

Rational Approach to Fire Engineering Design of Steel Buildings

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LUND INSTITUTE OF TECHNOLOGY · LUND · SWEDEN DIVISION OF BUILDING FIRE SAFETY AND TECHNOLOGY REPORT LUTVDG/(TVBB-3002)

OVE PETTERSSON - SVEN ERIK MAGNUSSON -JÖRGEN THOR

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TO FIRE ENGINEERING DESIGN
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Presented at a workshop "Engineering Applications of Fire Technology", April 16-18, 1980, at National Bureau of Standards, Gaithersburg, Maryland, USA

Preface

The present paper describes a rational analytical approach to a fire engineering design of load-bearing structures and partitions. The design method is permitted to be generally applied in Sweden, as one alternative, since about ten years. The method is directly based on the natural fire concept and strictly defined functional requirements and performance criteria.

For facilitating the practical application of the design method to steel structures, a comprehensive design basis has been worked out in the form of diagrams and tables for a direct and quick determination of the maximum steel temperature during a complete compartment fire and the corresponding design load-bearing capacity of the fire exposed structure. The design basis is presented in a manual [4] which is approved for practical use by the National Swedish Board of Physical Planning and Building.

The paper is organized in such a way, that a reader, who only wants to be informed of the practical application of the design method, can limit himself to a study of chapter 3 and the explanatory example. Chapters 1 and 2 are supplementing this description with respect to the general design philosophy behind the design method and the connected structural fire safety characteristics.

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RATIONAL APPROACH TO FIRE ENGINEERING DESIGN OF STEEL BUILDINGS

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A development of analytical design procedures, based on well-defined functional requirements, is an important task of the future fire research within different fields of the overall fire safety concept. Such procedures, successively replacing the present, internationally prevalent, schematic design methods, are necessary for getting an improved economy and for enabling more qualified and reliable fire safety analyses. A derivation of such analytical design systems is also in agreement with the present trend of development of the building codes and regulations in many countries towards an increased extent of functionally based requirements and performance criteria.

In the ideal case, a rational fire design methodology includes as essential components [1]

- * analytical modelling of relevant processes; verification of model validation and accuracy; determination of critical design parameters,
- * formulation of functional requirements, independent of choice of design process and expressed either in deterministic or probabilistic terms,
- * determination of design parameter values, and
- * verification by the means of a reliability analysis that the choice of safety factors leads to safety levels, which are consistent with the expressed functional requirements.

For a fire engineering design of load-bearing structures and partitions, a differentiated analytical procedure is permitted to be applied in Sweden, as one alternative, since about ten years. The procedure constitutes a direct design method based on temperature characteristics of the fully developed compartment fire as a function of the fire load density, the

ventilation of the fire compartment and the thermal properties of the structures enclosing the fire compartment. The design method is approved for a general practical use by the National Swedish Board of Physical Planning and Building [2]. For facilitating the practical application, design diagrams and tables are systematically produced, giving directly, on one hand, the design temperature state of the fire exposed structure, on the other, a transfer of this information to the corresponding design load-bearing capacity of the structure; c.f., for instance [3], [4], [5], [6]. Fig. 1 describes the design method in a summary way.

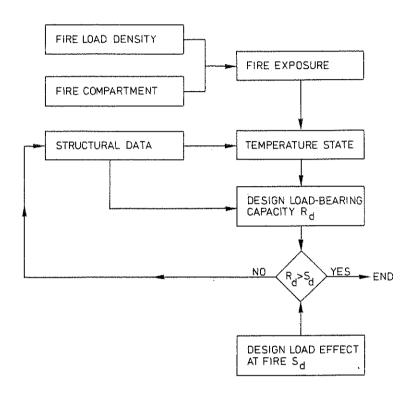


Figure 1. Summary description of a rational design method for fire exposed load-bearing structures

1. Main Principles of an Analytical Design of Fire Exposed Load-Bearing Structures

In a generalized summary way, an analytical design method for fire exposed structures, based on well-defined functional requirements, can be described according to Fig. 2.

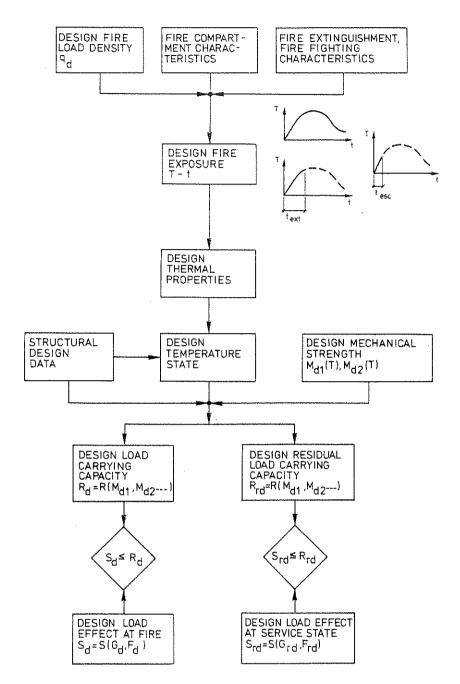


Figure 2. Procedure of a rational, reliability-based design of fire exposed load-bearing structures [1]

The design fire load density, the fire compartment characteristics and the fire extinguishment and fire fighting characteristics constitute the basis for a determination of the design fire exposure, given as the gastemperature-time curve T-t of the fully developed compartment fire. Depending on the type of practical application, the load-bearing function of the structure can be required to be fulfilled for

- * the complete fire process,
- * a shortened fire process, limited by the time $t_{\rm ext}$, necessary for the fire to be extinguished under the most severe conditions, or
- * a shortened fire process, limited by the design evacuation time $\mathbf{t}_{\mathsf{esc}}$ for the building.

Together with the structural design data, the design thermal properties and the design mechanical strength of the structural materials, the design fire exposure gives the design temperature state and the design load-carrying capacity $R_{\mbox{\scriptsize d}}$ as the lowest value during the relevant fire process.

A direct comparison between the design load-carrying capacity R_d and the design load effect at fire S_d decides whether the structure can fulfil its required function or not at the fire exposure. The quantities R_d and S_d then both can be referred to a defined load or a decisive section effect, for instance, a bending moment or a shear force.

Following, for instance the new Draft Code for Loading Regulations, issued by the Nordic Committee for Building Regulations [7], the determination of the design load effect S_d starts from characteristic values of permanent and variable loads G_k and F_k , connected to a defined probability of excess during a specified time period (Fig. 3). A multiplication by partial factors γ and load combination factors ψ transfers the characteristic load values to design loads G_d and F_d . The load combination factors ψ then may be differentiated with respect to whether a complete evacuation of people can be assumed or not in the event of fire. Finally, the design loads are combined and transformed to the design load effect at fire S_d .

