

Ship Steering

A Test Example for Robust Regulator Design

Åström, Karl Johan

1981

Document Version: Publisher's PDF, also known as Version of record

Link to publication

Citation for published version (APA): Aström, K. J. (1981). Ship Steering: A Test Example for Robust Regulator Design. (Technical Reports TFRT-7222). Department of Automatic Control, Lund Institute of Technology (LTH).

Total number of authors:

General rights

Unless other specific re-use rights are stated the following general rights apply:

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

• Users may download and print one copy of any publication from the public portal for the purpose of private study or recognise.

- You may not further distribute the material or use it for any profit-making activity or commercial gain
 You may freely distribute the URL identifying the publication in the public portal

Read more about Creative commons licenses: https://creativecommons.org/licenses/

Take down policy

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

CODEN: LUTFD2/(TFRT-7222)/1-009/(1981)

S H I P S T E E R I N G
A TEST EXAMPLE FOR ROBUST REGULATOR DESIGN

K J ÅSTRÖM

DEPARTMENT OF AUTOMATIC CONTROL LUND INSTITUTE OF TECHNOLOGY JUNE 1981

SHIP STEERING

A TEST EXAMPLE FOR ROBUST REGULATOR DESIGN

K.J. ASTROM

Department of Automatic Control Lund Institute of Technology

LUND INSTITUTE OF TECHNOLOGY	Document name Internal report				
DEPARTMENT OF AUTOMATIC CONTROL	Date of issue				
Box 725 S 220 07 Lund 7 Sweden	June 1981 Document number				
	CODEN: LUTFD2/(TFRT-7222)/1-009/(1981)				
Author(s)	Supervisor				
Karl Johan Åström	Sponsoring organization				
	Sportsoft mg of gamzarton				
Title and subtitle	E				
 Ship steering - A test example for robust	regulator design				
Ship becering in test example for lobust	regulator design				
Abstract					
A simple version of the shipsteer design problem for the VDI/VDE theoretical design procedures in problem can also be useful in teach	working group on new automatic control. The				
Key words					
	© F				
Classification system and/or index terms (if any)					
Supplementary bibliographical information					
ISSN and key title	LISBN				
Language Number of pages	Recipient's notes				
English 9 Security classification					

Distribution: The report may be ordered from the Department of Automatic Control or borrowed through the University Library 2, Box 1010, S-221 03 Lund, Sweden, Telex: 33248 Lubbis Lund.

3/81

DOKUMENTDATABLAD RT

1. INTRODUCTION

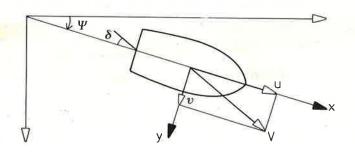
Ship steering is a classical example of control. This note presents the ship steering problem in a simple setting. The control variable is the rudder angle. The purpose of control is to make the ship keep a specified heading or a specified path. The heading angle is measured and sometimes also the yaw rate.

The dynamics of a ship changes with speed, trim and depth. A ship can be unstable in certain operating conditions. The ship is influenced by disturbances due to wind, waves and currents. There are disturbances in the measurements. The heading has a finite resolution. Both the heading and the yaw rate are influenced by the motion of the ship.

There are many different requirements on a control system for ship steering. The system must primarily make it possible to operate the ship in a safe way. This means that the closed loop system must be stable with reasonable damping and response. Secondly it is desired that the steering losses are small. Steering losses are generated if the ship motion deviates too much from a straight line course. The coupling between transverse velocity and turning rate gives an average breaking force. Deflections of the rudder also give rise to losses. A good control system should satisfy the requirements of safe economic operation over all possible operating conditions. The robust control problem is to find a fixed feedback which satisfies all the requirements.

2. SHIP DYNAMICS

The ship dynamics is obtained by applying Newton's equations to the ship's motion. For large ships the motion in the vertical plane can be separated from the other motions. It is customary to describe the motion using the coordinates shown in Fig. 1. The equations of motion are then given by



<u>Fig. 1</u> Coordinates and notations used to describe the equations of motion.

where X and Y are the hydrodynamic forces and N the hydrodynamic torque. These forces and torques are complicated functions of the motion. If they are linearized along a straight line motion the following equations are obtained.

