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On an Interface Between OmSim and IdKit

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<i>Title and subtitle</i> On an Interface Between OmSim and IdKit.		
<i>Abstract</i> <p>This report describes a code-generation interface between OM SIM and ID KIT which has been developed during a nine month post-doctoral visit at the department. The interface consists of command-line tools which transform model equations exported from OM SIM into C-code subroutines that can be used by ID KIT for parameter optimization. The tools make use of batch calls to MAPLE and its packages MACROC and TPLC for symbolic manipulation and code generation. These tools were used in a case-study documented in a companion report.</p>		
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Chapter 1

Introduction

This document is my final progress report and is intended to document the results of my postdoctoral visit at LTH Reglerteknik. While planned as a seven month stay, my visit was extended two months. The original goal of my visit was to further investigate and develop a software interface [1, Ch. 5] between the LTH's model definition tools [2] and KTH's identification tools [3].

In late November 1996, with the then coming visit of Professor Rodney Bell from Australia, a decision was made to investigate parameter optimization of the Åström–Bell drum boiler model [4]. Since then, this has been my primary goal. This has been a collaborative effort with Jonas Eborn, a doctoral candidate at the department, and has yielded one conference paper [5] and a final report [6].

The main components in this report are:

- (i) A final status report on the OMSIM-IDKIT interface. Because of the change in plans, I adopted the “kiss” strategy in developing the software, i.e. do only that needed to get on with the case study. Minimally, this equated to command-line oriented tools for automatic code generation of model equations according to the existing IDKIT model subroutine specification. Development of an interface based on symbolically derived Kalman filter equations has been left incomplete.
- (ii) A concluding discussion of the directions that this work could be continued.
- (iii) Attached as an appendix are listings of the various files discussed in the report.

Acknowledgments

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I would like to thank Docent Sven Erik Mattsson and Professor Karl Johan Åström for the invitation to visit LTH's Department of Automatic Control, and gratefully acknowledges the arrangements made for financial support.

Professionally, I very much enjoyed the interaction with Jonas Eborn. We first met in 1996 at a mini-course in Uppsala and enjoyed talking about OMOLA. I thank him for his patience in acting as my sounding board, and also for his efforts in keeping me attuned to happenings at the department.

Finally, the visit would not have been the same without the attention paid by the charming women of the fifth floor.

Chapter 2

Status of Software Development

A preliminary proposal written in October 1996 listed the following software design issues:

- internal versus external symbolic manipulation/code generation
- continuous and/or discrete-time model support
- level of the interface, i.e. model versus predictor equations
- degree of task automation

Time constraints and the change of focus of my visit have forced a number of design decisions. Rather than diving into the internals of OMSIM's implementation, I elected to proceed developing **modular external tools** and thereby build upon the products of my doctoral research. These tools were developed for **continuous-time models** and the case study involves a continuous-time process. Hence, no effort has been directed toward either discrete-time or hybrid systems.

The shift in emphasis to *using* rather than *developing* tools dictated that I do only that needed for the case study. Minimally this requires generation of the C-language subroutines for IDKIT. Again, time constraints dictated that we stick with the existing **IDKIT subroutine interface for model equations** and forego development of a predictor equation level interface.

As for the degree of task automation, the modular external tools have been packaged, where possible, as **command-line oriented** shell scripts. The only exception is the creation of the OMSIM log file, i.e. the "input" to the automatic code generation. Creation of the log file requires user interaction via the mouse.

2.1 Project Planning and Progress Made

The preliminary proposal's project planning was summarized in a Gant chart and is reproduced here in figure 2.1. Below we reconsider these issues and document the progress made in developing the interface.

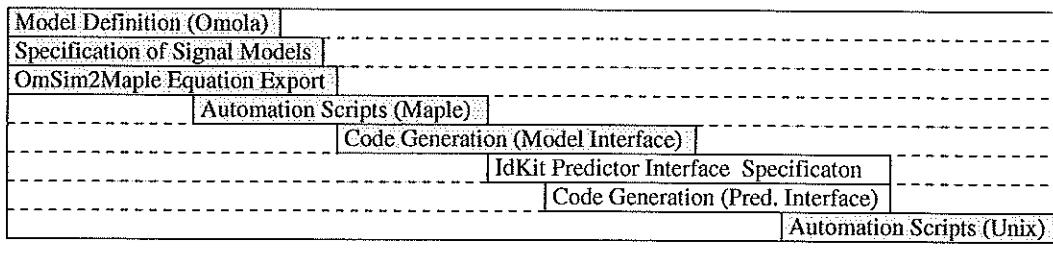


Figure 2.1: Original Gant chart for project planning of an interface between OMSIM and IDKIT. Shading indicates tasks which have been addressed and/or completed.

2.1.1 Model Definition (OMOLA)

Originally this block was included to indicate the need for test cases. In October, I upgraded the test cases in my Ph.D. thesis [1, Ch. 4] to the latest version of OMSIM (3.6). With regard to the drum boiler case study, Jonas Eborn and I have developed a family of OMOLA definitions of the model structure. The complexity of the definitions ranges from first through fifth-order state equations; cf. [4, 7–9]. Class inheritance, the K2 library [10], and OMOLA’s freedom to over-write attributes have proven very useful in making the model definitions concise.

2.1.2 Specification of Signal Models

To facilitate symbolic processing of equations exported from OMSIM, I proposed in my Ph.D. thesis a signal model “wrapper” class library. Its purpose was to standardize the definition of signal model mappings, i.e. the mapping of long hierachic names to short symbolic names. Such a class library proves to be over-kill. The name mappings can be more clearly programmed as a sub-model in the definition of a models simulation interface.

An example of this revised approach is shown in appendix listings A.1 and A.2. When viewed in OMSIM’s graphical editor MED, this sub-model approach takes on the flavor of a “Data Store” block in SystemBuild [11]. Unless a formal equation export mechanism for OMSIM were planned, this simple approach is flexible, practical, and suffices.

2.1.3 OMSIM2MAPLE Equation Export

As part of my thesis work, I developed a shell-script translator which extracted the sorted modeling equations from a log file containing OMSIM’s debug output, specifically, the “Simulation code” and “Parameter part.” In version 3.6 of OMSIM, the “Flat model” debug option was added and the functionality of the initial attribute of variables was abandoned in favor of handling state variable initialization as a discrete event. These changes necessitated changes in the export procedure as well as the translator.

The new export procedure, i.e. creation of the log file, is visualized in figure 2.2. The “Flat model” output contains all information previously groped from the “Simulation code” plus “Parameter part” outputs combined. The new discrete state initialization necessitates including the “Event part” in the OMSIM log file.

The revised version of the shell-script translator, more appropriately named flat-model2maple, is listed in the appendix; see listing A.3, pages 11–12. Although the syntax of OMSIM’s compiled equations (and hence the “Flat model” output) is very close to MAPLE’s syntax, there are some key incongruities. Table 2.1 provides a summary of the translations performed by the shell script.

Syntax	OmSim	Maple
model hierarchy†	m.attribute.attribute	m.attribute_attribute
time derivative†	x', X[1]'	x_prime, X_prime[1]
function names	asin, acos, atan, atan2	arcsin, arccos, arctan, arctan
column vectors	[x1; x2; ...; xn]	[[x1], [x2], ..., [xn]]
matrices	[x11, x12; x21, x22]	[[x11, x12], [x21, x22]]
conditional statement	IF expr1 THEN expr2 ELSE expr3	piecewise(cont.,expr1,expr2,expr3)

Table 2.1: Summary of syntactic incongruities between the OMSIM and MAPLE; syntactic translations marked † indicate arbitrary design choice in the translation.

Conditional Branches The most troublesome translation is conditional statements. OMOLA lacks a tag marking the end of the final branch expression. Since this allows a cleaner nesting of conditional branches, the language is better without one. It is however difficult to program the translation in a shell-script. The following simple example breaks the translator as implemented today:

```
y := m*(IF x < a THEN x-a ELSE IF x < b THEN 0 ELSE x-b) + c;
```

In MAPLE, this would be expressed as follows:

```
y := m*piecewise(0, x<a, x-a, x<b, 0, x-b) + c;
```

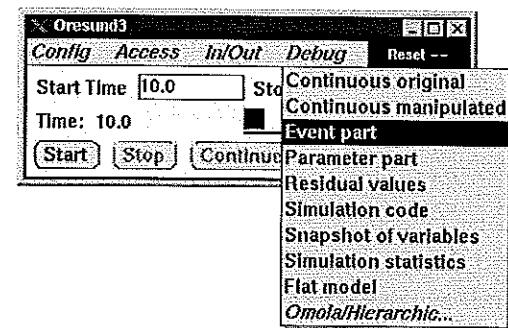
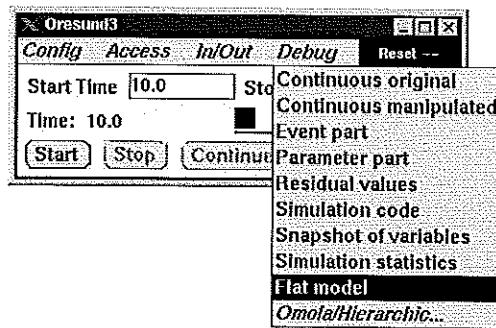


Figure 2.2: The two steps of mouse interaction involved in exporting modeling equations from OMSIM to a log file; after translation using the shell-script in listing A.3, the equations can be loaded into MAPLE.