Analogously, the design material strength M_d is to be calculated via characteristic strength values M_k at actual temperature, divided by resulting partial factors γ_m (Fig. 4). The characteristic strength values are defined as corresponding to specified fractiles of the probability density distribution. The different partial factors γ_m^1 , γ_m^2 , γ_m^3 , and γ_m^4 , are expressing the influence of the scatter in material strength, the uncertainty of the design model, the uncertainty in relation between material property in the structure and material property determined in test, and the safety class, respectively. The predicted extent of personal and property damage at failure – very serious, serious, not serious – decides the safety class.

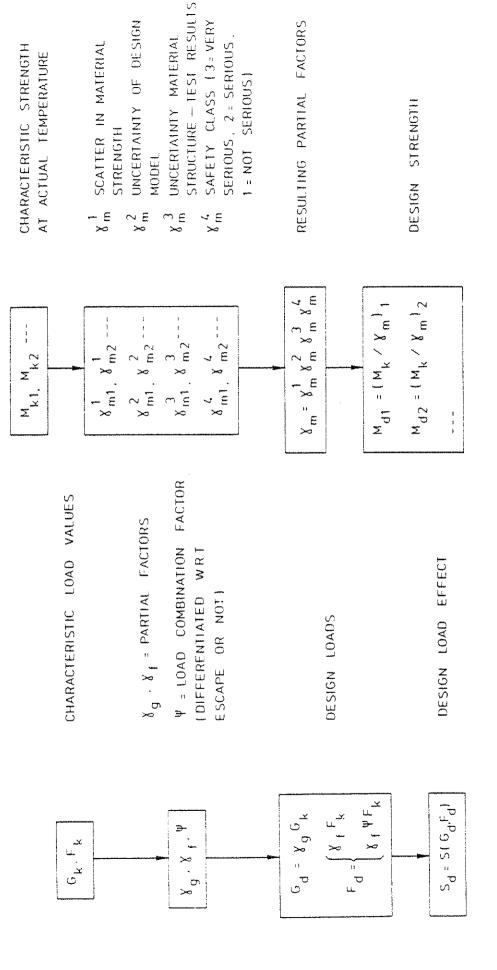


Figure 3. Procedure of determination of design load effect \mathbb{S}_{d}

Figure 4. Procedure of determination of design strength $\mathbf{M}_{\mathbf{d}}$

A similar approach - as outlined for the design load effect \mathbf{S}_d and the design mechanical strength \mathbf{M}_d - can be applied also to the design fire load density \mathbf{q}_d and the design thermal properties of the structural materials.

The level of the functional requirements to be laid down for a structural fire engineering design must be differentiated with respect to such influences as the occupancy, the height and volume of the building, and the importance of the structure or the structural member for the overall stability of the building. This can be met by, for instance, a division of buildings in categories with a related differentiation of the design fire load density and the length of the fire process, to be considered in the design.

For buildings containing activities, which are particularly important from, for instance, an economical point of view, there can be the motive for requiring that the building can be used again after a fire, almost immediately or very soon, for the current activities in a full extent. If the design also comprises such a requirement on re-serviceability of the structure after fire, the design procedure is to be expanded in the following way.

From the time curve of the load-carrying capacity R, the design residual load-carrying capacity R_{rd} of the structure after fire is obtained as end information. This quantity R_{rd} has to be compared with the design load effect at service, non-fire state, on the structure S_{rd} , given by the corresponding characteristic load values, partial factors and load combination factors.

2. Fire Safety of Load-Bearing Structures

In a general sense, the fire engineering design problem is non-deterministic. Performance has to be described and measured in probabilistic terms.

This is one essential perspective from which we have to judge or appraise the building fire safety code systems now in force. Historically, they had to be written without actually stating their objective level of safety and, still far less, without any analytical measurement of the

objectives involved. For this reason, there is an urgent need for future attempts to evaluate the levels of safety inherent in present local and national fire protection regulations and to develop rational, reliability-based design methods, leading to safety levels which are consistent with the relevant functional requirements [1].

For the case that the load-bearing capacity R and the load effect S can be expressed analytically, are statistically uncorrelated and have known probability density functions f_R and f_S , the probability of failure is given by the formula - cf. Fig. 5

$$P_{f} = \int_{0}^{\infty} \int_{0}^{S} f_{S}(s) f_{R}(r) ds dr$$
 (1)

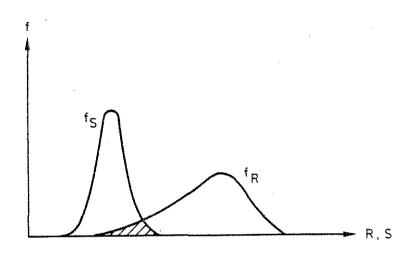


Figure 5. Probability density function f_R and f_S of load-bearing capacity R and load effect S

The computation of the probability of failure P_f can be re-formulated in the following way - Fig. 6. The difference between the load-bearing capacity R and the load effect S defines the safety margin. In the probability density function of the safety margin f_{R-S} , positive values mean survival, negative values failure. The dashed area gives the failure probability P_f .

Ideally, P_f should form the basis for deriving design criteria. However, P_f can be evaluated accurately only if the probability density function

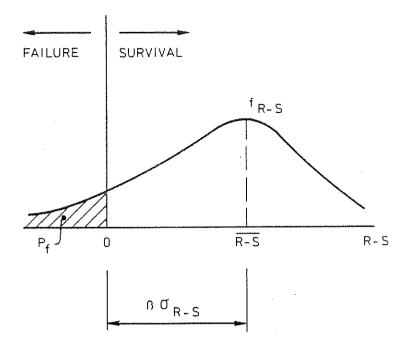


Figure 6. Probability density function f_{R-S} of safety margin R-S and definition of safety index $\boldsymbol{\beta}$

of R-S is known in detail. In practice, this is very seldom the case. Two main alternatives then are open [8], [9]

- * to base a design code format on prescribed distributions of R and S, and
- * to acknowledge the incompleteness of statistical information and disregard the form of the distribution involved.

In the latter case, a design scheme can be based simply on requiring that some minimum safety margin be maintained. In place of requiring that a calculated risk of failure must fall below a specified probability, it may be required that the average safety margin R-S must lie a specified number β standard deviation above zero, giving the formulas

$$\overline{R-S} \ge \beta \sigma_{R-S}$$
 or $\overline{R} \ge \overline{S} + \beta \sqrt{\sigma_R^2 + \sigma_S^2}$ (2)

 σ_{R-S} is the standard deviation of the safety margin R-S, σ_R and σ_S are the standard deviation of R and S, respectively.

