1 | 69598 | 1 | $\ldots$ |
| 1777.122 . | 1000 | 56270.76 | 13324 | 1 | 69598 | 1 |  |
| 1787.406. | 4000 | 55947.00 | 33936 | 2 | 89883 | 1 |  |
| 1791.842 . | 15000 | 55808.49 | 13324 | 1 | 69133 | 0 |  |
| 1823.728. | 2000 | 54832.74 | 33936 | 2 | 88769 | 2 | Complex |
| $1902.341^{\text {d }}$. | 15000 | 52566.81 | 17030 | 2 | 69598 | 1 | Complex; 0.14 |
| 1989.250 . | 3 | 50270.20 | 44173 | 0 | 94440 | 1 | ... |
| 1989.305... | 4 | 50268.81 | 44173 | 0 | 94440 | 1 | $\ldots$ |
| 1989.374. | 5 | 50267.07 | 44173 | 0 | 94440 | 1 | $\ldots$ |
| 2069.598. | 10 | 48318.56 | 33936 | 2 | 82255 | 3 | Complex; 0.09 |
| 2144.105. | 6 | 46639.51 | 33936 | 2 | 80575 | 1 | ... |
| 2144.150. | 8 | 46638.53 | 33936 | 2 | 80575 | 1 | $\ldots$ |
| 2144.203. | 10 | 46637.38 | 33936 | 2 | 80575 | 1 | $\ldots$ |
| 2187.610. | 120 | 45711.99 | 44173 | 0 | 89883 | 1 | $\ldots$ |
| 2214.680 . | 12 | 45153.25 | 33936 | 2 | 79089 | 2 | $\ldots$ |
| 2214.713. | 10 | 45152.58 | 33936 | 2 | 79089 | 2 | $\ldots$ |
| 2214.738. | 9 | 45152.07 | 33936 | 2 | 79089 | 2 | $\ldots$ |
| 2214.760 . | 8 | 45151.62 | 33936 | 2 | 79089 | 2 | $\ldots$ |
| 2368.916.. | 120 | 42213.40 | 33936 | 2 | 76147 | 2 | $\ldots$ |
| 2369.053 . | 110 | 42210.96 | 33936 | 2 | 76147 | 2 | $\ldots$ |
| 2369.170 . | 100 | 42208.87 | 33936 | 2 | 76147 | 2 | $\ldots$ |
| 2369.266 . | 90 | 42207.16 | 33936 | 2 | 76147 | 2 | $\ldots$ |
| 2369.339. | 80 | 42205.86 | 33936 | 2 | 76147 | 2 | $\ldots$ |
| 2480.815. | 8 | 40309.33 | 109904 | 2 | 69598 | 1 | $\ldots$ |
| 2480.905. | 10 | 40307.87 | 109904 | 2 | 69598 | 1 | ... |
| 2481.018. | 12 | 40306.04 | 109904 | 2 | 69598 | 1 | $\ldots$ |
| 2501.758 . | 4 | 39971.89 | 13324 | 1 | 69133 | 0 | $\ldots$ |
| 2501.771. | 5 | 39971.68 | 13324 | 1 | 69133 | 0 | $\ldots$ |
| 2501.794. | 6 | 39971.32 | 13324 | 1 | 69133 | 0 | $\ldots$ |
| 2503.280 . | 10 | 39947.59 | 116089 | 3 | 76147 | 2 | $\ldots$ |
| 2503.384. | 12 | 39945.93 | 116089 | 3 | 76147 | 2 | $\ldots$ |
| 2503.527. | 12 | 39943.65 | 116089 | 3 | 76147 | 2 | Double |
| 2503.692 . | 15 | 39941.02 | 116089 | 3 | 76147 | 2 | Shaded to blue |
| 2503.887 . | 20 | 39937.90 | 116089 | 3 | 76147 | 2 | ... |
| 2714.036.. | 300 | 36845.50 | 115933 | 3 | 79089 | 2 | $\ldots$ |
| 2804.161. | 40 | 35661.29 | 33936 | 2 | 69598 | 1 | $\ldots$ |
| 2804.312 . | 35 | 35659.37 | 33936 | 2 | 69598 | 1 | $\ldots$ |
| 2804.433 .. | 30 | 35657.83 | 33936 | 2 | 69598 | 1 |  |
| 2806.049 .. | 80 | 35637.30 | 116212 | 2 | 80575 | 1 | Complex; 0.06 |
| 2817.733. | 10 | 35489.52 | 105083 | 2 | 69598 | 1 | Perturbed by Pt |
| 2817.900 . | 12 | 35487.42 | 105083 | 2 | 69598 | 1 | ... |
| 2818.082 . | 15 | 35485.13 | 105083 | 2 | 69598 | 1 | $\ldots$ |
| 2937.60 .. | 40 | 34041.4 | 116089 | 3 | 82047 | 2 | Flag; 0.30; 2937.742 |
| 2951.277... | 150 | 33883.64 | 115933 | 3 | 82047 | 2 | ... |
| 3111.756. | 4 | 32136.20 | 108278 | 3 | 76147 | 2 | ... |
| 3111.888 . | 5 | 32134.83 | 108278 | 3 | 76147 | 2 | ... |
| 3112.056... | 8 | 32133.10 | 108278 | 3 | 76147 | 2 | ... |
| 3112.262 . | 11 | 32130.97 | 108278 | 3 | 76147 | 2 | ... |
| $3112.507 \ldots$ | 15 | 32128.44 | 108278 | 3 | 76147 | 2 | $\ldots$ |
| 3117.736... | 10 | 32074.56 | 112645 | 0 | 80575 | 1 | $\ldots$ |
| 3117.829. | 8 | 32073.60 | 112645 | 0 | 80575 | 1 | $\ldots$ |
| $3117.905 \ldots$ | 7 | 32072.82 | 112645 | 0 | 80575 | 1 | $\ldots$ |

[^2]TABLE 3
Wavelengths for Bi iII

| $\begin{aligned} & \lambda_{\mathrm{rac}}{ }^{\text {a }} \\ & (\AA \mathrm{A}) \end{aligned}$ | Int. | $\underset{\left(\mathrm{cm}^{-1}\right)}{\sigma}$ | Odd Level ( $\mathrm{cm}^{-1}$ ) | $J_{\text {odd }}$ | Even Level ( $\mathrm{cm}^{-1}$ ) | $J_{\text {even }}$ | Comments |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1051.787 ....... | 3 | 95076.28 | 0 | 1/2 | 95075 | 1/2 | $\ldots$ |
| $1145.903 \ldots \ldots$. | 3 | 87267.42 | 20788 | 3/2 | 108052 | 1/2 | ... |
| 1145.937 ....... | 2 | 87264.83 | 20788 | 3/2 | 108052 | 1/2 | $\ldots$ |
| $1204.234 \ldots . . .$. | 2 | 83040.34 | 0 | 1/2 | 83038 | 3/2 | $\ldots$ |
| 1204.277 ....... | 1.6 | 83037.37 | 0 | 1/2 | 83038 | 3/2 | $\ldots$ |
| 1204.310 . | 1.2 | 83035.10 | 0 | 1/2 | 83038 | 3/2 | $\ldots$ |
| $1224.617 \ldots . .$. | 150 | 81658.18 | 20788 | 3/2 | 102446 | 5/2 | $\ldots$ |
| 1326.848 ....... | 200 | 75366.58 | 20788 | 3/2 | 96154 | 3/2 | $\ldots$ |
| $1346.088 \ldots . . .$. | 60 | 74289.35 | 20788 | 3/2 | 95075 | 1/2 | $\ldots$ |
| $1346.124 \ldots . . .$. | 50 | 74287.36 | 20788 | 3/2 | 95075 | 1/2 | $\ldots$ |
| $1423.3081^{\text {b }} \ldots \ldots$. | 120 | 70258.857 | 0 | 1/2 | 70254 | 1/2 | $\ldots$ |
| $1423.3565^{\text {b }} \ldots \ldots$ | 90 | 70256.468 | 0 | 1/2 | 70254 | 1/2 | $\ldots$ |
| $1423.4806^{\text {b }}$ | 70 | 70250.343 | 0 | 1/2 | 70254 | 1/2 | ... |
| $1423.5290^{\text {b }} \ldots \ldots$. | 120 | 70247.954 | 0 | 1/2 | 70254 | 1/2 | $\ldots$ |
| 1460.846 ....... | 80 | 68453.49 | 20788 | 3/2 | 89236 | 5/2 | ... |
| 1460.920 | 70 | 68450.02 | 20788 | 3/2 | 89236 | 5/2 | $\ldots$ |
| 1460.985 ....... | 60 | 68446.97 | 20788 | 3/2 | 89236 | 5/2 | ... |
| 1461.038 ....... | 50 | 68444.49 | 20788 | 3/2 | 89236 | 5/2 |  |
| 1461.079 ....... | 40 | 68442.57 | 20788 | 3/2 | 89236 | 5/2 | Perturbed by Pt |
| 1461.112 ....... | 30 | 68441.02 | 20788 | 3/2 | 89236 | 5/2 | ... |
| 1606.343 ........ | 80 | 62253.20 | 20788 | 3/2 | 83038 | 3/2 | $\ldots$ |
| 1606.419 | 70 | 62250.26 | 20788 | 3/2 | 83038 | 3/2 | $\ldots$ |
| $1606.484 \ldots . . .$. | 60 | 62247.74 | 20788 | 3/2 | 83038 | 3/2 | $\ldots$ |
| 1606.535 ....... | 50 | 62245.76 | 20788 | 3/2 | 83038 | 3/2 | $\ldots$ |
| 2021.457. | 6 | 49469.27 | 20788 | 3/2 | 70254 | 1/2 |  |
| $2021.797^{\circ}$ | 5 | 49460.95 | 20788 | 3/2 | 70254 | 1/2 | Blend with Bi I |
| 2073.555 ....... | 8 | 48226.36 | 137455 | 7/2 | 89236 | 5/2 | ... |
| 2073.619 . | 5 | 48224.87 | 137455 | 7/2 | 89236 | 5/2 |  |
| 2073.710 . | 12 | 48222.75 | 137455 | 7/2 | 89236 | 5/2 | Perturbed |
| 2073.828 ....... | 10 | 48220.01 | 137455 | 7/2 | 89236 | 5/2 | ... |
| 2073.950 ....... | 12 | 48217.17 | 137455 | 7/2 | 89236 | 5/2 | $\ldots$ |
| 2074.105 .. | ... | 48213.57 | 137455 | 7/2 | 89236 | 5/2 | Perturbed by Cu |
| 2415.380 ....... | 25 | 41401.35 | 137555 | 5/2 | 96154 | 3/2 | ... |
| 2415.411 ........ | 20 | 41400.82 | 137555 | 5/2 | 96154 | 3/2 | $\ldots$ |
| 2415.436 ....... | 15 | 41400.39 | 137555 | 5/2 | 96154 | 3/2 | Perturbed |
| 2415.448 ....... | 10 | 41400.19 | 137555 | 5/2 | 96154 | 3/2 | Unresolved |
| 2856.238 ....... |  | 35011.09 | 137455 | 7/2 | 102446 | 5/2 | ... |
| 2856.273 ....... | 5 | 35010.66 | 137455 | 7/2 | 102446 | 5/2 | $\ldots$ |
| 2856.319 ....... | 7 | 35010.10 | 137455 | 7/2 | 102446 | 5/2 |  |
| 2856.377 ........ |  | 35009.38 | 137455 | 7/2 | 102446 | 5/2 | $\ldots$ |
| 2856.448 ........ | 12 | 35008.51 | 137455 | 7/2 | 102446 | 5/2 | $\ldots$ |
| 2856.530 ....... | 15 | 35007.51 | 137455 | 7/2 | 102446 | 5/2 | ... |