The problem is simple: the conditional expression appears as a sub-expression in a composite expression. The correct translation of such requires the intelligence of a lexical analyzer. The work-around “solution” has been to avoid programming such composite expressions in OMOLA. This is done simply by introducing interim variables. In the example above, the “solution” looks like this:

```
xx ISA Variable WITH value := IF x < a THEN x-a ELSE IF x < b
    THEN 0 ELSE x-b; END; y := m*xx + c;
```

Note that all these problems existed in the original version of the shell-script translator. They were not as well understood before. Adapting to “Flat model” export greatly simplified the translator. The “Flat model” debug output is a tangible step towards providing a useful high-level equation export mechanism. Nevertheless, the need for a translator to MAPLE persists.

2.1.4 Automation Scripts (MAPLE)

This block refers to the post-processing task that is necessary after one has created the OMSIM log file. The task has been automated as a MAPLE command script. Because the post-processing is an integral part of the code generation, the MAPLE command script is itself embedded as a “here-document” inside a Unix shell script; see lines 17–140 of listing A.4 (pp. 13–15). Note that this command script sources (in line 28) the utility procedures shown in listing A.5 (pp. 16–17).

Event Initialization Switching to OMSIM’s “Flat model” output homogenized the post-processing task somewhat. The bulk of the post-processing, specifically lines 59–118 in listing A.4, is spent manipulating the “Event part” i.e. the *initialization event equations*. Lines 59–71 of the script yield expressions of the initial state conditions in terms of initial input conditions, numerical constants and the model parameters. Similarly, lines 78–111 construct expressions for possible initial event equations, i.e. parameter equations. To un-

derstand how event equations arise, consider the following OMOLA code (taken from the drum-boiler case study):

```

OnEvent Init DO
    % Initialize state variables.
    new(Vwt) := 1/2*Vd + (1-ar0)*Vr + Vdc + dVwt0; new(P) := P0;
    schedule(Start,0.0); % fire immediately after OMSIM's init-solver
END; OnEvent Start DO
    % Initialize variables dependent upon the initial conditions
    new(ar0) := ar; new(qct0) := qct; new(qfw0) := qfw; new(qr0) :=
    qr; new(gs0) := gs; new(rs0) := rs; new(rw0) := rw; new(Vwd0)
    := Vwd-Tsd*(hw-hfw)*qfw/rs/hc; END;

```

During the built-in `Init` event, the two state variables are initialized; note that one state is parameterized. During the scheduled `Start` event, eight variables are initialized, capturing the initial values of these signals. Although only `Vwd0` appears to be parameterized, all are parametric functions. These event equations depend solely on the values of the model parameters, the initial input and state conditions.

It should be emphasized that the *export of event equations from OMSIM is limited to initialization events*. Including the “Event part” in the OMSIM log file is necessary to export state variable initialization. Exporting the initialization events is an added benefit. The exported equations do remain however completely continuous-time.

2.1.5 Code Generation (Model Interface)

Automatic encoding of OMSIM model equations according to the IDKIT model subroutine specifications has been implemented. This work is an extension of the TPLC package for MAPLE [1, App. C] which provides code generation according to the Simulink SimStruct S-function subroutine interface [12]. TPLC stands for Template-C. The package was strongly inspired by the template programming language behind AutoCode [13] from Integrated Systems. Architecturally, this package is built on top of the MACROC share-ware package for MAPLE [14].

The newly developed code generation template for IDKIT is included in the appendix; see listing A.6, pp. 18–24. Half of the code (lines 31–269) is spent processing the model equations, checking for errors, and constructing lists of C pre-processor (CPP) definitions and include files. The code generation template, i.e. MACROC definitions of IDKIT subroutines, is in lines 277–433. Processing the template using the MACROC code generator occurs in line 436. The usage of the code generation template (listing A.6) is shown in listing A.4; see lines 145–168 on page 15.

Sub-Expression Optimization One may wonder “what sets code generation using MAPLE and MACROC apart from AutoCode [13] and the Real Time Workshop [15] from MathWorks?” The answer is *sub-expression optimization* [14]. Optimal numerical computation of a set of equations is achieved by collecting interim variables, i.e. common sub-expressions, evaluating them once, and re-using the computed values. In MAPLE, the deduction of these common sub-expressions is performed by the `optimize` package [16].

The result of using MAPLE and MACROC is best shown by example. Consider the implicit third-order state equations from the Åström-Bell drum boiler model [4]:

$$\begin{bmatrix} e_{11} & e_{12} & 0 \\ e_{21} & e_{22} & 0 \\ 0 & e_{32} & e_{33} \end{bmatrix} \begin{bmatrix} \frac{\partial}{\partial t} V_{wt} \\ \frac{\partial}{\partial t} P \\ \frac{\partial}{\partial t} x_r \end{bmatrix} = \begin{bmatrix} q_{fw} - q_s \\ Q + h_{fw} q_{fw} - h_s q_s + \Delta_{geb} \\ -h_c x_r q_{dc} + Q + \Delta_{reb} \end{bmatrix} \quad (2.1)$$

Solving explicitly for the state derivatives, we have:

$$\begin{bmatrix} \frac{\partial}{\partial t} V_{wt} \\ \frac{\partial}{\partial t} P \\ \frac{\partial}{\partial t} x_r \end{bmatrix} = \begin{bmatrix} \frac{(Q + h_{fw} q_{fw} - h_s q_s + \Delta_{geb}) e_{12} + (-q_{fw} + q_s) e_{22}}{-e_{11} e_{22} + e_{12} e_{21}} \\ \frac{(Q + h_{fw} q_{fw} - h_s q_s + \Delta_{geb}) e_{11} + (-q_{fw} + q_s) e_{21}}{-e_{11} e_{22} + e_{12} e_{21}} \\ \frac{-h_c x_r q_{dc} + Q + \Delta_{reb} - e_{32} (\frac{\partial}{\partial t} P)}{e_{33}} \end{bmatrix} \quad (2.2)$$

Specifically, note the dependency of the third state equation on $\frac{\partial}{\partial t} P$, the time-derivative of pressure. An excerpt from the output of the TPLC code generation template is shown in the appendix listing A.7, pp. 25–26. Lines 22–79 of the listing show the computation of the common sub-expressions. Lines 80–90 perform the actual computation of the state derivatives.¹ As in equation 2.2 above, notice how the expression for $\frac{\partial}{\partial t} P (= t116*t111)$ reappears in the computations; look at lines 85 and 89 respectively in the listing. In these lines, $t111$ corresponds to the denominator expression $-e11 e22 + e12 e21$.

The explicit formulation in equation 2.2 is the most compact solution for the system of state equations and corresponds the result generated by the OMSIM compiler. As shown above, this is also the result yielded using MAPLE for code generation. However fortunate, this conclusion is contrary to what I thought in mid-April this year. The reason has to do with complexity introduced through multiple realizations [1, Ch. 4] and the translation of (nested) branch statements to (nested) piecewise functional statements.

Conditional Branches (revisited) As implemented today, my approach to code generation is to take the sorted OMSIM model equations and translate them into MAPLE assignment statements. When loaded into the MAPLE interpreter, this leads to an automatic substitution of the sorted definitions. The explicit state equations are thereby constructed and the sorted ordering provided by OMSIM is lost.

In complex cases, such as the drum boiler model, this approach leads to extremely large composite expressions. As demonstrated by listing A.7, MAPLE's optimize facility can handle the complex job of reconstructing the (lost) sorted information. However, the facility does have its limitations.

As mentioned above, in mid-April, I believed these limitations (i.e. the loss of information) to be more of a problem than they are. The problem manifested itself as follows:

- (i) Code generation was only possible on the department's most powerful computer, Bellman, equipped with 128 MByte of RAM memory.
- (ii) Processing times were on the order of two minutes.
- (iii) Although the resulting numerical code functioned properly, it seemed extremely complex for “optimized” code.

The cause of the problem turns out to be the complexity introduced by conditional statements. Consider the following OMOLA code:

```
value := IF Sw < 1 THEN hypothesis[1] ELSE IF Sw < 2 THEN
    hypothesis[2] ELSE IF Sw < 3 THEN hypothesis[3] ELSE
    hypothesis[4];
```

The output of the shell-script translator (listing A.3) is then:

```
value := piecewise( 0, Sw<1, hypothesis[1], piecewise( 0, Sw<2,
    hypothesis[2], piecewise( 0, Sw<3, hypothesis[3],
    hypothesis[4] ) ) );
```

Note the nesting of the piecewise operators. This functional nesting aggravates the job of the optimize facility. Common sub-expressions are found by recursively comparing the branch arguments of the functional operators. At each level, the first hypothesis is compared against a functional expression. If each of the hypotheses above represents a complex composite expression, then the comparisons fail (i.e. optimize fails to dissect the complexity).