The safety index β defines the reliability of, for instance, a design system. A greater value of β then corresponds to a higher safety level.

With this safety measure we can improve our design methods to be more consistent and assess the implications of assumptions and guesses.

A methodology for a probabilistic analysis of fire exposed steel structures, connected to the design method described in chapter 1, has been developed in [10]. The methodology comprises a general systematized scheme for the identification and evaluation of the various sources and kinds of uncertainty in the differentiated structural fire engineering design. The structure of the methodology is quite general and applicable to a wide class of structures and structural elements. To get applicable and efficient final safety measures, the probabilistic analysis is numerically exemplified for an insulated, simply supported steel beam of I-cross section as a part of a floor or roof assembly. The chosen statistics of dead and live load and fire load density are representative for office buildings.

With the basic data variables selected, the different uncertainty sources in the design procedure are identified and dissembled in such a way that available information from laboratory tests can be utilized in a manner as profitable as possible. The derivation of the total or system variance Var(R) in the load-carrying capacity R is divided into two main stages: variability $\text{Var}(T_{\text{max}})$ in maximal steel temperature T_{max} for a given type of structure and a given design fire compartment, and variability in strength theory and material properties for known value of T_{max} .

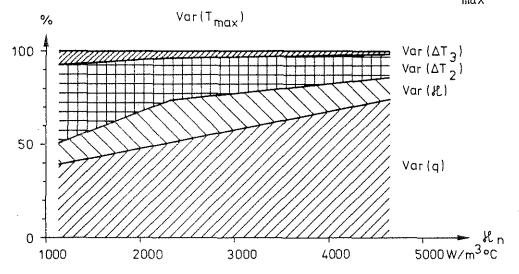


Figure 7. Decomposition of total variance in T_{max} into component variances as a function of insulation parameter κ_n [10]

The results obtained are exemplified in Fig. 7, giving the decomposition of the total variance in maximum steel temperature T_{max} into the component variances as a function of the insulation parameter $\kappa_n = A_i \lambda_i / (V_s d_i)$. A_i is the interior jacket surface area of the insulation per unit length, d_i the thickness of the insulation, λ_i the thermal conductivity of the insulating material, corresponding to an average value for the whole process of fire exposure, and V_s the volume of the steel structure per unit length. Increasing κ_n expresses a decreased insulation capacity.

The component variances refer to the stochastic character of the fire load density q, the uncertainty in the insulation properties κ , the uncertainty reflecting the prediction error in the theory of compartment fires and heat transfer from the fire process to the structural member ΔT_2 , and a correction term reflecting the difference between a natural fire in a laboratory and under real life service conditions ΔT_3 . Analogously, Fig. 8 exemplifies the decomposition of the total variance in the load-carrying capacity R into component variances as a function of the insulation parameter κ_n . The component variances refer to the variability in the maximum steel temperature T_{max} , variability in material strength M, the uncertainty reflecting the prediction error in the strength theory $\Delta \varphi_1$, and the uncertainty due to the difference between laboratory tests and in situ fire exposure $\Delta \varphi_2$.

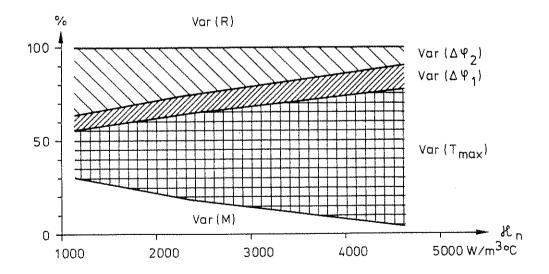


Figure 8. Decomposition of total variance in load-carrying capacity R into component variances as a function of insulation parameter κ_n [10]

The component variances are quantified, whenever possible by comparing the design theory with experiments. System variance is evaluated in two ways: by Monte Carlo simulation and by use of a truncated Taylor series expansion. Employing the Monte Carlo procedure, the mean and variance of R and S have been computed for different values of the ventilation factor of the fire compartment, the insulation parameter κ and the ratio D_n/L_n , where D_n is nominal dead load and L_n nominal live load, used in the normal temperature design. The second moment reliability as a function of these design parameters is evaluated by the safety index formulation according to Eq. (2).

A fragmentary illustration of the results received is given in Table 1, showing the range of variation for the safety index β , as determined for the present Swedish differentiated analytical design model (case II). Varying the opening factor of the fire compartment $A\sqrt{\hbar}/A_t$ from 0.04 to 0.12 $m^{1/2}$ and the ratio between the nominal value of dead load D_n and live load L_n from 1/3 to 3, then leads to a range of β from 1.66 to 2.84. A is the total area of the window openings, h the mean value of the heights of window and door openings, weighed with respect to each individual opening area, and A_t the total interior area of the surface bounding the compartment, opening areas included. For the structural member designed in accordance to the standard fire endurance test (case I), the corresponding range of β will be from 1.77 to 3.69. Completing the present differentiated design model with statistically derived load factors (case III) will improve the consistency of β considerably by giving a very narrow range from 2.35 to 2.45.

 $\underline{\text{Table 1}}.$ Safety index β and probability of failure P_f for different design procedures, applied to an insulated, simply supported steel beam as a part of a floor or roof assembly in office buildings

Design procedure	Range of ß	Range of P _f	(P _f) _{max} /(P _f) _{min}
I. Classification, standard endurance test	1.77 - 3.69	(1-400)10-4	~ 400
II.Present Swedish design model	1.66 - 2.84	(23-500)10 ⁻⁴	~ 20
III = II, improved by statistically derived load fac- tors	2.35 - 2.45	(72-95)10 ⁻⁴	~ 1.5

The corresponding range of the probability of failure P_f is shown in the table, too. Related to this quantity, the difference between the three design procedures is extremely striking with the respective ratios $(P_f)_{max}/(P_f)_{min}$ - 400, 20 and 1.5. The P_f values presented are connected to a probability = 1 for a fire outbreak leading to flashover within the fire compartment.

3. Detailed Description of a Differentiated, Analytical Fire Engineering Design of Steel Structures

As mentioned in the introduction, a differentiated analytical procedure is permitted to be applied in Sweden for a fire engineering design of load-bearing structures and partitions since about ten years. The main principles behind the design precedure and the connected fire safety aspects are dealt with in the proceding chapters.

Applied to fire exposed load-bearing structures or structural members, inside a fire compartment, the design procedure includes the following steps - Fig. 9.