[^3]the hfs of many of the lines are given by Mrozowski (1942). For some lines we have made use of Mrozowski's measurements for the widths of the patterns.
Precise measurements of the spectrum of Bi I in the infrared using a Fourier transform spectrometer have been reported by George, Munsee, \& Vergès (1985). Based on these observations they gave revised values for some levels of neutral bismuth with an uncertainty estimated to be less than $0.005 \mathrm{~cm}^{-1}$. From their level values we have calculated wavelengths for many of the ultraviolet lines observed in this work. The calculated wavelengths are reported for comparison with our measurements in Table 1. Approximately 20 of the lines reported in Table 1 were observed in absorption by Mathews et al. (1989). These authors estimate the uncertainty of their measurements to be $\pm 0.09 \mathrm{~cm}^{-1}$ and
comment that there is a possible bias in the data toward the negative end of the uncertainty range. This bias is confirmed by our wavelengths, which are systematically shorter than those of Mathews et al. (1989) by approximately $0.003 \AA$.

For Bi II and Bi iII the hfs splittings are greater than for Bi I , and we thus give the wavelengths of all of the observed components. Most of the lines were originally reported by Crawford \& McLay (1934), although a few are newly presented here. Figures 1 and 2 display tracings of the newly acquired photographic plate data for Bi II $\lambda 1436.8$ and Bi III 21423.4, respectively, two of the main lines of astrophysical interest in the present study. In both figures the hyperfine components are clearly resolved. Measurement of each of these components can be made to an estimated uncertainty of $1 \mathrm{~m} \AA$.


Fig. 1.-Microdensitometer trace of the Bi II $6 p^{2}{ }^{3} P_{0}\left[F^{\prime}=9 / 2\right]-6 p 7 s$ ${ }^{3} P_{1}[F]$ transition ( $\lambda 1436$ ) as observed photographically in the laboratory.

## 3. ATOMIC CALCULATIONS

Complex systems with nuclear charge as high as bismuth require a careful treatment of both electron correlation and relativistic effects. Recently, we have investigated different computational approaches (Brage, Leckrone, \& Froese Fischer 1996; Brage, Proffitt, \& Leckrone 1998a, 1999), mainly based on the multiconfiguration Dirac-Fock (MCDF) method (Grant et al. 1980) in the form of the GRASP_VU code (Parpia, Froese Fischer, \& Grant 1996). From this and similar work it is clear that systematic and large-scale calculations are necessary to obtain reliable results. For the ions $\mathrm{Bi}^{+}$and $\mathrm{Bi}^{++}$we have computed both oscillator strengths and hfs constants. For the latter we have applied software developed by Jönsson, Parpia, \& Froese Fischer (1996).


Fig. 2.-Microdensitometer trace of the Bi iII $6 s^{2} 6 p^{2} P_{1 / 2}\left[F^{\prime}\right]-6 s 6 p^{2}$ ${ }^{4} P_{1 / 2}[F]$ transition ( $\lambda 1423$ ) as observed photographically in the laboratory.

### 3.1. The MCDF Method

The codes in the GRASP family are based on the MCDF method (Grant et al. 1980; McKenzie, Grant, \& Norrington 1980). Our approach is commonly referred to as DiracCoulomb, since the Hamiltonian defining the variational method is written as

$$
\begin{equation*}
H_{\mathrm{DC}}=\sum_{i}\left(\alpha_{i} \cdot \boldsymbol{p}_{i} c+\beta_{i} c^{2}-\frac{Z}{r_{i}}\right)+\sum_{i \neq j} \frac{1}{r_{i j}}, \tag{1}
\end{equation*}
$$

with standard notations. The first part is a sum over singleparticle Dirac Hamiltonians, while the second represents the instantaneous Coulomb potential. The trial functions are expansions over configuration state functions (CSFs), $\Phi_{j}\left(\alpha_{j} J\right)$,

$$
\begin{equation*}
\Psi(\gamma J)=\sum_{j} c_{j} \Phi_{j}\left(\alpha_{j} J\right) \tag{2}
\end{equation*}
$$

where $\alpha_{j}$ represents all other quantum numbers needed to define uniquely the CSFs (Grant 1988). The label $\gamma$ for the atomic state function (ASF), $\Psi(\gamma J)$, is usually chosen as the $\alpha_{j}$ of the CSF with largest weight, $\left|c_{j}\right|$ in the expansion above. However, in this paper we will use the same labels as in the experimental investigation, based on the $L S$ coupling, instead of the $j j$ coupling used to construct the relativistic CSFs.

To set up the system of integrodifferential equations according to the MCDF method, we need to define an energy functional to optimize. In this paper we use the extended optimal level (EOL) scheme, where the functional is

$$
\begin{equation*}
F=\frac{\sum_{k}\left(2 J_{k}+1\right) E_{k}\left(\gamma_{k} J_{k}\right)}{\sum_{k}\left(2 J_{k}+1\right)}, \tag{3}
\end{equation*}
$$

i.e., the weighted (with $2 J_{k}+1$, where $J_{k}$ is the total angular momentum) sum of the energies $\left[E_{k}\left(\gamma_{k} J_{k}\right)\right.$ ] of a set of ASFs, defined by the labels $\left\{\gamma_{k} J_{k}\right\}$.

The influence of corrections to the Dirac-Coulomb Hamiltonian, in the form of the Breit interaction, was considered in calculations for similar systems (Brage et al. 1996). It was found that they contribute less than $1 \%$ to the oscillator strengths for heavy ions of low-ionization states.

### 3.2. Computational Strategies

In our earlier work it was shown that in relatively simple systems and for states with low-excitation energies, the systematic restricted active space (RAS) calculations can be used and pushed to a convergence, accounting for a number of different types of correlation. In more complex systems, and for higher excitation energies, this method was modified invoking first-order calculations, where the full interaction matrix was only set up for a subset of the CSFs. As a first step only first-order interaction was included for the large CSF set. By using condensation techniques, where all CSFs with a weight smaller than a certain cutoff are omitted, the size of the calculations can be drastically limited, while still including all important contributions.

In this work we encounter two different ionic systems, $\mathrm{Bi}^{+}$and $\mathrm{Bi}^{++}$. The latter is a three-electron system outside closed core subshells, and we are in this case mainly interested in the lowest odd and even levels. This makes it possible to use the RAS technique with only slight modifications when including CV correlation. The ion $\mathrm{Bi}^{+}$is a
more complex four-valence electron system, and for this system we use a more approximate approach to the handling of the larger number of configurations and hence to a slower convergence as a function of the number of included orbitals.

### 3.3. Calculations for Bi III

For Bi III we are interested in resonance transitions between the terms $6 s^{2} 6 p^{2} P$ and $6 s 6 p^{2} P$. The EOL functional is therefore defined according to the reference states $6 s^{2} 6 p^{2} P_{1 / 2,3 / 2}, 6 s 6 p^{2}{ }^{4} P_{1 / 2,3 / 2,5 / 2}$. From a predefined set of orbitals, usually labeled an active set, we can now generate all possible CSFs under certain constraints, with the same parity and $J$-values as the CSFs in the reference set. By increasing the size of the active set in a systematic way, we may investigate the convergence of our approach. In Table 4 we list the results with different sizes of active sets of orbitals.

The first goal is to investigate the valence correlation, i.e., the correlation between the outer three electrons. We are here able to apply a systematic approach, where the active set is increased in four steps, as shown in Table 4. We can see that the excitation energies do converge, albeit to values that are too low. In a final attempt to model the energy spectrum, we add (CV) correlation, by including CSFs with one hole in the $5 d$ core subshell and four outer electrons. This improves the excitation energies, and the fine structure of the ground term is now in excellent agreement with experiment.

The resulting $g f$-values are given in Table 5. Some instabilities are clear for the first calculations. These can be understood from the fact that the transitions we investigate are basically intercombination lines. In a quasi-relativistic treatment (solving the Schrödinger equation and including Breit-Pauli interaction as perturbations) they would be induced by spin-dependent interaction between the $6 s 6 p^{2}$ ${ }^{4} P$ term and different doublets of the same configuration. The computed oscillator strengths are therefore very sensitive to the relative positions of the terms within the $6 s 6 p^{2}$ configuration. It requires quite a large active set of orbitals to represent this term splitting correctly. In the relativistic approach, this complication is represented by a cancellation of different large contributions to the line strengths of the intercombination transitions. In spite of these complications, it is clear that the valence correlation result, at least for the stronger lines, is approaching convergence.
The $g f$-values can be computed using two different forms for the transition operator, the Babushkin and the Coulomb form. In the nonrelativistic limit these converge to the length and velocity forms, respectively. It is well known that for relatively weak transitions, the convergence of the Coulomb form is very slow. We therefore use the Babushkin form all through our calculations. The $g f$-values do depend on the line strength and the transition energy. As is common in this kind of calculation, we use theoretical line strengths but experimental transition energies.