Before revealing the work-around “solution”, it should be mentioned that this problem could have been avoided (at least to some extent). The complexity is compounded by the simple approach taken in translating from OMSIM to MAPLE. The formal syntax of MAPLE's piecewise operator is as follows:

```
piecewise( c_1, f_1, c_2, f_2, ..., c_n, f_n, f_(n+1) )
```

Hence, a better translation from OMOLA to MAPLE, which avoids the unnecessary nesting, would be:

```
value := piecewise( 0, Sw<1, hypothesis[1], Sw<2, hypothesis[2],
    Sw<3, hypothesis[3], hypothesis[4] );
```

The simplistic approach taken in the translation was necessitated by the limitations of the lexical logic that can be implemented in a shell-script.

¹The first four states in the IDKIT model belong to stochastic disturbance models not shown above.

Fixed Realization Compilation The work-around to the complexity problem is to “hard-wire” the value of the realization switches prior to model compilation. Specifically, the parameterized definition of the switching parameter is programmed as

```
Sw TYPE STATIC Real := 1; % Hard-wired during compilation.
```

rather than:

```
Sw ISA Parameter WITH default := 1; END; % Modifiable after compilation.
```

With the switching parameter Sw hard-wired, conditional branches are eliminated automatically by the OMSIM compiler. The chief disadvantage of this “solution” is that one cannot switch between realizations after compilation. One must manually edit the OMOLA source code *before compilation* and equation export.

By using the OMSIM compiler to eliminate the realization branches, we totally circumvent the problems MAPLE’s optimize has during code generation. With this concession of convenience, MAPLE’s memory requirements during code generation decrease drastically. For the most complex drum boiler model (sixth-order), execution times drop to 10–15 seconds on a 120 MHz Pentium running Linux and equipped with 24 MByte RAM.

Finally, we note that the concession of hard wiring realizations before code generation is necessary for another reason. If one wishes to derive predictor equations from the OMSIM model equations, fixing the active realization is necessary because of the symbolic differentiation involved in the derivation. Automatic derivation of first-order EKF predictor equations is demonstrated in lines 157–160 of listing A.4, page 15; cf. [1, App. C].

2.1.6 IDKIT Predictor Interface Specification

Creating a new code generation template is relatively easy using the MACROC and TPLC packages. However, defining a new application interface requires deeper thought. For this reason, and because of the change of focus of my visit at LTH, I have not developed a specification for the predictor equation interface for IDKIT. In the Gant chart on page 2, this remains one of the un-shaded blocks, i.e. work left incomplete.

2.1.7 Code Generation (Pred. Interface)

Without the interface specification, it is not possible to develop the code generation template. Hence, the Simulink S-function code generation template remains the only support for predictor equations derived from OMSIM model equations.

2.1.8 Automation Scripts (Unix)

To make code generation as automatic as possible, the steps of:

- (i) OMSIM log file translation,
- (ii) MAPLE post-processing of the equations, and
- (iii) MAPLE code generation,

have been embedded within a single Unix shell-script; see listing A.4, pp. 13–15. The command script is simple to use; it takes no arguments. One merely executes it in the directory where the OMSIM log file resides. If successful, the script will create two files in the same directory:

model.c — a subroutine module for use with IDKIT,

Smodel.c — a Simulink S-function for Matlab.

The results of running the script are logged in two files: prep.c and codegen.log. These logs can be useful in diagnosing problems, should they arise.

Chapter 3

Conclusion

A fully functional interface between OMSIM and IDKIT has been designed, prototyped and tested. The interface consists of tools for translation of model equations exported from OMSIM into C-language subroutines—the format of the equations required by IDKIT. With these subroutines, computer-aided parameter optimization of OMOLA models becomes possible. The tools have been tested and extensively used in a case study. A companion report [6] documents these experiences.

Time constraints forced the decision to only develop tools for IDKIT’s existing subroutine interface, i.e. for the model equations. Plans had included the development of a subroutine interface for predictor equations, i.e. an extended Kalman filter derived from the model equations. The chief purpose of such an interface would be to allow efficient and proper treatment of numerically stiff systems.

3.1 Directions for Continued Development

As I see it, there exist two distinct directions to continue this work. One is to continue developing modular external tools as done here. Were someone to do this, things to prioritize would be:

- (i) finalizing a subroutine specification for an IDKIT predictor equation interface;
- (ii) implementing code generation for such a subroutine interface.

The other direction would be to develop tools internally within OMSIM and the realm of the CACE project. Topics for study would be:

- (i) investigate how the symbolic derivation of the Kalman filter equations, and code generation, could be implemented utilizing the sorted equations provided by OMSIM;
- (ii) finalizing a specification for *high-level* equation export, i.e. define a nonlinear control data object (CDO).

Appendix A

Listings

A.1 Model Definition and Equation Export

```
1  SignalModelMapping ISA Base::Model WITH
2      Graphic ISA super::Graphic WITH
3          bitmap TYPE String := "SignalModelMapping"; x_pos := 250; y_pos := 300;
4      END;
5      input_signals:
6          U, U0, Wv, Wy ISA Std::VectorVar;
7      state_signals:
8          X ISA Std::VectorVar;
9      output_signals:
10         Y ISA Std::VectorVar;
11     data_store:
12         PM ISA Std::MatrixVar;
13         Nan ISA Parameter;
14     END;
```

Listing A.1: DrumBoller/SignalModelMapping.om—An Omola class that defines the signal-model name mapping required by the equation export utilities.

```

1  Oresund2 ISA DrumBoiler::OresundSimIC WITH
2
3      Boiler ISA DrumBoiler::Boiler2FM;
4
5  equation_export:
6      SMM ISA DrumBoiler::SignalModelMapping WITH
7      input_signals:
8          U.n := 5; U := [qs1; qs2; qf; qfw; Tfw ];
9          U0.n := 5; U0 := [qs10; qs20; qf0; qfw0; Tfw0];
10         Wv.n := 4; Wv := [CN1; CN2; CN3; CN4];
11         Wy.n := 2; Wy := [DN1; DN2];
12     output_signals:
13         Y.n := 2; Y := [dp; d1];
14     state_signals:
15         X ISA Std::VectorVar WITH
16             n := 6;
17             value := [LPF1.x; Wp1.W; Wp2.W; Wp3.W; Boiler.Vwt; Boiler.P];
18         END;
19     parameter_matrix_mapping:
20         PM ISA Std::MatrixVar WITH
21             m := 23;
22             n := 5;
23             value := [qs10,           qs20,           qf0,           qfw0,           Tfw0;
24                         Boiler.mdc,   Boiler.Vd,   Boiler.Vr,   Boiler.Vdc,   NaN;
25                         Tcf,           qfrng,          NaN,           NaN,           NaN;
26                         Boiler.Sw0,   Boiler.Sw1,   Boiler.Sw2,   Boiler.Sw3,   NaN;
27                         qscf,          NaN,           NaN,           NaN,           NaN;
28                         qfcf,          NaN,           NaN,           NaN,           NaN;
29                         Sigma1,        NaN,           NaN,           NaN,           NaN;
30                         Sigma2,        NaN,           NaN,           NaN,           NaN;
31                         Sigma3,        NaN,           NaN,           NaN,           NaN;
32                         Sigma4,        NaN,           NaN,           NaN,           NaN;
33                         Sigma5,        NaN,           NaN,           NaN,           NaN;
34                         Boiler.md,    NaN,           NaN,           NaN,           NaN;
35                         Boiler.mr,    NaN,           NaN,           NaN,           NaN;
36                         Boiler.Ad,    NaN,           NaN,           NaN,           NaN;
37                         Boiler.kf,    NaN,           NaN,           NaN,           NaN;
38                         Boiler.ks,    NaN,           NaN,           NaN,           NaN;
39                         Boiler.L0,    NaN,           NaN,           NaN,           NaN;
40                         Boiler.xi0,   NaN,           NaN,           NaN,           NaN;
41                         Boiler.b1,    NaN,           NaN,           NaN,           NaN;
42                         Boiler.b2,    NaN,           NaN,           NaN,           NaN;
43                         Boiler.dVwt0, NaN,           NaN,           NaN,           NaN;
44                         Boiler.P0,    NaN,           NaN,           NaN,           NaN;
45                         Boiler.xr0,   NaN,           NaN,           NaN,           NaN];
46         END;
47     END;
48 END;