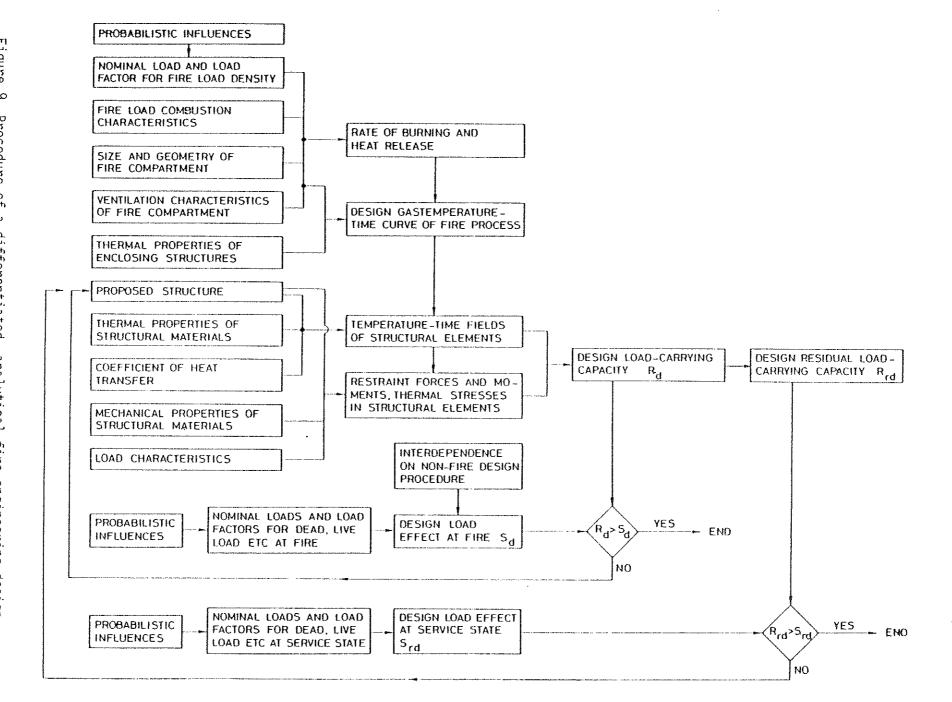
The basis of the design is given by the fully developed compartment fire exposure. Decisive entrance quantities then are

- (1) nominal load and load factor for fire load density,
- (2) combustion properties of this design fire load,
- (3) size and geometry of the fire compartment,
- (4) ventilation characteristics of the fire compartment, and
- (5) thermal properties of structures enclosing the fire compartment.

These quantities jointly determine the rate of burning, the rate of heat release, and the design gas temperature-time curve of the complete fire process. Together with

- (6) structural data for the proposed structure,
- (7) thermal properties of structural materials, and
- (8) coefficients of heat transfer for various surfaces of the structure

this design gas temperature-time curve gives the requisite information for a determination of the transient temperature fields of the fire exposed structure or structural members. With



- (9) mechanical properties of structural materials (Fig. 4), and
- (10) load characteristics

as further entrance quantities the time variation of restraint forces and moments, thermal stresses, and load-carrying capacity R can be determined. The lowest value of R during the complete fire process defines the design load-carrying capacity $\mathbf{R}_{\mathbf{d}}$.

Over nominal loads and load factors for dead load, live load, etc, statistically representative of a fire occasion, the design load effect at fire S_d is defined, interdependent on non-fire design procedure (Fig. 3).

A direct comparison between the design load-carrying capacity $R_{\rm d}$ and the design load effect at fire $S_{\rm d}$ decides whether the structure can fulfilits required function or not at a fire exposure.

Exceptionally, a requirement on re-serviceability of the structure after fire may be included on the fire engineering design. If so, the design residual load-carrying capacity $R_{\rm rd}$ of the structure after fire has to be determined in the design and compared with the design load effect at service, non-fire state, on the structure $S_{\rm rd}$.

For exterior, load-bearing structures, the procedure for a direct, differentiated design will be modified with respect to the thermal exposure. For such a structure, the transient temperature fields are determined by a combined radiation and convection exposure from the flames and combustion gases outside the fire compartment as well as by radiation from the interior of the fire compartment through its window openings; cf., for instance [11], [12]. For the rest, the design procedure is principally the same as for interior, load-bearing structures.

3.1 Fire Load Density and Gas Temperature-Time Curves of a Fully Developed Compartment Fire

At known combustion characteristics of the fire load, the gas temperature-time curve of a fully developed compartment fire can be calculated in the individual practical application from the heat and mass balance equations of the fire compartment with regard taken to the size, geometry and ventilation of the compartment, and to the thermal properties of the structures enclosing the compartment - Fig. 10 [2], [4], [6], [13], [14], [15], [16], [17], [18], [19].

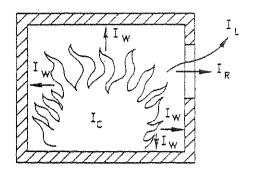


Figure 10. Energy balance equation $I_C = I_L + I_W + I_R$ of a fire compartment. I_C is the heat release per unit time from the combustion of the fuel, and I_L , I_W and I_R the quantities of energy removed per unit time by change of hot gases against cold air, by heat transfer to the surrounding structures, and by radiation through the openings of the compartment, respectively

For interior, load-bearing structures and partitions, the fire engineering design provisionally can be based on gas temperature-time curves T_t -t according to Fig.11, [2], [4], [6], [15], which applies to a fire compartment with surrounding structures made of a material with a thermal conductivity $\lambda = 0.81~\text{W·m}^{-1} \cdot \text{C}^{-1}$ and a heat capacity oc = 1.67 MJ·m⁻³.0C⁻¹ (fire compartment, type A). Entrance parameters of the diagrams are the fire load density q, defined by the formula

$$q = \frac{1}{A_{+}} \sum \mu_{v} m_{v} H_{v}. \qquad (MJ \cdot m^{-2})$$

and the ventilation characteristics of the fire compartment, expressed by the opening factor $A\sqrt{h}/A_+$ (m^{1/2}), where

A = total area of window and door openings (m^2) ,

h = mean value of the heights of window and door openings, weighed
 with respect to each individual opening area (m),

 A_t = total interior area of the surfaces bounding the compartment, opening areas included (m^2) ,

 $m_{_{\rm M}}$ = total weight of combustible material v (kg)

 H_{ν} = effective heat value of combustible material ν of the fire load $(MJ \cdot kg^{-1})$, and

 μ_{ν} = a fraction between 0 and 1, giving the real degree of combustion for each individual component of the fire load.