We give the results for the magnetic dipole and electric quadrupole hfs constants (labeled A and B) in Table 6 and

TABLE 4
Energy Levels in Bi iII

| Active Set | Excitation Energies$\left(\mathrm{cm}^{-1}\right)$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $6 s^{2} 6 p^{2} P$ |  | $6 s 6 p^{2}{ }^{4} P$ |  |  |
|  | $J=1 / 2$ | $J=3 / 2$ | $J=1 / 2$ | $J=3 / 2$ | $J=5 / 2$ |
| Dirac-Fock ${ }^{\text {a }} \ldots \ldots \ldots$. | 0 | 20287 | 62012 | 73484 | 82797 |
| $6 s, 6 p, 6 d, 6 f, 6 g \ldots .$. | 0 | 20228 | 64072 | 80394 | 83223 |
| $7 \mathrm{~s}, 7 \mathrm{p}, 7 \mathrm{~d} \ldots \ldots \ldots \ldots$. | 0 | 20094 | 65008 | 76822 | 83887 |
| $8 s, 8 p, 8 d \ldots \ldots \ldots .$. | 0 | 20091 | 65086 | 76911 | 83944 |
| $9 \mathrm{~s}, 9 p, 9 d \ldots \ldots . .$. | 0 | 20090 | 65100 | 76921 | 83953 |
| Including $\mathrm{CV}^{\text {b }} \ldots \ldots$. | 0 | 20744 | 67525 | 80008 | 87369 |
| Experiment ${ }^{\text {c }} \ldots \ldots \ldots$. | 0 | 20788 | 70254 | 83038 | 89236 |

${ }^{\text {a }}$ Single-configuration Dirac-Fock calculation.
${ }^{\mathrm{b}}$ Core-valence correlation (see text).
${ }^{\mathrm{c}}$ See Table 3.

TABLE 5
Computed ${ }^{\text {a }} g f$-Values for Select Bi iII Transitions

| Active Set | $\begin{gathered} { }^{2} P_{1 / 2}^{o}-{ }^{4} P_{1 / 2} \\ 1423 \AA \end{gathered}$ | $\begin{gathered} { }^{2} P_{1 / 2}^{o}-{ }^{4} P^{3 / 2} \\ 1204 \AA \end{gathered}$ | $\begin{gathered} { }^{2} P_{3 / 2}^{o}-{ }^{4} P_{1 / 2} \\ 2022 \AA \end{gathered}$ | $\begin{gathered} { }^{2} P_{3 / 2}^{o}-{ }^{4} P_{3 / 2} \\ 1606 \AA \end{gathered}$ | $\begin{gathered} { }^{2} P_{3 / 2}^{o}{ }^{4} P^{5 / 2} \\ 1461 \AA \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Dirac-Fock | $6.72 \mathrm{E}-2$ | $1.98 \mathrm{E}-2$ | $5.19 \mathrm{E}-3$ | $1.46 \mathrm{E}-2$ | $2.06 \mathrm{E}-1$ |
| $6 s, 6 p, 6 d, 6 f, 6 g \ldots .$. | $6.15 \mathrm{E}-2$ | $3.72 \mathrm{E}-2$ | $1.01 \mathrm{E}-2$ | $1.36 \mathrm{E}-1$ | $9.33 \mathrm{E}-2$ |
| $7 s, 7 p, 7 d \ldots \ldots . . .$. | $6.56 \mathrm{E}-2$ | $2.73 \mathrm{E}-3$ | $8.71 \mathrm{E}-3$ | $1.24 \mathrm{E}-2$ | $3.19 \mathrm{E}-2$ |
| $8 s, 8 p, 8 d$ | $6.72 \mathrm{E}-2$ | $2.16 \mathrm{E}-3$ | $9.25 \mathrm{E}-3$ | $1.15 \mathrm{E}-2$ | $2.84 \mathrm{E}-2$ |
| $9 \mathrm{~s}, 9 p, 9 d$ | $6.75 \mathrm{E}-2$ | $1.65 \mathrm{E}-3$ | $9.36 \mathrm{E}-3$ | $1.07 \mathrm{E}-2$ | $2.73 \mathrm{E}-2$ |
| CV ${ }^{\text {b }}$ | $6.45 \mathrm{E}-2$ | $2.26 \mathrm{E}-3$ | $6.57 \mathrm{E}-3$ | $1.51 \mathrm{E}-2$ | $6.92 \mathrm{E}-2$ |

[^4]TABLE 6
Hyperfine Structure Constants ${ }^{\text {a }}$ for Bi iII

| Active Set | $6 s^{2} 6 p^{2} P$ |  |  | $6 s 6 p^{2}{ }^{4} P$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $J=1 / 2$ <br> A | $J=3 / 2$ |  | $\frac{J=1 / 2}{\mathrm{~A}}$ | $J=3 / 2$ |  | $J=5 / 2$ |  |
|  |  | A | B |  | A | B | A | B |
| Dirac-Fock . | 13993 | 1186 | -1233 | 41614 | 14378 | -1047 | 14858 | 1346 |
| $6 s, 6 p, 6 d, 6 f, 6 g$. | 13585 | 1334 | -1213 | 42690 | 14034 | -1000 | 14605 | 771 |
| $7 s, 7 p, 7 d \ldots \ldots$. | 13057 | 536 | -1093 | 43553 | 14042 | -1022 | 14355 | 734 |
| $8 s, 8 p, 8 d$ | 13313 | 533 | -1111 | 43377 | 13908 | -1022 | 14262 | 702 |
| $9 \mathrm{~s}, 9 p, 9 d$ | 13204 | 531 | -1103 | 43450 | 13899 | -1021 | 14261 | 706 |
| $\mathrm{CV}^{\text {b }} \ldots \ldots$. | 13502 | 647 | -1146 | 46592 | 14401 | -1024 | 14884 | 662 |
| Experiment...... | $14320^{\text {c }}$ | ... | ... | $51050{ }^{\text {c }}$ | $15000^{\text {d }}$ | ... | $15000^{\text {d }}$ | ... |

a Hyperfine electric dipole (A) and magnetic quadrupole (B) constants presented in units of MHz.
${ }^{\text {b }}$ Including core-valence correlation.
${ }^{\text {c }}$ Measured value from $\lambda 1423$, uncertainty 80 MHz .
${ }^{\text {d }}$ Crawford \& McLay 1934 .
the hyperfine induced wavelength splittings in Table 7. From Table 6 it is clear that the valence correlation calculations have converged to within a few percent. The inclusion of core-valence correlation increases the values of A and B, in most cases, by a fairly small amount. Looking at the splitting in wavelengths, shown in Table 7, experiment and theory agree to within a few percent. This agreement provides additional support for the accuracy of our calculations.

### 3.4. Calculations for $\mathrm{Bi}_{\mathrm{II}}$

The four-electron system of Bi II is an even greater challenge to atomic calculations. Henderson et al. (1996) mea-
sured the lifetimes of some of the upper levels, which makes it possible to make some comparisons. There are no measured branching ratios, however, and as we will see below, the measured lifetimes do lead to some contradictions when compared to our calculations. A number of calculations have been performed for this system (e.g., Biéron, Marcinek, \& Migdalek 1991), and we refer the reader to Henderson et al. (1996) for a more complete discussion.

The ground configuration of $\mathrm{Bi}^{+}$is $6 s^{2} 6 p^{2}$, while the first excited odd levels belong to the $6 s 6 p^{3}, 6 s^{2} 6 p 7 s$, and $6 s^{2} 6 p 6 d$ configurations. We use a technique in which we stepwise include one, two, and three configurations, and finally all configurations as obtained from a multireference set, single

TABLE 7
Hyperfine Structure Splitting for Bi iil

| Transition | $F_{\text {lower }}$ | $F_{\text {upper }}$ | Theoretical $\lambda^{a}$ ( $\AA$ ) | Experimental $\lambda$ <br> (A) |
| :---: | :---: | :---: | :---: | :---: |
| $6 s^{2} 6 p^{2} P_{1 / 2}^{o}-6 s 6 p^{2}{ }^{4} P_{1 / 2} \ldots \ldots$. | 4 | 5 | 1423.3081 | 1423.3081 |
|  | 5 | 5 | 1423.3537 | 1423.3565 |
|  | 4 | 4 | 1423.4655 | 1423.4806 |
|  | 5 | 4 | 1423.5111 | 1423.5290 |
| $6 s^{2} 6 p^{2} P_{3 / 2}^{o}-6 s 6 p^{2}{ }^{4} P_{3 / 2} \ldots \ldots$. | 5 | 6 | 1606.343 | 1606.343 |
|  | 6 | 6 | 1606.346 |  |
|  | 4 | 5 | 1606.414 |  |
|  | 5 | 5 | 1606.417 | 1606.419 |
|  | 6 | 5 | 1606.420 |  |
|  | 3 | 4 | 1606.474 |  |
|  | 4 | 4 | 1606.476 | 1606.484 |
|  | 5 | 4 | 1606.480 |  |
|  | 3 | 3 | 1606.524 | 1606.535 |
|  | 4 | 3 | 1606.526 |  |
| $6 s^{2} 6 p^{2} P_{3 / 2}^{o}-6 s 6 p^{2}{ }^{4} P_{5 / 2} \ldots \ldots$. | 6 | 7 | 1460.846 | 1460.846 |
|  | 5 | 6 | 1460.918 | 1460.920 |
|  | 6 | 6 | 1460.920 |  |
|  | 4 | 5 | 1460.979 |  |
|  | 5 | 5 | 1460.981 | 1460.985 |
|  | 6 | 5 | 1460.984 |  |
|  | 3 | 4 | 1461.029 |  |
|  | 4 | 4 | 1461.032 | 1461.038 |
|  | 5 | 4 | 1461.034 |  |
|  | 3 | 3 | 1461.071 | 1461.079 |
|  | 4 | 3 | 1461.074 |  |
|  | 3 | 2 | 1461.103 | 1461.112 |