State Equations

The natural state variables are the sway velocity ν_1 the turning rate ν_1 and the heading ν_2 . If ν_1 and ν_2 are solved from (1) the following equations are obtained.

$$\frac{d}{dt} \begin{bmatrix} v \\ r \\ dt \end{bmatrix} = \begin{bmatrix} a & a & 0 \\ 11 & 12 \\ a & a & 0 \\ 21 & 22 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} n \\ r \\ dt \end{bmatrix} + \begin{bmatrix} b \\ 1 \\ b \\ 2 \\ 0 \end{bmatrix} \delta. \tag{2}$$

If normalized coordinates are introduced, where the length unit is the length of the ship and the time unit the time it takes to travel a ships length, the parameters of the state equations are surprisingly similar for many different ships. See Table 1.

The Nomoto Model

The transfer function from rudder to heading is given by

$$G(s) = \frac{K (1+sT_3)}{s (1+sT_1) (1+sT_2)}.$$
 (3)

The parameters K, T, T and T may change considerably $1 \quad 2 \quad 3$

although the parameters of the state model do not change much. See Table 1. In many cases, however, one pole of the model is close to its zero and the model can be simplified to

G (s)
$$\approx ----\frac{k}{s}$$
 (4)

This model is called the Nomoto model. It has the following

Ship	Cargo	Cargo	Tanker	Tanker		Tanker	
Length Breadth	160 22.9	161 23.2	305 47.2	322 54.6		350 60.0	
Draught Draught	9.1 9.1	6.9 8.1	18.5 18.5	21.7 21.7	12.2		9.0
Displ. Speed	23.4 15.2	16.6 15.0	220 16.0	312 16.0	189	389 15.8	172
Prop RPM	74.4	69.0	80.0	100.0	98.4	87.6	87.6
a11 a12	-0.286	-0.335	-0.597 -0.372	-0.279	-0.359	-0.433	-0.448
a21 a22			-3.651 -0.792				
b1 b2	0.108 -0.918		0.103 -0.792		0.150 -1.011		0.144 -1.145
K T1	-1.092 2.743	-3.855	3.511 -10.59		2.660	0.831 -2.882	5.881 -16.91
T2 T3	0.308	0.372		0.443	0.438	0.382	0.447
a	0.427		-0.090				

<u>Table 1</u> - Parameters of statemodels for different ships. The parameters are given in normalized units. The Cargo ship 1 is a series 60 ship with a block coefficient 0.70. Cargo ship 2 is of the Mariner Class.

state representation.

$$\frac{d}{dt} \begin{bmatrix} r \\ \psi \end{bmatrix} = \begin{bmatrix} -a & 0 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} r \\ \psi \end{bmatrix} + \begin{bmatrix} k \\ 0 \end{bmatrix} \delta. \tag{5}$$

The parameter k of the Nomoto model can approximatively be expressed as follows.

$$k = c \left[\frac{V}{L} \right]^2 - \frac{A_R L}{V}$$
 (6)

where L is the length of the ship, ∇ is the displacement , V the ship speed, A is the rudder area and c is a parameter R whose value is approximatively 0.5. The parameter a will

depend on trim, speed and loading. Its sign may change with the operating conditions. Disregarding the speed variations the parameter k does not change much with the operating conditions. The parameter a may however change considerably with the operating conditions. Typical ranges for a tanker under different operating conditions are given in Table 2.

a	k					
0.75	0.37					
0.26	0.38					
0.04	0.18					
-0.11	0.14					
	0.04					

<u>Table 2</u> - Parameters a and k for a tanker under different operating conditions. The parameters are given in normalized units.

3. MODELS OF DISTURBANCES

Wind

The influence of the wind can be described by additional forces and torques. For tankers which are large the net effect is well described as the sum of a constant component and a white noise stochastic processes. This is possible because the ships length (300 m) is typically much larger than the turbulence scale. When winds are taken into account the Nomoto model is changed to

$$\frac{d}{dt} \begin{bmatrix} r \\ \psi \end{bmatrix} = \begin{bmatrix} -a & 0 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} r \\ \psi \end{bmatrix} + \begin{bmatrix} k \\ 0 \end{bmatrix} \delta + \begin{bmatrix} v \\ 0 \end{bmatrix}$$
 (7)

where v = unknown constant + white noise.

The magnitude of the disturbances depends on the sea conditions. The forces are in general quadratic functions of the wind speed. At 18 m/s the wind torque could typically correspond to a velocity of 0.05 deg/s for a tanker.