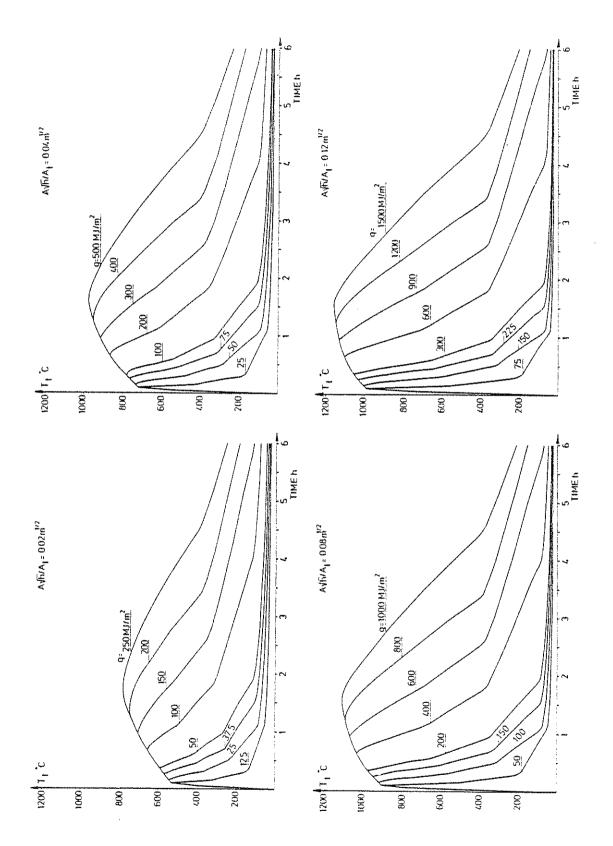


Figure 11. Gas temperature-time curves $T_{\mbox{\scriptsize t}}-t$ of the complete process of fire development for different values of the fire load density q and the opening factor $A\sqrt{h}/A_{\mbox{\scriptsize t}}$. Fire compartment, type A

The non-dimensional factor μ_{ν} is a function of type of fuel, geometrical properties of fuel, and the position of fuel in a fire compartment, among other things. For some types of fire load components, μ_{ν} will depend on the time of fire duration and on the gas temperature-time characteristics of the fire compartment. Bookcases and floor coverings are examples of fire components whose real degree of combustion is low, and whose μ_{ν} values are probably appreciably below unity. At present, however, there is a lack of experimentally substantiated and verified μ_{ν} values, and it is therefore usually necessary in the course of practical design to employ a fire load calculation with μ_{ν} generally put equal to unity.

As a rule, the design fire load density is to be determined on the basis of statistical investigations for the type of building or premises in question. Such statistical investigations have been carried out for dwellings, offices, administration buildings, schools, stores, and hospitals [2], [4], [6]. As a temporary regulation, the Swedish Building Code authorizes the 80 percent level of the statistical distribution curve to be applied as the design fire load density.

A fragmentary example of the results, obtained in the statistical investigations of the fire load density q, is given in Fig. 12 [20], which refers some distribution curves, representative to dwellings in the suburbs and the central parts of Stockholm. In the figure the fire load density is specified on one hand by a minimum value, which only includes the highly inflammable components, and on the other hand by a maximum value, corresponding to all combustible material in the compartment, excluding floor covering. Table Al in the appendix summarizes the average and standard deviation of the fire load density as well as the design fire load density from the investigations, determined according to Eq. (3) with $\mu_{\rm N}$ = 1 [2], [4], [6].

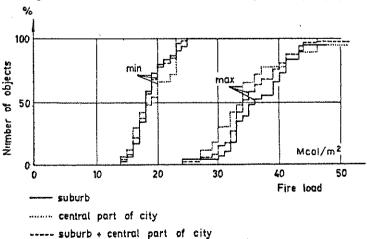


Figure 12. Distribution curves for the fire load density q, defined according to Eq. (3), representative to dwellings in the suburbs and the central parts of Stockholm. 1 Mcal/ m^2 = 4.19 MJ/ m^2

The gas temperature-time curves in Fig. 11 have generally been determined on the assumption of ventilation controlled fires. For fires, which are fuel bed controlled in reality, this assumption leads to a structural fire engineering design on the safe side in practically every case, giving an overestimation of the maximum gastemperature and a simultaneous, partly balancing underestimation of the fire duration. For the minimum load-bearing capacity, which thermally can be seen as an integrated effect, the gas temperature-time curves in Fig. 11 give reasonably correct results, verified in [4], [10], [16].

As pointed out, the gas temperature-time curves in Fig. 11 apply to a certain fire compartment, type A, specified with respect to the thermal properties of its surrounding structures. Fire compartments with surrounding structures of deviating thermal properties can be transferred to fire compartment, type A, via effective values of the fire load density q_f and the opening factor $(A\sqrt{h}/A_t)_f$ in accordance to Table A2 in the appendix [2], [4], [6].

3.2 Opening Factor A√h/At

According to Fig. 11, the opening factor of a fire compartment is a fundamental concept in calculating the gastemperature-time curve of the process of fire development.

For a fire compartment with only <u>vertical openings</u>, the opening factor is defined by the quantity $A\sqrt{h}/A_+$, where - cf. Fig. 13

A = total area of the window and door openings (m^2) ,

h = mean value of the heights of window and door openings (m), weighed with respect to each individual opening area, and

 A_t = total interior area of the surfaces bounding the compartment, opening areas included (m^2).

If a fire compartment also comprises <u>horizontal openings</u>, an equivalent opening factor $(A\sqrt{h}/A_+)_e$ can be determined by the formula [15]

$$(A\sqrt{h}/A_{t})_{e} = f_{k} (A\sqrt{h}/A_{t})_{v}$$

$$(4)$$

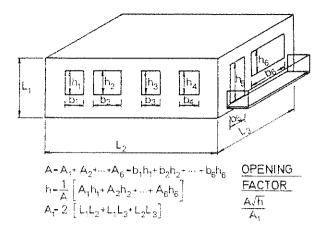


Figure 13. Definitions of the total opening area A, the weighed mean value of the opening height h, the total interior area of the surrounding structures A_{t} , and the opening factor $A\sqrt{\hbar}/A_{t}$ of a fire compartment

where $(A\sqrt{h}/A_t)_V$ is the opening factor, corresponding to the vertical openings of the compartment, calculated according to Fig. 13, and f_k a dimensionless multiplier, given by the alignment chart in Fig. 14. For the notations used in this chart, then see Fig. 15.