[^5]TABLE 8
EOL Functional States for Bi ii

| Parity | $J$ | Level Designation |
| :---: | :---: | :--- |
| Even $\ldots \ldots$ | 0 | $6 s^{2} 6 p^{2}{ }^{3} P_{0}, 6 s^{2} 6 p^{2}{ }^{1} S_{0}$ |
| Even..... | 1 | $6 s^{2} 6 p^{2}{ }^{3} P_{1}$ |
| Even.... | 2 | $6 s^{2} 6 p^{2}{ }^{3} P_{2}, 6 s^{2} 6 p^{2}{ }^{1} D_{2}$ |
| Odd $\ldots \ldots$ | 0 | $6 s^{2} 6 p 7 s{ }^{3} P_{0}$ |
| Odd $\ldots \ldots$ | 1 | $6 s^{2} 6 p 7 s s^{3} P_{1}, 6 s^{2} 6 p 6 d d^{3} D_{1}, 6 s^{2} 6 p 7 s{ }^{1} P_{1}$ |
| Odd $\ldots \ldots$ | 2 | $6 s 6 p^{3}{ }^{5} S_{2}, 6 s^{2} 6 p 6 d^{3} D_{2}, 6 s^{2} 6 p 6 d{ }^{3} F_{2}, 6 s^{2} 6 p 7 s{ }^{3} P_{2}$ |

and double replacement calculation. The multireference set includes all levels with a given $J$-value belonging to the $\left\{6 s^{2} 6 p^{2}, 6 s 6 p^{2} 6 d, 6 p^{4}\right\}$ set for the even configurations and the $\left\{6 s 6 p^{3}, 6 s^{2} 6 p 6 d, 6 s^{2} 6 p 7 s\right\}$ set for the odd. The orbitals are optimized by using the EOL technique, on an energy functional composed of the equally weighted total energies of a reference set of states (Table 8). A separate calculation was performed for each pair of $J$-values. From the reference set, we generated new CSFs by single and double replacements of orbitals to a virtual orbital set, $\{6 s, 6 p, 6 d, 5 f, 7 s\}$. Table 9 gives the resulting oscillator strengths, Table 10 compares our transition rates with previous determinations, and Table 11 gives an example of a hyperfine transition array.

One of the most interesting results of our calculations is related to branching ratios (the ratio of the transition rates of two lines with a common upper level) of two transitions involving the upper level $6 s^{2} 6 p 7 s^{3} P_{1}$. In an earlier treatment of Bi iI lines (Henderson et al. 1996), labeled NICA in Table 10, the predicted branching ratio between the two resonance lines at $1902.31 \AA\left(6 s^{2} 6 p^{2}{ }^{3} P_{2}-6 s^{2} 6 p 7 s^{3} P_{1}\right)$ and $1436.83 \AA\left(6 s^{2} 6 p^{2}{ }^{3} P_{2}-6 s^{2} 6 p 7 s^{3} P_{1}\right)$ was almost unity ( $0.35 /$ 0.34 ). This is in sharp contrast to that predicted from the MCDF calculations presented here (first set of results in Table 4), which gives a value close to $2(0.37 / 0.18)$. This difference is completely attributed to relativistic effects, and

TABLE 9
Computed gf-Values for Bi ii

| $\lambda_{\text {vac }}{ }^{\text {a }}$ <br> (A) | Designation | $\begin{gathered} E_{\text {low }}^{\mathrm{b}} \\ \left(\mathrm{~cm}^{-1}\right) \end{gathered}$ | $g f_{\text {th }}{ }^{\text {c }}$ | $g f_{\text {sc }}{ }^{\text {d }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1112.5 . | $6 s^{2} 6 p^{2}{ }^{3} P_{0}-6 s^{2} 6 p 7 s^{1} P_{1}$ | 0 | 0.08 | .. |
| 1241.0 . | $6 s^{2} 6 p^{2}{ }^{3} P_{0}-6 s^{2} 6 p 6 d^{3} D_{1}$ | 0 | 0.12 |  |
| 1436.8 . | $6 s^{2} 6 p^{2}{ }^{3} P_{0}-6 s^{2} 6 p 7 s^{3} P_{1}$ | 0 | 0.17 | 0.21 |
| 1306.2 | $6 s^{2} 6 p^{2}{ }^{3} P_{1}-6 s^{2} 6 p 7 s^{1} P_{1}$ | 13324 | 0.08 | $\ldots$ |
| 1325.4...... | $6 s^{2} 6 p^{2}{ }^{3} P_{1}-6 s^{2} 6 p 7 s^{3} P_{2}$ | 13324 | 0.34 |  |
| 1486.9 | $6 s^{2} 6 p^{2}{ }^{3} P_{1}-6 s^{2} 6 p 6 d^{3} D_{1}$ | 13324 | 0.055 |  |
| 1455.1 | $6 s^{2} 6 p^{2}{ }^{3} P_{1}-6 s^{2} 6 p 6 d^{3} F_{2}$ | 13324 | 0.65 |  |
| 1520.5 | $6 s^{2} 6 p^{2}{ }^{3} P_{1}-6 s^{2} 6 p 6 d^{3} D_{2}$ | 13324 | 0.007 |  |
| 1591.8..... | $6 s^{2} 6 p^{2}{ }^{3} P_{1}-6 s 6 p^{3}{ }^{5} S_{2}$ | 13324 | 0 |  |
| 1777.1...... | $6 s^{2} 6 p^{2}{ }^{3} P_{1}-6 s^{2} 6 p 7 s^{3} P_{1}$ | 13324 | 0.16 | 0.19 |
| 1791.8 | $6 s^{2} 6 p^{2}{ }^{3} P_{1}-6 s^{2} 6 p 7 s^{3} P_{0}$ | 13324 | 0.30 | 0.31 |
| 1372.6 | $6 s^{2} 6 p^{2}{ }^{3} P_{2}-6 s^{2} 6 p 7 s^{1} P_{1}$ | 17030 | 0.10 |  |
| 1393.9 | $6 s^{2} 6 p^{2}{ }^{3} P_{2}-6 s^{2} 6 p 7 s^{3} P_{2}$ | 17030 | 0.13 |  |
| 1538.0 . | $6 s^{2} 6 p^{2}{ }^{3} P_{2}-6 s^{2} 6 p 6 d^{3} F_{2}$ | 17030 | 0.04 |  |
| 1573.7. | $6 s^{2} 6 p^{2}{ }^{3} P_{2}-6 s^{2} 6 p 6 d^{3} D_{1}$ | 17030 | 0.045 |  |
| 1611.4 | $6 s^{2} 6 p^{2}{ }^{3} P_{2}-6 s^{2} 6 p 6 d^{3} D_{2}$ | 17030 | 0.17 |  |
| 1691.6 | $6 s^{2} 6 p^{2}{ }^{3} P_{2}-6 s 6 p^{3}{ }^{5} S_{2}$ | 17030 | 0.005 |  |
| 1902.3 | $6 s^{2} 6 p^{2}{ }^{3} P_{2}-6 s^{2} 6 p 7 s^{3} P_{1}$ | 17030 | 0.60 | 0.73 |
| 1787.4 | $6 s^{2} 6 p^{2}{ }^{1} D_{2}-6 s^{2} 6 p 7 s^{1} P_{1}$ | 33936 | 0.95 | ... |
| 1823.7 | $6 s^{2} 6 p^{2}{ }^{1} D_{2}-6 s^{2} 6 p 7 s{ }^{3} P_{2}$ | 33936 | 0.001 | $\ldots$ |
| 2078.5 | $6 s^{2} 6 p^{2}{ }^{1} D_{2}-6 s^{2} 6 p 6 d^{3} F_{2}$ | 33936 | 0.008 | $\ldots$ |
| 2144.1 | $6 s^{2} 6 p^{2}{ }^{1} D_{2}-6 s^{2} 6 p 6 d^{3} D_{1}$ | 33936 | 0 |  |
| 2214.7...... | $6 s^{2} 6 p^{2}{ }^{1} D_{2}-6 s^{2} 6 p 6 d^{3} D_{2}$ | 33936 | 0.009 |  |
| 2369.0...... | $6 s^{2} 6 p^{2}{ }^{1} D_{2}-6 s 6 p^{3}{ }^{5} S_{2}$ | 33936 | 0.004 | $\ldots$ |
| 2804.3 . | $6 s^{2} 6 p^{2}{ }^{1} D_{2}-6 s^{2} 6 p 7 s^{3} P_{1}$ | 33936 | 0.01 | 0.01 |
| 2187.6...... | $6 s^{2} 6 p^{2}{ }^{1} S_{0}-6 s^{2} 6 p 7 s^{1} P_{1}$ | 44173 | 0.15 | ... |
| 3933.1...... | $6 s^{2} 6 p^{2}{ }^{1} S_{0}-6 s^{2} 6 p 7 s{ }^{3} P_{1}$ | 44173 | 0.001 | 0.001 |