```

Listing A.2: DrumBoiler/Oresund2.om—An example demonstrating how the signal model mapping is included as a sub-model attribute in the simulation interface; specifically, see lines 6–47 and listing A.1.

```

1 #!/bin/sh
2 # $Id: flat-model2maple,v 1.7 1997/06/24 11:32:55 sorliej Exp $
3 ######
4 # First process the "flat-model" output.
5 #####
6 cat $1 | \
7 sed '1,/^model .*/d;
8 /^.*= /!d;
9 /^.*= ?;/d;
10 /^Non-linear equation: .*/d;
11 s/;$/:/g;
12
13 # Strip lines from the Event part of the log-file.
14
15 /^.*=.*[^:]/d;
16
17 # Convert the end-of-line character (^M) to a Maple command terminator (:).
18
19 s/^M//g;
20
21 # Convert any equalities (=) into Maple bindings (:=).
22
23 s/ = / := /g;
24
25 # Convert differential syntax (prime notation) to something unique.
26 # First process vector-valued (indexed) symbols, then scalars.
27
28 s/\([0-9]*\)'`__prime\1/g;
29 s/'`__prime/g;
30
31 # Convert the period in Omola names to an underscore.
32
33 s/\.\(([^\0-9])/_\1/g;
34
35 # Convert semi-colons in between square brackets to commas.
36 # This converts Omola vectors and matrices into Maple lists.
37 # NOTE: one _should_ be able to program this as a loop.
38
39 s/\[\(.*\);\(.*\)\]/[\1,\2]/g;
40 s/\[\(.*\);\(.*\)\]/[\1,\2]/g;
41 s/\[\(.*\);\(.*\)\]/[\1,\2]/g;

... (duplicate lines deleted) ...

105 s/\[\(.*\);\(.*\)\]/[\1,\2]/g;
106 s/\[\(.*\);\(.*\)\]/[\1,\2]/g;
107 s/\[\(.*\);\(.*\)\]/[\1,\2]/g;
108
109 # Finally, comment out equations designating the OmSim inputs. This
110 # makes the script-output suitable as "include file" input for Maple.
111
112 s/^`(.*)`*continuousinput`.*\,.*,[ ]*\(.*)\,.*$//;
113

```

Listing A.3: flat-model2maple—A shell script which translates OmSim’s “Flat model” and “Event part” debug information into a format that can be loaded into Maple.

```

114 # Convert conditional assignment statements to piecewise function calls.
115 # Through repetition of the sed command, conditional statements with up to
116 # ten branches are translated into nested two-branch piecewise operators.
117 # NOTE!! This translation breaks if the conditional block is a component
118 # sub-expression of a larger right-hand side expression. This is a con-
119 # sequence of the Omola conditional statement not having an end delimiter.
120
121 s/^\\(.*:=.*\\)if\\(.*)then\\(.*)else\\(.*):$\\1 piecewise\\(2,\\2,\\3,\\4\\):/g;
122 s/^\\(.*:=.*\\)if\\(.*)then\\(.*)else\\(.*):$\\1 piecewise\\(2,\\2,\\3,\\4\\):/g;
123 s/^\\(.*:=.*\\)if\\(.*)then\\(.*)else\\(.*):$\\1 piecewise\\(2,\\2,\\3,\\4\\):/g;
124 s/^\\(.*:=.*\\)if\\(.*)then\\(.*)else\\(.*):$\\1 piecewise\\(2,\\2,\\3,\\4\\):/g;
125 s/^\\(.*:=.*\\)if\\(.*)then\\(.*)else\\(.*):$\\1 piecewise\\(2,\\2,\\3,\\4\\):/g;
126 s/^\\(.*:=.*\\)if\\(.*)then\\(.*)else\\(.*):$\\1 piecewise\\(2,\\2,\\3,\\4\\):/g;
127 s/^\\(.*:=.*\\)if\\(.*)then\\(.*)else\\(.*):$\\1 piecewise\\(2,\\2,\\3,\\4\\):/g;
128 s/^\\(.*:=.*\\)if\\(.*)then\\(.*)else\\(.*):$\\1 piecewise\\(2,\\2,\\3,\\4\\):/g;
129 s/^\\(.*:=.*\\)if\\(.*)then\\(.*)else\\(.*):$\\1 piecewise\\(2,\\2,\\3,\\4\\):/g;
130 s/^\\(.*:=.*\\)if\\(.*)then\\(.*)else\\(.*):$\\1 piecewise\\(2,\\2,\\3,\\4\\):/g;
131
132 # Translate function names
133
134 s/acos/arccos/g;
135 s/asin/arcsin/g;
136 s/atan/arctan/g;
137 s/atan2/arctan/g;
138
139 # Finish by translating relational operators.
140
141 s/~=/<>/g;
142 s/^[_]*//g;
143 /^$/d;
144 s/===/g' |\
145 cat
146
147 ######
148 # Second, process the "Event part" output.
149 #####
150 # Begin by deleting everything upto the beginning of the Event part.
151 cat $1 |\
152 sed '1,/^ Event model instantiated from .*$/d;
153
154 # Delete the message OmSim outputs under Linux (if necessary).
155 /^Non-linear equation: .*$/d;
156
157 # Delete lines that are not Event-part assignment statements.
158 /^.*:=.*[^;]*$/!d;
159
160 # Convert the period in Omola names to an underscore.
161 s/.\\([^\0-9]\\)/_\\1/g;
162
163 # Strip the first hierachic level from every name in the Event dump.
164 s/[A-Za-z0-9]*_\\([_A-Za-z0-9]*\\)/\\1/g;
165
166 # A more portable form of the previous step is, using GNUs regexps,
167 # s/[[alnum:]]+_\\([_[:alnum:]]+\\)/\\1/g;
168
169 # Finally, post-fix a colon to each Event-dump assignment statement.
170 s/^\\(.*)$/\\1:/g' |\
171 cat

```

Listing A.3: flat-model2maple (continued).

A.2 Symbolic Processing and Code Generation

```

1  # $Id: CodeGen.sh,v 1.10 1997/06/24 11:43:57 sorliej Exp $
2  #
3  # Needed for LTH-Regler's version of the maple script
4  DISPLAY="" ; export DISPLAY;
5  #
6  # 1) Translate the equations in the log-file into Maple syntax.
7  #
8  echo "Running the OmSim log-file translator."
9  flat-model2maple omsim.log > omsim.mpl
10 #
11 # 2) Start Maple and process the translated equations.
12 #
13 echo "Post-processing the equations in Maple."
14 maple -q > prep.log << "____PostProcess____"
15
16 # Define a utility function and then load the translated equations
17 # and post-translation processing utilities.
18 REVERSE_LST := lst -> map( rel->rhs(rel)=lhs(rel), lst );
19 read 'omsim.mpl';
20 read '/home/sorliej/maple/post-processing-utilities':
21
22 # Compensate for case-changes made by the Omola compiler.
23 if not assigned(SMM_U) then SMM_U := SMM_u: fi:
24 if not assigned(SMM_X) then SMM_X := SMM_x: fi:
25 if not assigned(SMM_Y) then SMM_Y := SMM_y: fi:
26
27 # Process the signal model mapping definitions.
28 state_mapping := table2mapping(SMM_X,x);
29 input_mapping := table2mapping(SMM_U,u);
30 disturb_mapping := table2mapping(SMM_Wv,wv)
31         union table2mapping(SMM_Wy,wy);
32 parameter_mapping := table2mapping(SMM_PM,theta):
33 numeric_mapping := defaults2mapping(SMM_PM,theta):
34 name_mapping := state_mapping
35         union input_mapping
36         union disturb_mapping
37         union parameter_mapping:
38
39 # Format the parameter matrix and default values.
40 par[default] := defaults2matrix(SMM_PM);
41
42 # Construct lists of state and output equations, substituting indexed vector
43 # names (i.e. x[], u[], wv[], wy[], theta[]) for the hierachic Omola names
44 eqns_dX := subs( name_mapping, table2primelist(SMM_X) ):
45 eqns_Y := subs( name_mapping, table2list(SMM_Y) ):
46
47 # Construct a list of the initial input and state conditions.
48 REVERSE_LST( table2mapping(SMM_U0,u0) ):
49 subs( name_mapping, eval(")"):
50 eqns_U0 := convert(table(map(r->op(1, lhs(r))=rhs(r), *)), list);
51 table2newmap(SMM_X,x0):
52 subs( name_mapping, eval(")"):
53 eqns_X0 := convert(convert(table(map(r->op(1, lhs(r))=rhs(r), *)), array)
      list):