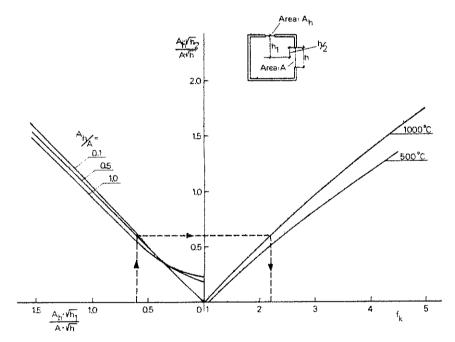


Figure 14. Alignment chart for a determination of the equivalent opening factor $(A/h/A_t)_e$ of a fire compartment with vertical as well as horizontal openings. For notations, see Fig. 15

A determination of the equivalent opening factor over Eq. (4) and Fig. 14 presupposes that the gas flow through the horizontal openings of the roof is not predominant. This can be examined via the quotient $A_h \sqrt{h}_2 / A \sqrt{h}$, which has an upper limit at which the applied gas flow model ceases to be valid. This upper limit is given by the values

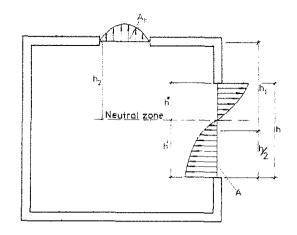


Figure 15. Gas flow mechanism for a fire compartment with vertical and horizontal openings

$$\frac{A_{h}\sqrt{h}_{2}}{A\sqrt{h}} = \begin{cases} 1.76 \text{ at } T_{t} = 1000^{\circ}C\\ 1.37 \text{ at } T_{t} = 500^{\circ}C \end{cases}$$
 (5)

At these limit values, the neutral zone coincides with the upper edge of the vertical opening and tests have indicated the validity of the model up to these upper limits [21].

3.3 Design Temperature State of Fire Exposed, Uninsulated Steel Structures

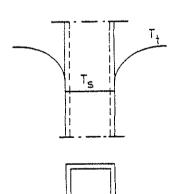


Figure 16. Fire exposed, uninsulated steel structure. T_t = gas temperature within fire compartment, T_s = steel temperature at time t

For a fire exposed, <u>uninsulated steel structure</u>, the energy balance equation gives the following formula for a determination of the steel temperature-time curve T_s -t - Fig. 16

$$\Delta T_{s} = \frac{\alpha}{\rho_{s} c_{ps}} \cdot \frac{F_{s}}{V_{s}} (T_{t} - T_{s}) \Delta t \qquad (^{\circ}C)$$
 (6)

where

 ΔT_s = change of steel temperature (${}^{O}C$) during time step $\Delta t(s)$,

 α = coefficient of heat transfer at fire exposed surface of structure $(W \cdot m^{-2} \cdot {}^{\circ}C^{-1})$

 ho_s = density of steel material (7850 kg·m⁻³), c_{ps} = specific heat of steel material (J·kg⁻¹·oc⁻¹),

 F_s = fire exposed surface of steel structure per unit length (m), V_s = volume of steel structure per unit length (m²),

= gas temperature (${}^{\circ}C$) within fire compartment at time t (s).

Eq. (6) presupposes that the steel temperature T_s is uniformly distributed over the cross section of the structure at any time t.

The coefficient of heat transfer α can be calculated from the approximate formula

$$\alpha = 23 + \frac{5.77 \epsilon_{r}}{T_{t} - T_{s}} \left[\left(\frac{T_{t} + 273}{100} \right)^{4} - \left(\frac{T_{s} + 273}{100} \right)^{4} \right] \quad (W \cdot m^{-2} \cdot {}^{0}C^{-1})$$
 (7.)

giving an accuracy which is sufficient for ordinary practical purposes. ϵ_{\star} is the resultant emissivity which for practical applications can be chosen according to the following table, giving values which generally are on the safe side.

1. Column, fire exposed on all sides	$\epsilon_r = 0.7$
2. Column, outside a facade	0.3
3. Floor structure, composed of steel beams with a	
concrete slab on the lower flange of the beams	0.5
4. Steel beams with a floor slab on the upper flang	ge
of the beams	
4a. Beams of I cross section with width/height	≥ 0.5 0.5
4b. Beams of I cross section with width/height	< 0.5 0.7
4c. Beams of box cross section and trusses	0.7

More accurate values of the resultant emissivity $\epsilon_{\mbox{\scriptsize m}}$ can be determined for the application alternative 4 - steel beams with a floor slab, supported on the upper flange of the beams - from the diagrams of Fig. 17 and 18, applicable to floor structures with the flames completely below the steel beams and reaching the slab, respectively [22]. For the emissivity of the

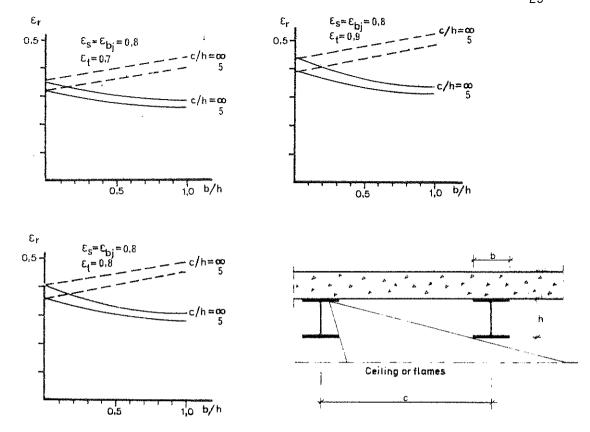


Figure 17. Resultant emissivity ε_r for steel beams with a floor slab, supported on the upper flange of the beams. Flames completely below the steel beams. $\varepsilon_{bj} = \varepsilon_{t} = \varepsilon_{t}$

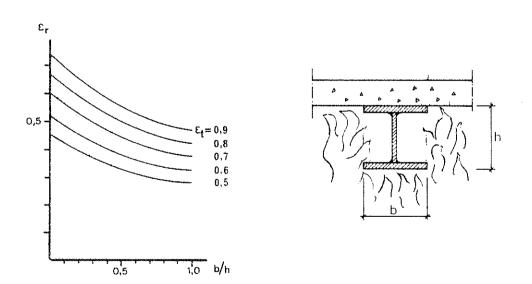


Figure 18. Resultant emissivity ε_r for steel beams of I cross section with a floor slab, supported on the upper flange of the beams. Flames reaching the slab. ε_t = emissivity of the flames

flames $\epsilon_{\rm t}$, the value 0.85 is to be inserted, if not any other value can be proved to be more correct.