[^6]TABLE 10
Rates for $6 s^{2} 6 p^{2}-6 s^{2} 6 p 7 s$ Transitions in Bi if

| Transition | $\lambda_{\text {vac }}^{\mathrm{a}}$ <br> (Å) | $\begin{aligned} & \text { Rates } \\ & \left(\mathrm{ns}^{-1}\right) \end{aligned}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Type I ${ }^{\text {b }}$ |  | Type $\mathrm{II}^{\text {c }}$ |  |  |
|  |  | $\mathrm{MCDF}^{\text {d }}$ | $\mathrm{RICA}^{\text {e }}$ | MCDF ${ }^{\text {d }}$ | $\mathrm{RICA}^{\mathrm{e}}$ | NICA ${ }^{\text {f }}$ |
| $6 s^{2} 6 p^{2}{ }^{3} P_{1}-6 s^{2} 6 p 7 s^{3} P_{0} \ldots \ldots$ | 1791.8 | 0.62 | 0.62 | 0.64 | 0.64 | 0.64 |
| $6 s^{2} 6 p^{2}{ }^{3} P_{0}-6 s^{2} 6 p 7 s^{3} P_{1} \ldots \ldots$ | 1436.8 | 0.18 | 0.16 | 0.22 | 0.20 | 0.34 |
| $6 s^{2} 6 p^{2}{ }^{3} P_{1}-6 s^{2} 6 p 7 s^{3} P_{1} \ldots \ldots$ | 1777.1 | 0.11 | 0.10 | 0.13 | 0.13 | 0.10 |
| $6 s^{2} 6 p^{2}{ }^{3} P_{2}-6 s^{2} 6 p 7 s^{3} P_{1} \ldots \ldots$ | 1902.3 | 0.37 | 0.37 | 0.45 | 0.47 | 0.35 |
| $6 s^{2} 6 p^{2}{ }^{1} D_{2}-6 s^{2} 6 p 7 s{ }^{3} P_{1} \ldots \ldots$ | 2804.3 | 0.003 | 0.003 | 0.004 | 0.004 | 0.003 |
| $6 s^{2} 6 p^{2}{ }^{1} S_{0}-6 s^{2} 6 p 7 s^{3} P_{1} \ldots \ldots$ | 3933.1 | 0.0001 | 0.0002 | 0.0001 | 0.0002 | 0.0004 |
| $\operatorname{BR}\left({ }^{3} P_{2} /{ }^{3} P_{0}\right)^{\text {g }} \ldots \ldots \ldots \ldots \ldots \ldots$ | ... | 2.1 | 2.3 | 2.1 | 2.3 | 1.0 |

[^7]TABLE 11
Hyperfine Structure in Bi iI $\lambda 1902.3$

| $F_{l}$ | $F_{u}$ | $\lambda_{\text {vac }}$ <br> $(\AA)$ | $g f$-Value |
| :---: | :---: | :---: | :---: |
| $4.5 \ldots \ldots$ | 5.5 | 1902.265 | 0.016 |
| $5.5 \ldots \ldots$ | 5.5 | 1902.288 | 0.071 |
| $6.5 \ldots \ldots$ | 5.5 | 1902.314 | 0.203 |
| $3.5 \ldots \ldots$ | 4.5 | 1902.325 | 0.045 |
| $4.5 \ldots \ldots$ | 4.5 | 1902.343 | 0.094 |
| $5.5 \ldots \ldots$ | 4.5 | 1902.365 | 0.103 |
| $2.5 \ldots \ldots$ | 3.5 | 1902.374 | 0.087 |
| $3.5 \ldots \ldots$ | 3.5 | 1902.388 | 0.071 |
| $4.5 \ldots \ldots$ | 3.5 | 1902.407 | 0.035 |

the disagreement between the two results initiated a separate study (Curtis et al. 1997), where relativistic effects were added to the method used by Henderson et al. (1996). These methods can only predict branching ratios and rely on experimental lifetimes to deduce the final transition rates. We now discuss the results from these different studies.

With reference to Table 10, if we start by looking at the branching ratios, it is clear that the relativistic effects drastically change the values for some of the levels and that our calculations do agree with the ones by Curtis et al. (1997). If we then look at the lifetimes, we find a good agreement between the experiment by Henderson et al. (1996; 1.61 ns ) and the present calculations ( 1.56 ns ) for the $6 s^{2} 6 p 7 s^{3} P_{0}$ level. On the other hand, for $6 s^{2} 6 p 7 s^{3} P_{1}$, experiment ( 1.24 ns ) and our theory ( 1.50 ns ) differ by about $20 \%$. It is instructive to compare the first set of results in Table 10 (type I, MCDF), which corresponds to ab initio calculations, with the fourth (type II, RICA), which corresponds to experimental lifetime and computed branching ratio. By comparing the relative difference as a function of transition rate magnitude for the four strongest lines, it is clear that the disagreement for the $\lambda 1902$ line stands out as comparatively large. This result is against our common experience that we should do better for stronger than for weaker lines.

In conclusion, we combine experimental lifetimes and theoretical branching ratios to deduce the $g f$-values for our synthetic spectra (see last column of Table 9 and type II MCDF results in Table 10), but we caution against a too high confidence level on the experimental lifetime for the $6 s^{2} 6 p 7 s^{3} P_{1}$ level.

## 4. astronomical data

The stellar spectra were obtained as part of the GHRS GTO programs of D. S. Leckrone (program GTO_6245) and J. C. Brandt (program GTO_6275). All observations utilized the echelle A mode of the GHRS and the Small Science Aperture (SSA), thus maximizing the spectral resolution attainable. Observation rationale and data reduction procedures for $\chi$ Lupi spectra have previously been discussed by Wahlgren et al. (1995). All of the $\chi$ Lupi high-resolution GHRS spectra have been presented by Brandt et al. (1999), along with further details of the observations and data reduction. A scientific summary of the project, including a listing of the abundance results to date, has been presented by Leckrone et al. (1999). Data reduction for HR 7775 spectra followed the same procedures as that for $\chi$ Lupi. All observations were obtained
after the HST First Servicing Mission, in the presence of the COSTAR instrument. An overview of the GHRS HR 7775 ultraviolet data will be provided in a forthcoming paper.

## 5. ABUNDANCE ANALYSES

### 5.1. General Comments

The bismuth abundances were investigated by application of a synthetic spectrum technique, whereby the observed spectra are fitted with spectra computed using the SYNTHE (Kurucz 1993) program. We have previously employed this technique as a means of aiding in line identification, elemental abundance determination, and investigation of heavy-element isotope mixtures in the analysis of $\chi$ Lupi GHRS spectra. The most recent works in this series are those for Sr and Y (Brage et al. 1998b), Zr (Sikström et al. 1999), Pt (Kalus et al. 1998), and Hg (Proffitt et al. 1999). The atomic line data, including the semiempirical line broadening constants, are from the compilation of Kurucz (1993), with limited alterations required to correct obvious inconsistencies between the observational and calculated spectra in the vicinity of the bismuth lines, as well as the new laboratory data presented in this paper. Casual inspection of the figures presented underscores the problems inherent in the use of existing line lists, particularly at vacuum ultraviolet wavelengths: an insufficient number of lines, inaccuracy of the wavelengths, and oscillator strength discrepancies. The elemental abundances for a majority of elements have been determined consistently for both stars ( $\chi$ Lupi, Wahlgren, Adelman, \& Robinson 1994a; HR 7775, Wahlgren et al. 2000), and it is unlikely that incorrect abundances are the cause of opacity excesses or deficiencies. Exceptions to this may arise from physical processes such as non-LTE and diffusion, in particular for lines not arising from the majority ion. Identical line lists were used for both stars when computing the spectra presented in this study.

Comparisons of the observed and calculated spectra are plotted on a normalized scale as determined by a synthetic spectrum technique (Wahlgren 1996). For the spectra containing the Bi iII feature it was not possible to normalize the spectrum in this same manner. The nature of the spectrum, in terms of higher line density and missing line opacity in the calculation, rendered this technique more uncertain than expected. Thus, local normalization was accomplished by synthetic spectrum fitting of iron group element lines and by evaluating the residual flux in the spectrum high points as a fraction of the line-free continuum level. In this manner a flux scale factor was obtained for the location of the bismuth line that would simulate a normalized spectrum.

We began the bismuth analysis by study of the star $\chi$ Lupi. Elemental abundance analyses of this star and HR 7775 have shown them to be remarkably similar, with the glaring exception of strong bismuth lines in the spectrum of HR 7775. A second difference is the binary nature of $\chi$ Lupi, which allows for observable lines from the companion star. At VUV wavelengths saturated lines from the companion will attain no more than a $10 \%$ depth from the continuum level. HR 7775 is part of a multiple-star system, which includes the bright star HR 7776 (located at a distance of $205^{\prime \prime}$ from HR 7775) and a close companion. The latter was observed by the Hipparcos astrometric satellite to be fainter by 3 mag and to lie at a distance of 0 ". 68 from HR 7775. This separation places the companion well outside the 0 ". 25
$\times 0$ " 25 SSA of the GHRS when centered on HR 7775, and we thus treat the spectrum of HR 7775 to be that of a single star. However, we also realize that since the orbit of the faint companion is unknown, so is its location with respect to the GHRS aperture at the time of the observations.

These exceptions notwithstanding, the spectra of these two HgMn stars are very similar, and owing to the great breadth of the bismuth lines arising from hfs, a study of the line blending is best accomplished from the spectrum of $\chi$ Lupi, for which the bismuth lines are weak. Unfortunately, the complexity and richness of the spectrum in the vicinity of $1400 \AA$ does not allow for an unequivocal determination of the bismuth abundance for either star.

In the following sections we discuss lines of Bi II and Bi III, which we were able to identify in our GHRS spectra and model. The search for lines from the Bi I spectrum was hampered by line blending and the paucity of strong Bi I lines in our data sets. None of the strong lines listed in Table 1 are located in our HR 7775 data, while only two such lines ( $\lambda_{\text {vac }}=2062.293$ and $2277.261 \AA$ ) could be investigated in our more extensive $\chi$ Lupi data. Neither line has been considered in the synthetic spectrum calculations presented in the $\chi$ Lupi GHRS spectral atlas (Brandt et al. 1999), where it can be seen that identified features can account for the observed absorption at these wavelengths. As a test of the existence of observable Bi I lines, synthetic spectra were calculated for the solar abundance and a 5.0 dex enhancement for the Bi I $\lambda 2062.293$ line using $g f=0.378$, as determined from the transition probability listed by Wiese \& Martin (1980). A very small difference in the blended feature profile resulted from this large enhancement level, indicating that Bi I lines in the $\chi$ Lupi spectrum would not be noticeable if the bismuth abundance is that indicated by the lines of Bi II and Bi III, and that for the bismuth enhancement determined for HR 7775 the severe line blending will prevent accurate abundance work unless a statistical approach is taken. An interesting aside pertains to the improvement of Bi I wavelengths over previous work. The air wavelength of the ground state $2062.293 \AA$ line is determined to be $\lambda_{\text {air }}=2061.633 \AA$ using the formula for the index of refraction of air by Edlén (1966). The air wavelength for this line, as listed by Moore (1962), is $2061.73 \AA$. This $0.1 \AA$ difference may reflect the difficulty in measuring and presenting the wide nature of the hfs for this line. In the case of the $\chi$ Lupi GHRS spectral atlas the older wavelength would appear to correspond to an unmodeled feature in the spectrum, which was attributed to a line of Pt II by Brandt et al. (1999).