```

Listing A.4: CodeGen.sh—Top-level shell script for translation of an OmSim log file into a Simulink MEX-file S-function and an IdKit model subroutine module.

```

54
55 # If the initial conditions are functions of other initial input
56 # and/or state conditions, make them functions of parameters.
57 indets(eqns_X0,u[integer]);
58 if nops("") <> 0 then
59     REVERSE_LST( table2mapping(SMM_U0,u0) );
60     eqns_X0 := subs(u=u0, ", parameter_mapping, eqns_X0 );
61 fi:
62 indets(eqns_X0,x[integer]);
63 if nops("") <> 0 then
64     eqns_X0:
65     {seq(x0[i]=op(i,"),i=1..nops(""))}:
66     eqns_X0 := subs( x=x0, ", eqns_X0 );
67 fi:
68
69 # Identify any remaining indeterminate names and construct their
70 # "new" names. The equation assignments for these names are
71 # obtained from the Event-part of the log file. These are the
72 # event equations computed either at the "Init" or "Start" events.
73 indets(eqns_dX,name) union indets(eqns_Y,name) union indets(eqns_X0,name):
74     " minus indets("",indexed);
75     {seq(op(i,")=insert_new(op(i,")), i=1..nops(""))}:
76     subs( name_mapping, eval(" ) :
77
78 # Substitute state vector references in the event equations with
79 # the initial state conditions.
80 table2newmap(SMM_X,x0):
81 eval("):
82 subs( x=x0, ", parameter_mapping, " " ) :
83
84 # Also substitute the initial input values into the relations,
85 # making them functions of only the model parameters.
86 REVERSE_LST( table2mapping(SMM_U0,u0) );
87 event_eqns := subs( u=u0, ", parameter_mapping, " " ) :
88
89 # Check if the event equations involve other event definitions.
90 map(lhs,event_eqns);
91 indets(map(rhs,event_eqns), name) minus
92 indets(map(rhs,event_eqns), indexed);
93
94 # Iteratively substitute the event definitions into their own
95 # right-hand-side's. This is necessary to completely reduce them
96 # to functions of the model parameters.
97 tmp := ":":
98 for i from 1 to 10 while nops(tmp) <> 0 do
99     print(i);
100    map(r->lhs(r)=subs(event_eqns,rhs(r)), event_eqns ) :
101    event_eqns := ":";
102    indets(map(rhs,event_eqns), name) minus
103    indets(map(rhs,event_eqns), indexed) :
104    tmp := ":";
105 od:
106 if i > 9 then ERROR('self-referencing parameter equation probable.'): fi;
107 indets(map(rhs,event_eqns), name);

```

Listing A.4: CodeGen.sh (*continued*).

```

108 # Finally substitute the relations into the existing definitions
109 # that contain the unassigned names.
110 event_egns:
111   eqns_dX := subs( "", eqns_dX ):
112   eqns_Y := subs( "", eqns_Y ):
113   eqns_X0 := subs( "", eqns_X0 ):
114
115
116 # Convert the lists of equations into functionals.
117   f[m] := unapply( eqns_dX, x, u, wv, theta ):
118   h[m] := unapply( eqns_Y, x, u, wy, theta ):
119   x0[m] := unapply( eqns_X0, theta ):
120   u0[m] := unapply( eqns_U0, theta ):
121
122 # Collect the model definition in a list-of-lists, plus the default
123 # parameter values. Then turn this into an operator (internally, a
124 # Maple procedure) and save it to a file using Maple's internal
125 # format. We do this so we can restart the Maple interpreter
126 # "fresh" before beginning the code generation step.
127 [ f[m](x,u,beta,theta),
128   x0[m](theta),
129   h[m](x,u,nu,theta),
130   u0[m](theta), rhs(par[default])]:
131 model := unapply( ", x,u,beta,nu,theta ):
132
133 # Save the model equations and exit.
134 save model, 'model.m':
135 quit:
136 __PostProcess__
137
138 #-----
139 # 3) Restart Maple and run the code-generation batch.
140 #-----
141 echo "Running the Maple code-generation utilities."
142 maple -q > codegen.log <<"__CodeGen__"
143
144 # Reload the signal model, and load the EKF and TplC packages.
145 read 'model.m';
146 read '/home/sorliej/maple/EKF':
147 read '/home/sorliej/maple/TplC':
148
149 # Encode the model as a Simulink S-function.
150 model(x,[seq('u'[i],i=5..9)], [u[1],u[2],u[3],u[4]], [u[11],u[11]], p):
151   SimStructModel( 'Smodel', [op(1..4,"")], [x,u,p], evalm("[5]) );
152
153 # Encode the model for use with IdKit.
154 model(xy,u,wv,wy,p):
155   IdKitModel( 'model', [op(1..4,"")], [xy,u,wv,wy,p], evalm("[5]) );
156
157 # Derive and encode a CKF predictor as a Simulink S-function.
158 # model(x,u,w,v,p):
159 #   filter[1,1] := ckf( [1,1], [op(1..3,"")], [x,u,w,v,p,X] ):
160 #   SimStructCKF('Sfilter', filter[1,1], [x,u,p], evalm(" "[5]) );
161
162 # Exit Maple
163 quit:
164 __CodeGen__

```

Listing A.4: CodeGen.sh (*continued*).

```

1 concat_lists := (L1,L2) -> [op(L1), op(L2)]:
2
3 table2list := tbl -> convert(convert(tbl,array),list):
4
5 list2matrix := lst -> convert(convert(lst,vector),matrix):
6
7 table2mapping := proc(Tbl,Name)
8   local lst, j;
9   if not type(Tbl,table) then ERROR('bad arguments'); fi;
10  lst := [ indices(Tbl) ]:
11  RETURN( {seq(Tbl[op(op(j,lst))]=Name[op(op(j,lst))], j=1..nops(lst))} );
12 end:
13
14 # Return a set of equalities from a name-d parameter matrix to default numeric values.
15 defaults2mapping := proc(Tbl,Name)
16   local lst, j;
17   if not type(Tbl,table) then ERROR('bad arguments'); fi;
18   lst := [ indices(Tbl) ]:
19   RETURN( {seq(Name[op(op(j,lst))]=eval(cat( Tbl[ op(op(j,lst)) ],
20           '_default' )), j=1..nops(lst))} );
21 end:
22
23 defaults2matrix := proc(Tbl)
24   local lst, j, m, n, M, N, MaxRowIndex, MaxColIndex;
25   if not type(Tbl,table) then ERROR('bad arguments'); fi;
26   lst := [ indices(Tbl) ]:
27   MaxRowIndex := < max(0,seq(op(1,op(i,set)),i=1..nops(set)))|set[i]>;
28   MaxColIndex := < max(0,seq(op(2,op(i,set)),i=1..nops(set)))|set[i]>;
29   m := MaxRowIndex(convert(lst,set));
30   n := MaxColIndex(convert(lst,set));
31   M := linalg[matrix](m,n,(i,j)->'NaN'):
32   N := linalg[matrix](m,n,(i,j)->'-'):
33   for j from 1 to nops(lst) do
34     Tbl[op(op(j,lst))]:
35     if type("",indexed) or searchtext('SMM_NaN', "") = 0 then
36       M[op(op(j,lst))] := eval(cat( Tbl[ op(op(j,lst)) ], '_default' )):
37       N[op(op(j,lst))] := substring( eval(Tbl[ op(op(j,lst)) ]), 1..10^4):
38     fi:
39   od:
40   RETURN( evalm(N) = evalm(M) ):
41 end:
42
43 reverse_searchtext := proc(str,c)
44   local i, n:
45   n := length(str):
46   for i from 1 to n
47     while searchtext(c,str,-i..-1) = 0
48     do od:
49   RETURN(n-i+1):
50 end:

```

Listing A.5: post-processing utilities—A collection of Maple procedures used in processing the OmSim modelling equations once loaded into Maple; see listing A.4.

```

51
52     insert_new := proc(str)
53         local s:
54         if type(str,string)  then
55             reverse_searchtext(str,'_'):
56             cat( substring(str,0.."), 'new_',
57                  substring(str,"+1..length(str)) ):
58         elif type(str,indexed) then
59             s := op(0,str):
60             reverse_searchtext(s,'_'):
61             cat( substring(s,0.."), 'new_',
62                  substring(s,"+1..length(s)) )[op(str)]:
63         else ERROR('bad arguments'); fi;
64         RETURN("):
65     end:
66
67     postfix_prime := proc(str)
68         local s:
69         if   type(str,string)  then RETURN(cat(      str, '__prime' )):
70         elif type(str,indexed) then RETURN(cat(op(0,str), '__prime')[op(str)]):
71         else ERROR('bad arguments'); fi;
72     end:
73
74     set2newmap := proc(Set,Name)
75         local lst, j;
76         if not type(Set,set)  then ERROR('bad arguments'); fi;
77         lst := [ indices(Tbl) ]:
78         RETURN({
79             seq(Name[op(op(j,lst))]=insert_new( Tbl[op(op(j,lst))]), j=1..nops(lst)
80           });
81     end:
82
83     table2newmap := proc(Tbl,Name)
84         local lst, j;
85         if not type(Tbl,table)  then ERROR('bad arguments'); fi;
86         lst := [ indices(Tbl) ]:
87         RETURN({
88             seq(Name[op(op(j,lst))]=insert_new( Tbl[op(op(j,lst))]), j=1..nops(lst)
89           });
90     end:
91
92     table2primelist := proc(Tbl)
93         local lst, j;
94         if not type(Tbl,table)  then ERROR('bad arguments'); fi;
95         lst := [ indices(Tbl) ]:
96         RETURN(convert(convert(table({
97             seq(op(op(j,lst))=postfix_prime( Tbl[op(op(j,lst))]), j=1..nops(lst)
98           }),array),list));
99     end:

```

Listing A.5: post-processing-utilties (*continued*).

```

1  #-----#
2  # $Source: /home/sorliej/maple/src/TplC/RCS/IdKitModel.src,v $
3  # $Revision: 1.18 $
4  # $Date: 1997/03/06 08:24:31 $
5  # $Author: sorliej $
6  # $Locker: $
7  #-----#
8  `type/IdKitModelargs` := {
9    # [string, list({list,vector})],
10   [string, list({list,vector}), list(string)],
11   [string, list({list,vector}), list(string), {list,vector,array,matrix}]
12 }:
13 #-----#
14 IdKitModel := proc( FileName, SignalModel, SignalNames, ParameterMatrix )
15 #-----#
16   local dX, Y, X0, N, NList, Pvals, Eqns, EqNames, name_mapping, Fcns,
17   numeric_mapping, par_index_mapping, Defines, Includes,
18   newlineC, IdKitHead, IdKitBody, IdKitFoot,
19   IdKit_initcond, IdKit_init_u, IdKit_yequ, IdKit_xyequ,
20   IdKit_setm, IdKit_setp, ij, Coldims, Passign,
21   # Declare names (strings) used as local in order to avoid evaluation of
22   # possibly existing variables from the calling (global) namespace.
23   i, par, xy, u, wv, wy, y, p, Pm, Pn, feedthru, C, S,
24   # Declare variables different from the SimStructModel template.
25   m, n, U0, t, t0, x0, u0, dx_dt, y_of_t:
26
27   options '© 1996, 1997 J.A.Sørlie, KTH S3-Reglerteknik, Stockholm Sweden':
28
29   newlineC := [commentC, '']:
30
31   if not type([args],IdKitModelargs) then
32     ERROR(cat(`invalid arguments. See ?`, procname)):
33   fi:
34
35   userinfo(1,'TplCcomment',
36   'Parsing the signal model equations, converting fractions to floats.'):
37
38   dX := evalf( convert(SignalModel[1],list) ): N[xy] := nops(dX):
39   userinfo(3,'TplCresult', 'state derivatives:', print(dX)):
40
41   if nops(SignalModel)<2 or type(SignalModel[2],[]) then
42     userinfo(2,'TplCcomment','Assuming initial conditions are zero.'):
43     X0 := evalf([{seq(0,i=1..N[xy])}]):
44   else
45     X0 := evalf( convert(SignalModel[2],list) ):
46     if nops(X0)<>N[xy] then ERROR('wrong number of initial conditions') fi:
47   fi:
48   userinfo(3,'TplCresult', 'state initialization:', print(X0)):
49
50   if nops(SignalModel)<3 or type(SignalModel[3],[]) then
51     userinfo(2,'TplCcomment','Assuming outputs to be state vector.'):
52     Y := evalf([{seq('xy'[i],i=1..N[xy])}]): N[y] := N[xy]:
53   else
54     Y := evalf( convert(SignalModel[3],list) ): N[y] := nops(Y):
55   fi:
56   userinfo(3,'TplCresult', 'measured outputs:', print(Y)):
57
58   if nops(SignalModel)<4 or type(SignalModel[4],[]) then
59     userinfo(2,'TplCcomment','Unspecified initial inputs left unassigned.'):
60   else
61     U0 := evalf( convert(SignalModel[4],list) ):
62     userinfo(3,'TplCresult', 'input initialization:', print(U0)):
63   fi:

```

Listing A.6: IdKitModel.src—Template that automatically encodes the IdKit model subroutines.

```

64      if nops(SignalModel)>=5 then
65          userinfo(2,'TplCcomment','Ignoring extra equations in the signal model.'):
66      fi:
67
68      if nargs >= 3 and not type(SignalNames,[]) then
69          if nops(SignalNames) >= 5 then
70              NList :=[op(1..5,SignalNames)]:
71              userinfo(1,'TplCcomment','Using parameter names:',print(NList)):
72          else
73              ERROR('expecting a list of signal names e.g. [xy, u, wv, wy, p].'):
74          fi:
75      else
76          NList := ['xy', 'u', 'wv', 'wy', 'p']:
77          userinfo(1,'TplCcomment','Using default parameter names:',print(NList)):
78      fi:
79
80      if nargs >= 4 and not type(ParameterMatrix,[]) then
81          if type(ParameterMatrix,{list,vector}) then
82              Pvals := evalf(convert(convert(ParameterMatrix,vector),matrix)):
83          else Pvals := evalf(convert(ParameterMatrix,matrix)): fi:
84          userinfo(2,'TplCcomment','Using default parameter values:',print(Pvals)):
85      else
86          userinfo(2,'TplCcomment','Unspecified parameter values left unassigned.'):
87      fi:
88
89      userinfo(1,'TplCcomment', 'Mapping signal names in the equations. '):
90      Eqns := { op(dX), op(X0), op(Y) }:
91      if assigned(U0) then Eqns := Eqns union { op(U0) } fi:
92      EqNames := indets(Eqns,name):
93      indets(EqNames,NList[1][integer]):
94          (seq( op(i,")=`xy`[op(1,op(i,"))], i=1..nops(")),indets(EqNames,NList[2][integer]):
95          " union (seq(op(i,")=`u`[op(1,op(i,"))],i=1..nops(")),indets(EqNames,NList[3][integer]):
96          " union (seq(op(i,")=`wv`[op(1,op(i,"))],i=1..nops(")),indets(EqNames,NList[4][integer]):
97          " union (seq(op(i,")=`wy`[op(1,op(i,"))],i=1..nops(")),indets(EqNames,NList[5][integer]):
98          name_mapping := " union (seq(op(i,")=`p`[op(1..2,op(i,"))],i=1..nops(")):
99          userinfo(3,'TplCresult',print('name_mapping'=name_mapping)):
100         dX := subs( name_mapping, dX ):
101         X0 := subs( name_mapping, X0 ):
102         Y := subs( name_mapping, Y ):
103         Eqns := { op(dX), op(X0), op(Y) }:
104         if assigned(U0) then
105             U0 := subs( name_mapping, U0   ):
106             Eqns := Eqns union { op(U0) }:
107         fi:
108         if assigned(Pvals) then Eqns := Eqns union convert(Pvals,set): fi:
109
110         EqNames := indets(Eqns,name):
111         userinfo(3,'TplCresult',print('EqNames'=EqNames)):
112
113         userinfo(1,'TplCcomment', 'Determining input vector dimension.'):
114         N[u] := 'TplC/MaxRowIndex'( indets(EqNames,'u'[integer]) ):
115         userinfo(2,'TplCresult',print('N[u]'=N[u])):
116         if not assigned(U0) then
117             if N[u] = 0 then U0 := [0] else U0 := evalf([seq(0,i=1..N[u])]): fi:
118             elif nops(U0) <> N[u] then ERROR(
119                 'Vector dim of initial input vector not = to the max index in equations.'):
120         fi:

```

Listing A.6: IdKitModel.sr (continued).

```

127 userinfo(1,'TplCcomment', 'Determining stochastic input vector dimensions.'):
128 N[wv] := 'TplC/MaxRowIndex'(~indets(EqNames,'wv'[integer]))~:
129 N[wy] := 'TplC/MaxRowIndex'(~indets(EqNames,'wy'[integer]))~:
130 userinfo(2,'TplCresult',print('N[wv]'=N[wv], 'N[wy]'=N[wy]))~:
131
132 userinfo(1,'TplCcomment', 'Determining parameter matrix dimensions.'):
133 indets(EqNames,'p'[integer,integer]):~:
134 N[Pm] := 'TplC/MaxRowIndex'(~):
135 N[Pn] := 'TplC/MaxColIndex'(~):
136 userinfo(3,'TplCcomment',print('Params'='')):
137 userinfo(4,'TplCcomment',print('Eqns'=Eqns)):
138 userinfo(2,'TplCcomment',print('N[Pm]'=N[Pm], 'N[Pn]'=N[Pn])):
139 if assigned(Pvals) then
140   if linalg[rowdim](Pvals) <> N[Pm] or linalg[coldim](Pvals) <> N[Pn] then
141     ERROR('Dimensions of numerical parameter matrix are wrong.'):
142   fi:
143 else
144   userinfo(0,'TplCwarning', print(''),
145   'WARNING: filling default numeric parameter matrix with NaN:s.~',
146   print('')):
147   Pvals := matrix(N[Pm],N[Pn],(i,j)->'NaN'):
148   EqNames := EqNames union {'NaN'}:
149 fi:
150
151 userinfo(1,'TplCcomment',
152   'Checking functional structure of the signal model.'):
153 indets({op(dx)},indexed) minus indets(EqNames,
154   {'xy'[integer], 'u'[integer], 'wv'[integer], 'p'[integer,integer]}):
155 if nops(~) <> 0 then ERROR(
156   cat('state equations contain unallowed names:\n\t',convert(~,string))):
157 fi:
158 indets({op(Y)},indexed) minus indets(EqNames,
159   {'xy'[integer], 'u'[integer], 'wy'[integer], 'p'[integer,integer]}):
160 if nops(~) <> 0 then ERROR(
161   cat('output equations contain unallowed names:\n\t',convert(~,string))):
162 fi:
163 indets({op(X0)},indexed) minus indets(EqNames, 'p'[integer,integer]):
164 if nops(~) <> 0 then ERROR(
165   cat('initial conditions contain unallowed names:\n\t',convert(~,string))):
166 fi:
167 indets({op(U0)},indexed) minus indets(EqNames, 'p'[integer,integer]):
168 if nops(~) <> 0 then ERROR(
169   cat('initial inputs contain unallowed names:\n\t',convert(~,string))):
170 fi:
171
172 userinfo(1,'TplCcomment',
173   'Checking for any unassigned variables in the equations.'):
174 EqNames
175   minus indets(EqNames,{ 'xy'[integer], 'u'[integer],
176   'wv'[integer], 'wy'[integer], 'p'[integer,integer]}):
177   minus { 'EPS', 'TRUE', 'FALSE', 'NaN', epsilon, pi, tau, '' }:
178 if nops(~) <> 0 then
179   ERROR(cat('equations contain unassigned names:\n\t',convert(~,string))):
180 fi:
181
182 Passign := []:
183 for ij in [indices(Pvals)] do
184   if type(Pvals[op(ij)],numeric) then
185     Passign := [ op(Passign),
186       [equalC, cat('p(',ij[1]-1,',',ij[2]-1,')'), Pvals[op(ij)]]]:
187   fi:
188 od;
189 if nops(Passign) < 1 then