Waves

The simplest wave model is a periodic force in the equations of motion. In the Nomoto model the waves can be modeled as a disturbance v in (5) where

$$v = v \sin \omega t$$
.

The amplitude v depends on the sea conditions. The

frequency of the disturbance will depend on the angle between the heading and the wave front. The most severe case occurs when the waves are coming from behind the ship. The wave frequency as seen from the ship could then be well inside the bandwidth of the servoloop. Typical values for sea state 5 are

$$v_0 = 0.2^{\circ}s.$$

The frequency can be anywhere between 1-2 rad/s.

Measurements Errors

The heading is normally measured by a gyroscope. The gyro has a finite resolution. Typical values between 0.01 and 0.1 degrees. The gyro can also be disturbed by the ships motion. This contribution to the measurement errors will increase with increasing sea state. The turning rate is measured by a rategyro. This gyro is subject to drift which could be of the order of 10^{-6} rad/s. Due to crosscoupling effects the rategyro may also pick up yawing and heaving motions.

Nonlinearities

The linear model is only valid for small turning rates (r<0.01 deg/s). For larger turning rates it is necessary to take nonlinear effects into account. The major nonlinearity comes from the so called cross flow drag, which give rise to a force proportional to v|v|. If this is taken into account the Nomoto model is changed to

$$\frac{d^2\psi}{dt^2} + f\left(\frac{d\psi}{dt}\right) = k \delta. \tag{8}$$

The function f has the form

$$f(x) = a x + b x |x|$$

See Fig. 2. Case B shown in Fig. 2 correspond to an unstable ship. If the rudder is kept at the midship position, there are three equilibrium values for the turning rate. The value r=0 correspond to a straight line motion. This motion is unstable. The other equilibria correspond to the motions when the ship goes in circles turning starboard or port.

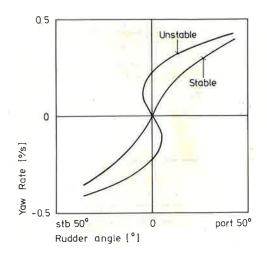


Fig. 2 Steady state yaw rate as a function of the rudder angle.

4. FORMULATION OF CONTROL PROBLEMS

Two simplified control problems are formulated. The first is a stabilization problem the second is an optimization problem.

Safe Operation

Find a feedback law for the Nomoto model (7) which gives satisfactory damping and response and moderate rudder motions. The feedback law could be of the form

$$\delta = \mathsf{K}_{\psi} \Big[\psi_{\mathsf{ref}} - \psi \Big] - \mathsf{k}_{r} r.$$

The rudder angle may never exceed 40 deg. To avoid difficulties with amplification of disturbances and for high rudder motions the gains are limited by

$$|k| \le 10, |k| \le 100 \text{ s.}$$
 (9)

The control problem can thus be formulated as to satisfy these constraints over all operating conditions e.g. those given in Table 2.

Economic Steering .

When the ship is operating on the open seas the major problem is to steer the ship so that the steering losses are minimal. The increase of the drag due to yawing and steering can be determined from the x-component of the equations of motion. Several attempts have been made to obtain a simple loss function which is well suited to evaluate steering

performance. The problem is not settled in the sense that there is universal agreement on the loss function. The following approximation is, however, often used

$$\frac{\Delta R}{R} = \beta \left[\frac{-2}{\psi + r} \frac{-2}{\delta} \right] \tag{10}$$

where ψ^2 and δ^2 are the mean square deviation in heading and rudder angle. R is the drag and ΔR is the increased drag due to steering. The values of β and ϱ depend on the ship. Typical values are $\beta=0.014$ and $\varrho=0.08$ for a tanker and $\beta=0.007$ and $\varrho=0.14$ for a cargo ship of the mariner class. Accepting the approxative loss function it seems resonable to base economic steering on minimazitation of criterion.

$$J = \lim_{T \to \infty} \frac{I}{T} \int \left[\psi^{2}(t) + \varrho \delta^{2}(t) \right] dt.$$
 (11)

5. REFERENCES

- 1. Aström: K.J. and Källström: C.G. (1976): Identification of ship steering. Automatica 12: 9-22.
- 2. Aström, K.J. (1978): Some aspects on the control of large tankers. Proc. Int. Symposium on Systems Optimization and Analysis. IRIA Rocquencourt December, p. 333-353.
- 3. Aström, K.J. (1980): Why use adaptive techniques for steering large tankers. International Journal on Control 32, 689-708.