### 5.2. Bismuth in $\chi$ Lupi

Bi II 21436 .-The three hfs components are amply separated in wavelength to be resolved from each other in the GHRS observation. The positions of these components are detectable in Figure 3, which plots the computed spectrum for four bismuth abundance enhancements: $[\mathrm{Bi} / \mathrm{H}]=$ $\log \left(N_{\mathrm{Bi}} / N_{\mathrm{H}}\right)_{\text {Star }}-\log \left(N_{\mathrm{Bi}} / N_{\mathrm{H}}\right)_{\text {Sun }}=0.0$ (solar), $1.4,1.6$, and 1.8. (The solar system [meteoritic] bismuth abundance by number is $\log N_{\mathrm{Bi}}=0.71$ on a scale where $\log N_{\mathrm{H}}=12.00$; Anders \& Grevesse 1989). The features are quite sensitive to the bismuth abundance over this range. An upper limit abundance from the Bi II $\lambda 1436$ line is approximately [ $\mathrm{Bi} /$ $\mathrm{H}]=1.6$ dex. This enhancement is smaller than that obtained by an earlier study (Wahlgren et al. 1994b) from a lower resolution, first-order grating, GHRS observation of


Fig. 3.-Bi II $\lambda 1436$ in $\chi$ Lupi. The GHRS observation (Z2MB010I, $R=86,000$; solid line) is compared with the synthetic spectrum for the cases of solar bismuth abundance (dashed line) and enhancements of the bismuth abundance by $[\mathrm{Bi} / \mathrm{H}]=1.4,1.6$, and 1.8 dex (dotted lines). The locations of the three hfs components are indicated. Other lines of note arise from Pt (unclassified line), Au II, and $\mathrm{S}_{\text {I }}$. The fictitious line introduced in the synthetic spectrum is denoted by a question mark.
the Bi II $\lambda 1902$ feature. Despite the uncertainties in line blending that exist, we cannot exclude the possibility that different abundances are extracted from lines of different excitation levels and ionization stages.

The absorption feature central to the two shorter wavelength Bi iI hfs components remains unidentified. Current line lists preclude this feature from being a very heavy element ( $\mathrm{Pt}, \mathrm{Au}, \mathrm{Hg}, \mathrm{Tl}$ ) or singly ionized iron group elements. To treat this absorption, we have introduced a fictitious line at the wavelength $1436.797 \AA$. When this is done, the entire extended feature is reasonably fitted, although we cannot be certain as to the uniqueness of this treatment. If the abundance of bismuth is less than $[\mathrm{Bi} / \mathrm{H}]=1.5$ dex, then the single fictitious line model would have to be replaced with a more complicated structure of multiple lines.

Other atomic species in this spectral interval are also of note. The strong line S I $\lambda 1436.967$, originating from the ground term, required a decrease in the sulfur abundance of 0.5 dex, to $\log N_{\mathrm{S}}=6.7$, relative to the optical region abundance found from two lines of S II (Wahlgren et al. 1995). This abundance difference may be an effect of non-LTE processes operating in the upper atmospheric levels. Similar discrepancies between abundances derived from ground versus higher terms have been noted at optical wavelengths for lines of $\mathrm{Mg}_{\text {II, }} \mathrm{Sr} \mathrm{II}^{2}, \mathrm{Hg}_{\text {II }}$, and $\mathrm{O}_{\mathrm{I}}$ in HR 7775 (Wahlgren et al. 2000). This line also serves to set the absolute wavelength scale in this region for both $\chi$ Lupi and HR 7775. The heavy-element lines Au II $\lambda \lambda 1436.6086,1436.8681$ and Pt $\lambda 1436.7340$ contribute the majority of absorption observed at these wavelengths in the Figure 3 computed spectrum features. The wavelength and oscillator strength data for the Au II lines are from Rosberg \& Wyart (1997), while the wavelength of the unclassified Pt line is from Reader et al. (1990). We have modeled this line as Pt II with an oscillator strength given by $\log g f=-0.6$ to account for absorption of this feature in the Bi iI line wing. Abundances for Au and Pt in $\chi$ Lupi have been taken from Wahlgren et al. (1995).

Bi II $\lambda 1902$.-The analysis of this line in $\chi$ Lupi has been presented by Wahlgren et al. (1994b). Since that study, we have revised the total $g f$-value of the transition from 0.600
to 0.725 . This change has a small effect upon the previous result, that of lowering the upper limit to the abundance of bismuth from this line by 0.1 dex to $[\mathrm{Bi} / \mathrm{H}]=2.0$ dex. We present the revised oscillator strengths for the individual hfs components in Table 11.

Bi III $\lambda 1423$.-The four-component hfs pattern of this line is also well spaced for detection at the observation spectral resolution. Line blending is a concern for the two inner components, leaving the two outer components to provide a more sensitive indication of abundance for small levels of bismuth enhancement such as that displayed by $\chi$ Lupi. The second hfs component ( $\lambda 1423.3565$ ) is blended with two stronger lines of Fe II $(\lambda \lambda 1423.351,1423.334)$ and an unknown contributor(s). Component three ( $\lambda 1423.4806$ ) is affected by a blend with lines of Fe II ( $\lambda 1423.489$ ), Mn II ( $\lambda 1423.487$ ), and Co II ( $\lambda 1423.499$ ) and a strong unknown line near $1423.46 \AA$. Figure 4 depicts the absorption of these lines after having the oscillator strength for the Fe II line arbitrarily reduced from $\log g f=-2.271$ to -2.771 in order not to violate the observed line profile. The absolute wavelength scale has been set by the well-fitted line Fe II $\lambda 1423.691$, while the equally well-fitted line of comparable strength Cr II $\lambda 1423.807$ was used in this capacity for HR 7775.

The contributions of the less blended components appear to be smaller than predicted by the LTE synthetic spectrum calculated assuming the 1.6 dex enhancement found from our fit to the Bi II $\lambda 1436$ line. Any increased line depth resulting from an enhancement of bismuth is rivaled by the amplitude of noise artifacts. We must therefore conclude that this Bi III line does not support a bismuth enhancement of even as much as 1 dex. Abundance enhancements at a level of 1.6 dex, as derived from the Bi in lines, would produce obvious Bi iII absorption features in Figure 4. This suggests an ionization anomaly of 0.6 dex, and perhaps larger depending upon observed noise levels and the accuracy of the oscillator strengths.

### 5.3. Bismuth in HR 7775

Bi II $\lambda 1436$.- Choice of the best fit is contingent upon several assumptions. Figure 5 compares the observed spec-


Fig. 4.-Bi III $\lambda 1423$ in $\chi$ Lupi. The GHRS observation (Z3650308, $R=82,000$; solid line) is compared with the synthetic spectrum for the cases of solar bismuth abundance (dashed line) and enhancements of the bismuth abundance by $[\mathrm{Bi} / \mathrm{H}]=1.0,1.5$, and 2.1 dex (dotted lines). The four hfs components are indicated. The labeled Fe II $\lambda 1423.691$ line has been used to set the absolute wavelength scale.


Fig. 5.-Bi iI $\lambda 1436$ in HR 7775. The GHRS observation (Z32M0107, $R=86,000$; solid line) is compared with the synthetic spectrum for the cases of solar bismuth abundance (dashed line) and enhancements of the bismuth abundance by $[\mathrm{Bi} / \mathrm{H}]=4.7$ and 4.8 dex (dotted lines). The locations of the three hfs components are labeled.
trum with synthetic spectra calculated for bismuth enhancements $[\mathrm{Bi} / \mathrm{H}]=0.0$ (solar), 4.7 , and 4.8 dex. The spectra have been flux normalized using the entire observation, which extends over $8 \AA$, and synthesized spectra. High points at the level of the synthesized continuum and wellfitted lines do exist in this region, unlike the region at 1423 $\AA$. The wavelengths of the three Bi il components, known to milliangstrom accuracy, agree well with the $\mathrm{S}_{\text {I }}$ wavelength calibration. It is also clear that 4.8 is entirely consistent with the observed line profile while 4.9 would violate the line profile to some degree. The outstanding issue remains the true nature of the unknown blending, which was modeled for $\chi$ Lupi by a fictitious $\lambda 1436.797$ line, and which is modeled here in a similar fashion. We can only assume that the unknown line is likely to behave in a similar manner for both stars since their spectra are so similar. Nevertheless, the wavelength of this line can be seen in Figure 5 to affect the abundance level chosen for bismuth. The bismuth abundance may also be artificially high by exclusion of absorptions from the interstellar medium, which may have a greater influence in HR 7775 than in $\chi$ Lupi as a result of the former being more distant. To account for line blending by lines of platinum and gold, we have determined their abundances of $\left(\log N_{\mathrm{Pt}}=6.5, \log N_{\mathrm{Au}}=4.8\right)$ via synthetic spectrum fitting of GHRS spectra using atomic line data for the strong lines Pt II $\lambda 2144$ (Kalus et al. 1997) and Au II $\lambda 1740$ (Wahlgren et al. 1995).