```

Listing A.6: IdKitModel.src (*continued*).

```

190     Passign :=
191         [commentC, ' No parameter values were given at code-gen time. ']:
192     fi:
193
194     indets(EqNames,'p'[integer,integer]):
195     Coldims := convert([seq(0,i=1..N[Pm])],array):
196     for ij in " do
197         Coldims[ op(1,ij) ] := max( Coldims[op(1,ij)], op(2,ij) ) :
198     od:
199
200     userinfo(1,'TplCcomment',
201         ' Mapping numeric constants to CPP definitions, e.g. C1, C2, etc.'):
202     convert(indets(Eqns,float),list):
203     numeric_mapping := [seq("[i] = cat('C',i), i=1..nops("))]:
204 # numeric_mapping := [seq("[i] = cat('C',printf('%02d',i)), i=1..nops("))]:
205     dX := subs(numeric_mapping,dX):
206     X0 := subs(numeric_mapping,X0):
207     Y := subs(numeric_mapping,Y):
208     U0 := subs(numeric_mapping,U0):
209
210     userinfo(1,'TplCcomment', 'Constructing list of CPP macro definitions.'):
211     Defines :=
212         [commentC, ' Definitions of numeric constants. '],
213         seq( ['defineC', cat('C',i,''), i=1..nops(numeric_mapping) ],
214             newlineC:
215
216     userinfo(1,'TplCcomment', 'Constructing list of include files.'):
217     Includes :=
218         [commentC,
219             ' Define interface for a continuous-time single-block model. '],
220         [includeC, '"cs.h"]:
221
222     userinfo(1,'TplCcomment',
223         'Building a list of functional operators used in the equations.'):
224     convert( indets(Eqns,function), list ):
225     Fcns := { seq(op(0,[i]), i=1..nops(")) }:
226     userinfo(2,'TplCcomment',
227         'The equations contain the following functional operators:',print(Fcns)):
228
229     if member('piecewise',Fcns) then
230         userinfo(2,'TplCcomment',
231             'Checking that piecewise() calls have either 3 or 4 arguments.'):
232         convert( indets(Eqns,specfunc(anything,'piecewise')),list );
233         if nops({seq(nops("[i]), i=1..nops(")) minus {3,4}}) <> 0 then ERROR(
234             cat('support for piecewise() is limited to if-then-else constructs.\n',
235                 'Its arguments should be: smoothness-order, condition, expr1, expr2')):
236         fi:
237     Defines := Defines, [defineC,
238         'piecewise(dummy,cond,expr1,expr2)', '((cond)?(expr1):(expr2))']:
239     Fcns := Fcns minus {'piecewise'}:
240
241     fi:
242
243     userinfo(1,'TplCcomment', 'Adding define/includes for supported constants.'):
244     if member('EPS',EqNames) then
245         Defines := Defines, [defineC, 'EPS', 'DBL_EPSILON']:
246     fi:
247     if member('epsilon',EqNames) then
248         Defines := Defines, [defineC, 'epsilon', 'DBL_EPSILON']:
249     fi:
250     if member('pi',EqNames) then
251         Defines := Defines, [defineC, 'pi', 'M_PI']:
252     fi:

```

Listing A.6: IdKitModel.src (*continued*).

```

253 if member('tau',EqNames) then
254   Defines := Defines, [defineC, 'tau', 'time_c']:
255 fi:
256 if member('NaN',EqNames) then
257   Defines := Defines, [defineC, 'NaN', '(0.0*(1.0/0.0))']:
258 fi:
259 userinfo(1,'TplCcomment',
260   'Map parameter references to a CPP macro, i.e. p[i,j] -> p(i-1,j-1).'):
261 convert(indets(EqNames,'p'[integer,integer]),list);
262 par_index_mapping :=
263 {seq(op(i,")=p'(op(1,op(i,"))-1,op(2,op(i,"))-1), i=1..nops(""))}:
264
265 dx := convert( subs(par_index_mapping,dx), vector ):
266 X0 := convert( subs(par_index_mapping,X0), vector ):
267 Y := convert( subs(par_index_mapping,Y), vector ):
268 U0 := convert( subs(par_index_mapping,U0), vector ):
269
270 #-----
271 userinfo(1,'TplCcomment', 'Defining a template in ``macroC``'):
272 #-----
273
274 i := 'i':
275
276 IdKitHead :=
277 [ [commentC, cat{
278   '*****',
279   '\n * FILE: ', FileName, '.c',
280   '\n * DATE: ', 'TplC/GetDate'(),
281   '\n *',
282   '\n * To compile, issue the command: "mcompile ', FileName, '.c"',
283   '\n *',
284   '\n * This file was automatically generated using Maple and MacroC,',
285   '\n * a shareware package developed by Patrick Capolsini. The code',
286   '\n * generation template, part of the TplC package, was developed',
287   '\n * by J.A.Sørlie, KTH S3-Reglerteknik, Stockholm SWEDEN.',
288   '\n *****'],
289   newlineC,
290   Includes,
291   newlineC,
292   Defines,
293   newlineC
294 ]]:
295
296 'TplC/debugger'(IdKitHead):
297
298 IdKit_initcond :=
299 [ [commentC, cat{
300   '*****',
301   '\n * initcond - user supplied state-vector initialization',
302   '\n *',
303   '\n * \tx0[*] = fcn(t0,p(*,*),constants)',
304   '\n *',
305   '\n * where:',
306   '\n * x0[*]\thas indices 0..',eval(N[xy]-1),
307   '\n * t0\tis the start time of the simulation',
308   '\n * p(i,j)\thas indices i=0..',eval(N[Pm]-1), ' and j=0..',eval(N[Pn]-1),
309   '\n * constants\thave numerical values or CPP definitions',
310   '\n *****'],
311   newlineC,
312   [functionm, 'void', 'initcond',
313    [ ['int ', ['dim']],
314     ['double', ['t0','*x0'] 1 ],
315     [ [matrixm,'x0',x0] 1 ],
316

```

Listing A.6: IdKitModel.src (*continued*).

```

316     newlineC ];
317   'Tp1C/debugger'(IdKit_initcond):
318
319   IdKit_init_u :=
320   [ [commentC, cat(
321     '*****',
322     '\n * init_u - user supplied input-vector initialization',
323     '\n *',
324     '\n * \tu0[*] = fcn(t0,p(*,*),constants)',
325     '\n *',
326     '\n * where:',
327     '\n * u0[*]\thas indices 0..',eval(N[u]-1),
328     '\n * t0\thas the start time of the simulation',
329     '\n * p(i,j)\thas indices i=0..',eval(N[Pm]-1), ' and j=0..',eval(N[Pn]-1),
330     '\n * constants\tare numerical values or CPP definitions',
331     '\n *****']),
332   newlineC,
333   [functionm, 'void', 'init_u',
334   [ ['double', ['t0', '*u0']] ],
335   [ [matrixm,'u0',U0] ],
336   newlineC ];
337   'Tp1C/debugger'(IdKit_init_u);
338
339   IdKit_yequ :=
340   [ [commentC, cat(
341     '*****',
342     '\n * yequ - user supplied measurement equations',
343     '\n *',
344     '\n * \ty_of_t[*] = fcn(xy[*],u[*],wy[*],t0,t,p(*,*))',
345     '\n *',
346     '\n * where:',
347     '\n * y_of_t[*]\thas indices 0..',eval(N[y]-1),
348     '\n * xy[*]\thas indices 0..',eval(N[xy]-1),
349     '\n * u[*]\thas indices 0..',eval(N[u]-1),
350     '\n * wy[*]\thas indices 0..',eval(N[wy]-1),
351     '\n * t0\thas the start time of the simulation',
352     '\n * t\thas the current time of the simulation',
353     '\n * p(i,j)\thas indices i=0..',eval(N[Pm]-1), ' and j=0..',eval(N[Pn]-1),
354     '\n *****'),
355   newlineC,
356   [functionm, 'void', 'yequ',
357   [ ['double', ['*y_of_t', 't0', 't'] ],
358   [ [matrixm,'y_of_t',Y] ],
359   newlineC ];
360   'Tp1C/debugger'(IdKit_yequ);
361
362   IdKit_xyequ :=
363   [ [commentC, cat(
364     '*****',
365     '\n * xyequ - user supplied state equations',
366     '\n *',
367     '\n * \tdx_dt[*] = fcn(xy[*],u[*],wv[*],t0,t,p(*,*))',
368     '\n *',
369     '\n * where:',
370     '\n * dx_dt[*]\thas indices 0..',eval(N[xy]-1),
371     '\n * xy[*]\thas indices 0..',eval(N[xy]-1),
372     '\n * u[*]\thas indices 0..',eval(N[u]-1),
373     '\n * wv[*]\thas indices 0..',eval(N[wv]-1),
374     '\n * t0\thas the start time of the simulation',
375     '\n * t\thas the current time of the simulation',
376     '\n * p(i,j)\thas indices i=0..',eval(N[Pm]-1), ' and j=0..',eval(N[Pn]-1),
377     '\n *****'),
378   newlineC,