At a given gas temperature-time curve T_t -t of the fire compartment, the steel temperature T_s can be directly calculated from Eqs. (6) and (7) with regard taken to the temperature dependence of c_{ps} and α . Such computations have been carried out in a systematized way, giving the basis of design in Table A3 in the appendix [4]. From this table, the maximum steel temperature $T_{s,max}$ during a complete compartment fire can be determined directly as a function of the effective fire load density q_f , the effective opening factor $(A\sqrt{h}/A_t)_f$, the F_s/V_s ratio and the resultant emissivity ϵ_r . The values of the table are connected to gas temperature characteristics according to Fig. 11.

Table A4 in the appendix gives some guide-lines for the determination of the structural parameter $F_{\rm s}/V_{\rm s}$ for different types of application.

3.4 Design Temperature State of Fire Exposed, Insulated Steel Structures

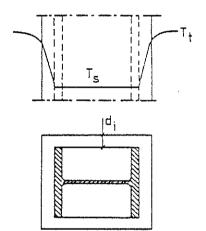


Figure 19. Fire exposed, insulated steel structure. T_t = gas temperature within fire compartment, T_s = steel temperature at time t

For a fire exposed, <u>insulated steel structure</u>, a simplified energy balance equation gives the following formula for a direct determination of the steel temperature-time curve T_s -t - Fig. 19

$$\Delta T_{s} = \frac{A_{i}}{(1/\alpha + d_{i}/\lambda_{i})\rho_{s}c_{ps}V_{s}} (T_{t} - T_{s})\Delta t \qquad (^{\circ}C)$$
(8)

with the additional quantities

 A_i = interior jacket surface area of insulation per unit length (m),

d; = thickness of insulation (m),

 λ_{i} = thermal conductivity of insulating material (W·m⁻¹·°C⁻¹).

Eq. (8) presupposes that the steel temperature T_s is uniformly distributed over the cross section of the structure at any time t, that the temperature gradient is linear and the heating contribution negligible for the insulation, and that the heat transfer is one-dimensional.

Computations, originating from Eqs. (7) and (8), enable a production of a systematized design basis, facilitating an analytical, differentiated fire engineering design in practice. An example from such a design basis is referred in Table A5 i the appendix [4], giving the maximum steel temperature $T_{s,max}$ during a complete compartment fire for varying values of the effective fire load density q_f , the effective opening factor $(A\sqrt{h}/A_t)_f$, the structural parameter A_i/V_s , and the insulation parameter d_i/λ_i . The values of the table are connected to gas temperature characteristics according to Fig. 11.

Table A5 was computed on the assumption of a constant thermal conductivity of the insulating material $\lambda_{\rm j}$, chosen as an average value for the whole compartment fire process. Calculations, carried through systematically, are verifying that this average value of $\lambda_{\rm j}$ approximately coincides with the value, determined for an insulation temperature equal to the maximum steel temperature $T_{\rm s,max}$. Table A6 in the appendix gives the thermal conductivity $\lambda_{\rm j}$ of some insulation materials as a function of the temperature [4].

For a specific insulating material, systematized design diagrams or tables can be computed very accurately with regard to the temperature dependence of the thermal properties of the steel as well as the insulating material. The influence of an initial moisture content and of a disintegration of the insulating material can be considered, too. Practically, such a determination can be carried out over a numerical data processing by computers on the basis of a finite difference or a finite element method. A great number of design tables, computed according to such an accurate procedure, are presented in [4]. Table A7 in the appendix exemplifies this, giving the maximum steel temperature $T_{s,max}$ at varying fire and structural design characteristics for a fire exposed steel structure, insulated with mineral wool of density $\rho_i = 150 \text{ kg m}^{-3}$ at varying effective fire load density q_f , effective opening factor $(A/\bar{h}/A_t)_f$, quotient A_i/V_s , and thickness d_i of the insulation.

Table A8 in the appendix gives some guide-lines for the determination of the structural parameter A_i/V_s for different types of application.

3.5 Design Temperature State of Fire Exposed Floor or Roof Assembly with Suspended Ceiling

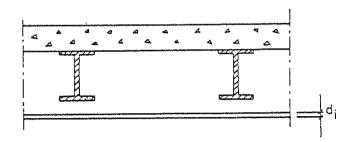


Figure 20. Floor structure, composed of a reinforced concrete slab, Toad-bearing steel beams, and an insulating ceiling

In [4], an analytical model is derived for a simplified determination of the temperature-time fields of a steel beam structure according to Fig. 20 - composed of a reinforced concrete slab, load-bearing steel beams, and an insulating ceiling - exposed to a fire from below. By applying this computational model in a systematic way, a design basis has been determined, facilitating a calculation of the steel beam temperature T_{ς} , assumed as uniformly distributed over the cross section of the beams. The design basis is exemplified in Table A9 in the appendix [4], which gives the maximum steel beam temparature $T_{s,max}$ during a complete compartment fire for varying values of the effective fire load density $q_{\mathbf{f}}$, the effective opening factor $(A\sqrt{h}/A_t)_f$, the structural parameter F_s/V_s , and the insulation parameter d_i/λ_i . F_s denotes the surface area of the steel beam, less the part covered by the concrete slab, and V_s the volume of the steel beam, per unit length. The values, given in brackets in the table, denote the corresponding maximum temperature at the centre level of the ceiling. The values of the table are connected to gas temperature characteristics according to Fig. 11.

For several types of steel beam structures with a suspended, insulating ceiling, the fire resistance of the ceiling and its fastening devices will be the decisive design criterion instead of the temperature of the steel beams. The ceiling can get a serious crack formation or fall down, partially or completely, after a comparatively short fire exposure. Under such conditions, the maximum steel beam temperature

cannot be determined from Table A9 solely on the basis of the thickness ${\rm d}_i$ and the thermal conductivity λ_i of the ceiling. If results are available for a type of a suspended ceiling from a standard fire resistance test, these results can be used for deriving an effective value of the insulation parameter ${\rm d}_i/\lambda_i-({\rm d}_i/\lambda_i)_{\mbox{eff}}$ - which describes the real fire behaviour of the suspended ceiling, including its fastening devices. From the test results, also a possible critical failure temperature of the suspended ceiling can be estimated. Cf., further [4].

After the determination of $(d_i/\lambda_i)_{\mbox{eff}}$ and the critical temperature of a type of a suspended ceiling, the analytical differentiated fire design can be carried out by a direct application of Table A9. Parallelly, then the maximum temperature at the centre level of the ceiling according to the table must be controlled against the critical temperature of the ceiling.

Effective d_i/λ_i values and critical temperatures have been determined for a number of types of suspended ceilings in a series of standard fire resistance tests performed at the National Swedish Institute for Testing and Metrology in Stockholm [23]. The compositions of these suspended ceilings, the results obtained and the characteristics derived are set out in Table AlO in the appendix [4].