Bi II $\lambda 1902$.-This feature was analyzed using the hfs component wavelengths presented by Wahlgren et al. (1994b) and the revised $g f$-values listed in Table 11. The red side of the feature profile is affected by blending with the autoionization line of Si II, which has not been included in our modeling. Figure 6 presents the fit to the observed line profile for the three bismuth abundances $[\mathrm{Bi} / \mathrm{H}]=0.0$ (solar), 4.8, and 5.3 dex. The feature appears to be best fitted for an abundance of 5.3. The fit to the blue side of the feature can be altered by the uncertainty of the oscillator strength for the unclassified Pt $\lambda 1902.26$ line. The fit to the redward side is influenced by uncertainties in the $f$-values for the Fe II lines ( $\lambda \lambda 1902.412,1902.418,1902.438)$ and the shape and extent of the unmodeled absorption related to the Si II line. The uneven nature of the Bi II feature trough


Fig. 6.-Bi iI $\lambda 1902$ in HR 7775. The GHRS observation (Z32M010A, $R=94,000$; solid line) is compared with the synthetic spectrum for the cases of solar bismuth abundance (dashed line) and enhancements of the bismuth abundance by $[\mathrm{Bi} / \mathrm{H}]=4.8$ and 5.3 dex (dotted lines). The locations of the hfs components for this transition are denoted, as well as the most obvious blends from an unclassified Pt line, Fe I, Fe II, and the location of the Si II $\lambda 1902.45$ autoionization feature.
may attest to absorption by unmodeled features, as well as to noise in the data. Therefore, our best-fit abundance should be interpreted as an upper limit.

Bi III 21423 .-The four hyperfine components are all observed. Blending with lines noted for the $\chi$ Lupi analysis is now aggravated by the increased strength of the latter. The cobalt oscillator strength was reduced from $\log g f=-2.221$ to -2.600 , in conjunction with use of the solar cobalt abundance, in order that the Co II 21423.499 line does not violate the observed line profile for the case of solar bismuth abundance. The unknown line at $1423.46 \AA$ in the spectrum of $\chi$ Lupi is also present in HR 7775 at a comparable strength.

In addition to blending with unknown lines, the fit is complicated by uncertain damping constants for the radiative and Stark line broadening mechanisms. Neither experimental nor calculated damping constants were found for this transition, and we began the analysis by employing the standard formalisms used by Kurucz (1993). For a bismuth abundance enhancement similar to that derived from the Bi II $\lambda 1902$ line it is clear that the line widths are computed too wide. A reduction in abundance serves to fit better the line wings at the expense of the line core depth and introduces an artificial conflict in ionization balance between $\mathrm{Bi}^{+}$and $\mathrm{Bi}^{++}$. By using the radiative transition probabilities from our calculations, the radiative damping constant is reduced from the classical value of $\log \gamma_{\text {rad }}=$ 9.04 to 8.05 . This result is not unexpected since the radiative decay lifetime for intercombination lines can be longer than for normal allowed transitions. This reduction leads to the discrepancy between the observed and computed line profiles to be reduced by half. Although a further reduction of $\log \gamma_{\text {rad }}$, to approximately 7.0 , could better match the line profile, the resulting lifetime would not agree with the calculations, and we chose not to alter the value derived from the calculation. Instead, to account for the remainder of the line broadening discrepancy, the Stark damping constant was reduced by 1 order of magnitude, from $\log \gamma_{\mathrm{S}}=-5.85$ to -6.85 . Figure 7 reflects the fits when using the original damping constants and the reductions in $\log \gamma_{\text {rad }}$ and $\log \gamma_{\mathrm{s}}$


Fig. 7.-Bi III $\lambda 1423$ in HR 7775. The GHRS observation (Z3650308, $R=82,000$; solid line) is compared with synthetic spectra for the cases of solar system bismuth abundance (dashed line) and an enhancement of $[\mathrm{Bi} / \mathrm{H}]=5.0$ dex in which the radiative and Stark damping constants are classical (dot-dashed line) and altered (dotted lines) values (described in text). Several features in the vicinity of the Bi lines remain unidentified and would lead to an overestimate of the Bi abundance if observed at lower $(I U E)$ spectral resolution.
by 1 order of magnitude. With these revised damping constants the abundance of bismuth is determined to be enhanced by 5.3 dex, which is a similar value to that derived from Bi II $\lambda 1902$. This apparent agreement in abundance between the ions $\mathrm{Bi}^{+}$and $\mathrm{Bi}^{++}$may be strictly fortuitous in light of our LTE analysis, and it may later be shown that the Bi III ground state transition is more affected by non-LTE or diffusion than Bi II $\lambda 1902$. The need for non-LTE physics may also be indicated by the 0.5 dex abundance difference between the ground state transition Bi II $\lambda 1436$ and the Bi II $\lambda 1902$ line.

## 6. CONCLUSIONS

The abundance of bismuth has been investigated in the cool HgMn stars $\chi$ Lupi and HR 7775 by fitting observed spectral line profiles obtained with the HST/GHRS with synthetic spectra computed under conditions of LTE model atmospheres. A summary of our results is presented in Table 12. Of critical importance to the analysis are accurate wavelengths for all hfs components for the transitions studied and a detailed knowledge of line blending. We have addressed the first point by laboratory measurements acquired at an accuracy of $1-2 \mathrm{~m} \AA$ for strong lines of the neutral state and the first two ions of bismuth. Oscillator strengths and hyperfine splitting for select lines of Bi II and Bi iII are presented from calculations.

TABLE 12
Bismuth Abundances ${ }^{\text {a }}$ in $\chi$ LUpi and HR 7775

| Wavelength <br> $(\AA)$ | Ion | $\chi$ Lupi | HR 7775 |
| :---: | :---: | :---: | :---: |
| $1436 \ldots \ldots$. | Bi II | $<2.3$ | 5.5 |
| $1902 \ldots \ldots .$. | Bi II $^{\AA}$ | $<2.7$ | 6.0 |
| $1423 \ldots \ldots$. | Bi III | $<1.7$ | 6.0 |

[^8]For $\chi$ Lupi the enhancement of bismuth above solar levels is constrained to be less than 1.6 dex from Bi II $\lambda 1436$ and 2.0 dex from Bi II $\lambda 1902$. Uncertainties in the treatment of line blending and oscillator strengths alone may account for the difference in these upper limits. The result for $\mathrm{Bi}^{+}$is in contrast with that for $\mathrm{Bi}^{++}$, for which no absorption is apparent from the Bi III $\lambda 1423$ resonance line. Uncertainties in the observation noise level and continuum placement place a loose upper limit on the bismuth abundance to be at an enhancement level of 1 dex. No absorption from Bi III is apparent, and an ionization anomaly between the resonance lines of Bi II $^{2}$ and Bi iII may therefore be as high as 1.5 dex as a result of data noise.

In contrast to $\chi$ Lupi, the spectrum of HR 7775 presents saturated lines for Bi II $\lambda \lambda 1436$ and 1902. A consistent abundance can be derived from these two lines within the uncertainties of line blending and the oscillator strengths. The bismuth enhancement is found to be 5 orders of magnitude above the solar system value. A similar abundance enhancement is found from the Bi III $\lambda 1423$ intercombination line. Therefore, an ionization anomaly is not suggested for HR 7775 as it is for $\chi$ Lupi. However, caution is required in this interpretation because of the uncertain nature of the line damping constants and the need for abundance calculations to be made under non-LTE assumptions. The bismuth enhancement level that we have determined is approximately 1 dex less than that determined by Jacobs \& Dworetsky (1982) from IUE spectra of this star. Our treatment of the hfs components and line blending, the latter resulting from the vastly different spectral resolutions of the IUE and $H S T / G H R S$ data, is likely to account for this difference.

The results of the abundance analysis confirm previous general knowledge of bismuth in $\chi$ Lupi and HR 7775 and provide a more detailed account of the line blending in the vicinity of the resonance lines Bi II $\lambda 1436$ and Bi III $\lambda 1423$. The atomic line data can now serve as templates for a more systematic search for bismuth absorption in other chemically peculiar stars. It is also necessary to investigate additional lines from these ions in the spectrum of HR 7775 to
substantiate suspicions regarding a bismuth ionization anomaly.

The determination of abundance enhancements in HR 7775 from UV transitions for platinum, $[\mathrm{Pt} / \mathrm{H}]=4.7 \mathrm{dex}$, and gold, $[\mathrm{Au} / \mathrm{H}]=3.8$ dex, substantiates similar values from optical region data (Wahlgren et al. 2000). The enhanced abundance peak for the elements $\mathrm{Pt}, \mathrm{Au}, \mathrm{Hg}$, and Tl is very similar for $\chi$ Lupi and HR 7775, yet bismuth provides a markedly different result that requires an investment in theoretical modeling in terms of non-LTE and diffusion processes. However, conducting useful numerical experiments in non-LTE requires additional atomic data. In particular, estimates of photoionization cross sections for the lower levels of Bi I and Bi ir lines, in addition to estimates of transition probabilities for a large number of lines, will allow complex model ions to be constructed.

An investment in acquiring atomic data for bismuth may prove to be particularly rewarding for understanding the CP star phenomenon. Among the HgMn stars the elements mercury and manganese are well known for their line strength enhancements. The spectral behavior of other heavy elements, platinum and gold, for example, also appears linked to that of mercury. Such is apparently not the case for bismuth, as it is only HR 7775 that has been found to display strong bismuth spectral lines among HgMn stars. Under further scrutiny other HgMn stars, such as $\chi$ Lupi, will show small enhancements of bismuth lines. Therefore, strong enhancement of bismuth lines may represent a brief period in the lifetime of a CP star and may thus provide valuable insight into atmospheric structure and dynamics and stellar age. As such bismuth may reveal itself to be a sensitive temporal discriminant of the CP star phenomenon.