```

Listing A.6: IdKitModel.src (continued).

```

379     [functionm, 'void', 'xyequ',
380      [ ['double', ['*t', '*xy', '*dx_dt'] ] ],
381      [ [matrixm, 'dx_dt', dX] ] ],
382      newlineC ];
383   'TpIC/debugger'(IdKit_xyequ):
384
385   IdKit_setm :=
386   [ [commentC, cat(
387      *****'n * InitializeSizes - set signal model dimensions',
388      'n *',
389      'n * A subroutine which could be used to automate initialization',
390      'n * of the IdKit model interface. This is just a proposal.',
391      'n *****)], newlineC,
392   [functionm, 'static void', 'InitializeSizes', []],
393     [ [equalc, 'V.dim ', '0' ],
394       [equalc, 'Z.dim ', '0' ],
395       [equalc, 'Y.dim ', N[y] ],
396       [equalc, 'X[0].dim', '0' ],
397       [equalc, 'X[1].dim', '0' ],
398       [equalc, 'X[2].dim', N[xy] ],
399       [equalc, 'Wv.dim ', N[wv] ],
400       [equalc, 'Wy.dim ', N[wy] ],
401       [equalc, 'U.dim ', N[u] ],
402       [equalc, 'P.nvect ', N[Pm] ],
403       [matrixm, 'P.dim', op(Coldims) ]
404     ],
405   ],
406 ],
407 ],
408   newlineC ];
409 'TpIC/debugger'(IdKit_setm):
410
411   IdKit_setup :=
412   [ [commentC, cat(
413      *****'n * InitializeParameters - set model's default parameters',
414      'n *',
415      'n * A subroutine which could be used to automate initialization',
416      'n * of the IdKit model interface. This is just a proposal.',
417      'n *****)], newlineC,
418   [functionm, 'static void', 'InitializeParameters', [], [Passign]],
419   newlineC ];
420 'TpIC/debugger'(IdKit_setup):
421
422 IdKitBody :=
423   IdKit_initcond,
424   IdKit_init_u,
425   IdKit_yequ,
426   IdKit_xyequ,
427   IdKit_setm,
428   IdKit_setup;
429
430
431 IdKitFoot := [commentC, cat(
432   *****'n * End-Of-File *****)],
433
434 userinfo(1,'TpICcomment', 'Running the ``macroC'' code generator.'):
435 genC(0,[IdKitHead, IdKitBody, IdKitFoot], filename=cat(FileName,'.c')):
436 userinfo(1,'TpICcomment', 'Code generation completed successfully!'):
437
438 RETURN(NULL):
439 end:

```

Listing A.6: IdKitModel.srC (*continued*).

```

1  ****
2  * xyequ - user supplied state equations
3  *
4  *      dx_dt[*] = fcn(xy[*,u[*],wv[*],t0,t,p(*,*))
5  *
6  * where:
7  * dx_dt[*]      has indices 0..6
8  * xy[*]         has indices 0..6
9  * u[*]          has indices 0..4
10 * wv[*]         has indices 0..2
11 * t0            is the start time of the simulation
12 * t              is the current time of the simulation
13 * p(i,j)        has indices i=0..22 and j=0..4
14 ****
15 void xyequ(t,xy,dx_dt)
16 double *t,*xy,*dx_dt;
17 {
18     static double t2,t3,t16,t21,t22,t23,t24,t32,t37,t41,t42,t47,t48,t50,t51,t52,
19     t54,t57,t59,t64,t69,t70,t71,t74,t81,t82,t87,t90,t94,t97,t104,t107,t111,t116,
20     t118,t121,t123,t124,t126,t127,t128,t129,t131,t132,t134,t140,t147,t152,t153,t154
21     ,t166,t168,t176,t180,t188,t189,t196;
22     t2 = 1/p(2,0);
23     t3 = sqrt(t2);
24     t16 = u[2]*(p(5,0)*C2+p(2,1)*atan(xy[0])*C1);
25     t21 = C7+xy[5]*C57;
26     t22 = (xy[5]*C5+C6)*t21;
27     t23 = t22+C24;
28     t24 = 1/t23;
29     t32 = p(4,0)*(u[0]+u[1]);
30     t37 = p(15,0)*(xy[5]+p(21,0)*C57);
31     t41 = (xy[5]*C19+C20)*t21;
32     t42 = t41+C21;
33     t47 = t16+u[3]*(u[4]*C4+xy[5]*t24*C8)*C9+(t32+t37)*t42*C57+p(6,0)*xy[1];
34     t48 = p(1,1);
35     t50 = p(1,3);
36     t51 = p(1,2);
37     t52 = t48+xy[4]*C57+t50+t51;
38     t54 = xy[5]*C22+C23;
39     t57 = xy[5]*C10+C11;
40     t59 = t52*t54+xy[4]*t57;
41     t64 = u[3]*C9+t32*C57+t37*C57;
42     t69 = xy[5]+C14;
43     t70 = (xy[5]*C12+C13)*t69;
44     t71 = t70+C15;
45     t74 = C16+xy[5]*C17;
46     t81 = (C18+xy[5]*C25)*t69;
47     t82 = t81+C26;
48     t87 = C27+xy[5]*C28;
49     t90 = p(12,0);
50     t94 = C29+xy[5]*C30;
51     t97 = t52*t42*t54+t52*t71*t74+t48*C57+t50*C57+t51*C57+xy[4]*t82*t57+xy[4]*t23
52     *t87+(p(11,0)+t90+p(1,0))*t94*C31;
53     t104 = t23*t82+t71*t42*C57;
54     t107 = t22+C32+t70*C57;
55     t111 = 1/(t59*t104+t107*t97*C57);
56     t116 = t64*t104+t47*t107*C57;

```

Listing A.7: Example of the sub-expression optimization, excerpted from the IdKit subroutine module produced by the TplC IdKitModel code generation template; cf. lines 363–377 of listing A.6.

```

57     t118 = t23*t23;
58     t121 = C33+p(17,0)*C57;
59     t123 = t107*xy[6];
60     t124 = 1/t71;
61     t126 = t123*t124+C33;
62     t127 = log(t126);
63     t128 = 1/t107;
64     t129 = t127*t128;
65     t131 = 1/xy[6]*t71;
66     t132 = t131*C57;
67     t134 = C33+t129*t132;
68     t140 = sqrt(t118*t121*t134*t51/p(14,0));
69     t147 = t41+C35+t81*C57;
70     t152 = t51*t121;
71     t153 = t152*t23;
72     t154 = t128*t134;
73     t166 = t154*C57;
74     t168 = t121*t23;
75     t176 = t51*(t168*t154+C36);
76     t180 = t70+C15+t123;
77     t188 = t23*t124;
78     t189 = 1/t126;
79     t196 = t107*t107;
80     dx_dt[0] = t3*wv[0]*C56+t2*xy[0]*C57;
81     dx_dt[1] = wv[1];
82     dx_dt[2] = wv[2];
83     dx_dt[3] = wv[2];
84     dx_dt[4] = (t47*t59+t64*t97*C57)*t111;
85     dx_dt[5] = t116*t111;
86     dx_dt[6] = (t16+(t140*C34+p(8,0)*xy[3])*xy[6]*t147*C57+p(7,0)*xy[2]+(t153*
87     t154*t71*t74+t152*t23*t134*t128*(C33+xy[6]*C57)*t147*t54+t153*t166+t51*(C33+
88     t168*t166)*t23*t87+t176*xy[6]*t147*t57+t176+t51*t180*t147*t121*(t23*t54+t71*t57
89     *C57)*(t188*t189+(t188+C33)*t127*t128*t132+C33)/t196+t90*t94*C31)*t116*t111*C57
90     )/t51/t180/t147/t121*t24/(t129*t131+t189*C57)*t107*xy[6];
91   }
}

```

Listing A.7: (continued)

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