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## REFERENCES

Anders, E., \& Grevesse, N. 1989, Geochim. Cosmochim. Acta, 53, 197
Biéron, J. R., Marcinek, R., \& Migdalek, J. 1991, J. Phys. B, 24, 31
Brage, T., Leckrone, D. S., \& Froese Fischer, C. 1996, Phys. Rev. A, 53, 192
Brage, T., Proffitt, C. R., \& Leckrone, D. S. 1998a, ApJ, 513, 524
Bre. 1999, J. Phys. B, 32, 1
Brage, T., Wahlgren, G. M., Johansson, S. G., Leckrone, D. S., \& Proffitt, C. R. 1998b, ApJ, 496, 1051

Brandt, J. C., et al. 1999, AJ, 117, 1505
Clearman, H. E. 1952, J. Opt. Soc. Am., 42, 373
Cowley, C. R. 1987, Observatory, 107, 188
Crawford, M. F., \& McLay, A. B. 1934, Proc. R. Soc. London A, 143, 540
Curtis, L. J., Ellis, D. G., Matulioniene, R., \& Brage, T. 1997, Phys. Scr., 56, 240
Edlén, B. 1966, Metrologia, 2, 71
George, S., Munsee, J. H., \& Vergès, J. 1985, J. Opt. Soc. Am. B, 2, 1258
Grant, I. P. 1988, Methods Comput. Chem., 2, 1
Grant, I. P., McKenzie, B. J., Norrington, P. H., Mayers, D. F., \& Pyper, N. C. 1980, Comput. Phys. Commun., 21, 207

Henderson, M., Curtis, L. J., Ellis, D. G., Irving, R. E., \& Wahlgren, G. M. 1996, ApJ, 473, 565
Jacobs, J. M., \& Dworetsky, M. M. 1982, Nature, 299, 535
Jönsson, P., Parpia, F. A., \& Froese Fischer, C. 1996, Comput. Phys. Commun., 96, 301
Kalus, G., Johansson, S., Wahlgren, G. M., Leckrone, D. S., Thorne, A. P., \& Brandt, J. C. 1998, ApJ, 494, 792
Kurucz, R. L. 1993, Kurucz CD-ROM 18, SYNTHE Synthesis Programs and Line Data (Cambridge: SAO)
Leckrone, D. S., Johansson, S., Kalus, G., Wahlgren, G. M., Brage, T., \& Proffitt, C. R. 1996, ApJ, 462, 937

Leckrone, D. S., Johansson, S. G., Wahlgren, G. M., Proffitt, C. R., \& Brage, T. 1998, in ASP Conf. Ser. 143, The Scientific Impact of the Goddard High Resolution Spectrograph, ed. J. C. Brandt, T. B. Ake, III, \& C. C. Petersen (San Francisco: ASP), 135
Leckrone, D. S., Proffitt, C. R., Wahlgren, G. M., Johansson, S. G., \& Brage, T. 1999, AJ, 117, 1454
Mathews, C. W., Ginter, M. L., Ginter, D. S., \& Brown, C. M. 1989, J. Opt. Soc. Am. B, 2, 1627
McKenzie, B. J., Grant, I. P., \& Norrington, P. H. 1980, Comput. Phys. Commun., 21, 233
Michaud, G. 1970, ApJ, 160, 641
Moore, C. E. 1958, Atomic Energy Levels, Vol. III, Natl. Bur. Std. Circ. 467 (Washington DC: US Gov. Printing Office)
(War. 1962, An Ultraviolet Multiplet Table, Natl. Bur. Std. Circ. 488 (Washington DC: US Gov. Printing Office)
Mrozowski, S. 1942, Phys. Rev., 62, 526
Parpia, F., Froese Fischer, C., \& Grant, I. P. 1996, Comput. Phys. Commun., 94, 249
Proffitt, C. R., Brage, T., Leckrone, D. S., Wahlgren, G. M., Brandt, J. C., Sansonetti, C. J., Reader, J., \& Johansson, S. G. 1999, ApJ, 512, 942
Reader, J., Acquista, N., Sansonetti, C. J., \& Sansonetti, J. E. 1990, ApJS, 72, 831
Rosberg, M., \& Wyart, J.-F. 1997, Phys. Scr., 55, 690
Ross, C. B. 1970, Los Alamos Scientific Laboratory Rep. 4498 (Springfield: National Technical Information Service)
Sansonetti, J. E., Reader, J., Sansonetti, C. J., \& Acquista, N. 1992, J. Res. NIST, 97,1
Seaton, M. J. 1997, MNRAS, 289, 700
$\xrightarrow{-}$ 1999, MNRAS, 307, 1008

Sikström, C. M., Lundberg, H., Wahlgren, G. M., Li, Z. S., Lyngå, C., Johansson, S., \& Leckrone, D. S. 1999, A\&A, 343, 297
Wahlgren, G. M. 1996, in ASP Conf. Ser. 108, Model Atmospheres and Spectrum Synthesis, ed. S. J. Adelman, F. Kupka, \& W. W. Wiese (San Francisco: ASP), 240
Wahlgren, G. M., Adelman, S. J., \& Robinson, R. D. 1994a, ApJ, 434, 349
Wahlgren, G. M., Dolk, L., Kalus, G., Johansson, S., Litzén, U., \& Leckrone, D. S. 2000, ApJ, 539, 908

Wahlgren, G. M., et al. 1994b, ApJ, 435, L67
Wahlgren, G. M., Leckrone, D. S., Johansson, S., Rosberg, M., \& Brage, T. 1995, ApJ, 444, 438
Wiese, W. L., \& Martin, G. A. 1980, Wavelengths and Transition Probabilities for Atoms and Atomic Ions, Part II: Transition Probabilities (Washington DC: US Gov. Printing Office)


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[^1]:    Table 1 is also available in machine-readable form in the electronic edition of the Astrophysical Journal.
    ${ }^{\text {a }}$ Wavelength uncertainty is $\pm 0.002 \AA$ (one standard deviation) except in the case of complex lines for which only two decimal places are given. For these lines the uncertainty is $\pm 0.01 \AA$.
    ${ }^{\mathrm{b}}$ Levels and $J$-values taken from George et al. 1985 except as noted.
    ${ }^{\text {c }}$ Vacuum wavelength calculated from the level values of George et al. 1985.
    ${ }^{\text {d }}$ Comments give appearance of hyperfine structure, width of pattern in $\AA$, and wavelength of leading components in $\AA$, if it is resolved. Positive (negative) widths indicate that pattern is degraded to shorter (longer) wavelengths.
    ${ }^{\text {e }}$ Level taken from AEL (Moore 1958).
    f $J$-value revised from AEL (Moore 1958) based on transition at 2731 Å.
    ${ }^{\mathbf{g}}$ Level from Clearman 1952.
    ${ }^{\text {h }}$ Center of gravity of the resolved components based on their estimated intensities.
    ${ }^{i}$ Level from Mrozowski 1942.

[^2]:    Table 2 is also available in machine-readable form in the electronic edition of the Astrophysical Journal.
    ${ }^{\text {a }}$ Wavelength uncertainty is $\pm 0.002 \AA$ except in the case of complex lines for which only two decimal places are given. For these lines the uncertainty is $\pm 0.01 \AA$.
    ${ }^{\text {b }}$ Comments give appearance of hyperfine structure, width of pattern in $\AA$, and wavelength of leading component in $\AA$, if it is resolved. Positive (negative) widths indicate that the pattern is degraded to shorter (longer) wavelengths.
    ${ }^{c}$ Wavelength uncertainty $\pm 0.0010 \AA$.
    ${ }^{\mathrm{d}}$ Center of gravity calculated from data of Wahlgren et al. 1994b.

[^3]:    Table 3 is also available in machine-readable form in the electronic edition of the Astrophysical Journal.
    ${ }^{\text {a }}$ Wavelength uncertainty is $\pm 0.002 \AA$.
    ${ }^{\mathrm{b}}$ Wavelength uncertainty is $\pm 0.0010 \AA$.
    ${ }^{\mathrm{c}}$ Line not observed owing to blend. Wavelength based on calculated interval from $\lambda 2021.457$ of $8.32 \mathrm{~cm}^{-1}$ derived from the values in Tables 3 and 6. Intensity based on theoretical ratios of the hyperfine components.

[^4]:    ${ }^{a}$ Using ab initio line strengths and experimental wavelengths.
    ${ }^{\mathrm{b}}$ Including core-valence correlation.

[^5]:    ${ }^{\text {a }}$ Shortest wavelength in each transition array affixed to experimental value.

[^6]:    ${ }^{\text {a }}$ Approximate wavelength; exact wavelengths with hyperfine structure are given in Table 2.
    ${ }^{\mathrm{b}}$ Excitation energy of lower state.
    c "Theoretical" gf-value computed using the Babushkin form of line strength and experimental wavelengths.
    d "Scaled" $g f$-value computed using a theoretical branching ratio and experimental lifetime (Hendersson et al. 1996).

[^7]:    ${ }^{\text {a }}$ Approximate wavelength.
    ${ }^{\text {b }}$ Assuming computed lifetimes $\left[\tau\left({ }^{3} P_{1}\right)=1.50 \mathrm{~ns}\right.$ and $\left.\tau\left({ }^{3} P_{0}\right)=1.61 \mathrm{~ns}\right]$.
    ${ }^{\text {c }}$ Assuming measured lifetimes, from Henderson et al. $1996\left[\tau\left({ }^{3} P_{1}\right)=1.24 \mathrm{~ns}\right.$ and $\left.\tau\left({ }^{3} P_{0}\right)=1.56 \mathrm{~ns}\right]$.
    ${ }^{\mathrm{d}}$ Branching ratios from MCDF calculations.
    ${ }^{\mathrm{e}}$ Branching ratios from Relativistic Intermediate Coupling Amplitude calculations by Curtis et al. 1997.
    ${ }^{\mathrm{f}}$ Branching ratios from Nonrelativistic Intermediate Coupling Amplitude calculations by Henderson et al. 1996.
    ${ }^{\mathrm{g}}$ Branching ratio for $6 s^{2} 6 p^{2}{ }^{3} P_{2}-6 s^{2} 6 p 7 s^{3} P_{1}(1902.3 \AA)$ and $6 s^{2} 6 p^{2}{ }^{3} P_{0}-6 s^{2} 6 p 7 s^{3} P_{1}(1436.8 \AA)$

[^8]:    ${ }^{\text {a }} \log N_{\mathrm{Bi}}$ includes solar system value of 0.7 dex.