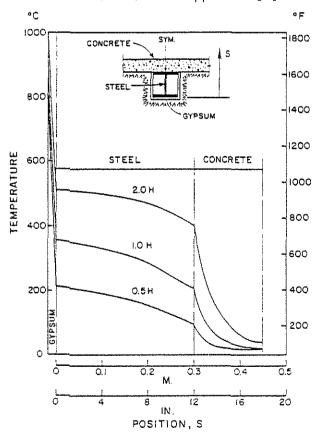


Figure 21. Calculated temperature distribution along line of symmetry of a steel beam, insulated by a 16 mm gypsum board (density 770 kg·m $^{-3}$) and carrying a 150 mm concrete slab on top flange, at selected times of a thermal exposure according to ISO 834 [24]

The design basis, reproduced in Tables A3, A5, A7 and A9, generally assumes the steel temperature to be uniformly distributed over the cross section of the beam or column at any time t. A more accurate theory, which enables a determination of the temperature variation over the cross section of the steel structure, is presented in [24], together with computer routines. The algorithm described can easily be coupled to most finite element programs. An illustration of the capability of the theory is given in Fig. 21, which shows calculated temperature distribution along the line of symmetry of a gypsum insulated steel beam with a concrete slab at the top flange at selected times of a standard fire resistance test according to ISO 834.

3.6 Design Temperature State of Fire Exposed Partitions

As a complement to the design temperature state of fire exposed load-bearing steel structures, dealt with above, also some remarks will be given on the fire engineering design of <u>partitions</u>. The performance requirements for partitions imply that these must prevent a penetration of flames and hot gases and limit the rise in temperature on the unexposed side of the construction during a complete compartment fire.

An analytical method for a determination of the temperature-time field in a multi-layer partition is presented in [25]; cf. also [4]. The method considers the temperature dependence of the thermal material properties, an initial moisture content, and a possible material disintegration at specified temperature criteria. An illustrating application of the method is shown in Fig. 22 [25], which gives a summary conception of the fire behaviour of a steel stud wall, insulated on each side with two 13 mm gypsum plaster sheets, type Gyproc, of density 790 kg·m⁻³, fire exposed on one side and acting as a partition. The behaviour has been determined on the basis of temperature dependent thermal properties of gypsum plaster material according to Fig. 23 and a critical failure temperature for a gypsum plaster sheet of 550°C on that side of the sheet facing away from the fire. The results of full scale fire tests confirm this failure criterion.

Fig. 22a describes the fire behaviour of the wall, when it is fire exposed on one side by a compartment fire with gas temperature-time

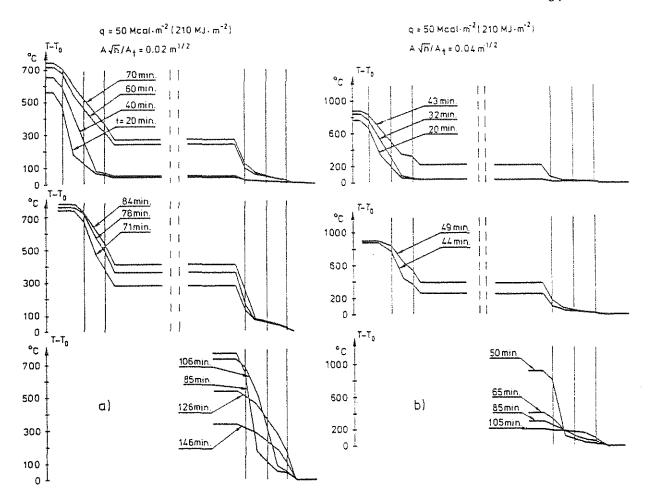


Figure 22. Calculated temperature-time fields for a steel stud wall, insulated on each side with two 13 mm gypsum plaster sheets, type Gyproc, of density 790 kg·m $^{-3}$. The wall is fire exposed on one side with compartment fire characteristics according to Fig. 11: a) q = 50 Mcal·m $^{-2}$ (210 MJ·m $^{-2}$), A \sqrt{h}/A_t = 0.02 m $^{1/2}$; b) q = 50 Mcal·m $^{-2}$ (210 MJ·m $^{-2}$), A \sqrt{h}/A_t = 0.04 m $^{1/2}$. T₀ = temperature at time t = 0 [25]

characteristics according to Fig.11 - fire load density q = 50 Mcal·m⁻² (210 MJ·m⁻²), opening factor $A\sqrt{h}/A_t = 0.02 \, \text{m}^{1/2}$. The figure gives a calculated failure of the directly fire exposed gypsum plaster sheet after about 70 min and of the next gypsum plaster sheet after about 85 min. The maximum temperature rise on the unexposed side of the wall amounts to 180°C during the complete fire process, i.e. precisely the maximum permissible value according to [2]. Fig. 22b analogously describes the fire behaviour of the wall, when it is exposed to a more rapid compartment fire - opening factor $A\sqrt{h}/A_t = 0.04 \, \text{m}^{1/2}$ - at the same fire load density q. The increase of the opening factor results in a considerably decreased value of the maximum temperature rise on the unexposed side of the wall, which amounts to only about 55°C in this case.

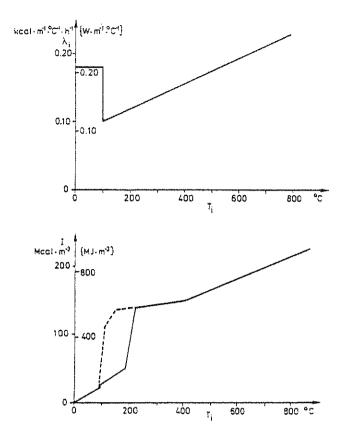
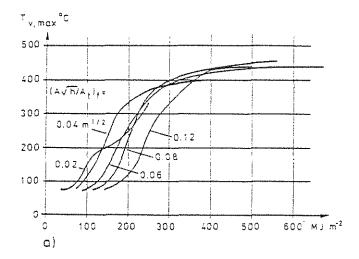


Figure 23. Thermal conductivity λ_i and enthalpy I (= $\int_{c_p}^{c_p} dT$) as a function of insulation temperature T_i for gypsum plaster slabs, type Gyproc, of density 790 kg·m⁻³. For enthalpy I, full line refers to a rapid heating and dashed line to a slow heating [25], [26]

Systematic calculations of the type, illustrated by Fig. 22, lead to design diagrams as shown in Fig. 24[4], [6], giving the maximum temperature $T_{v,max}$ during a complete fire process on the unexposed side of a steel stud-gypsum plaster sheeting wall as a function of the effective fire load density q_f and the effective opening factor of the fire compartment $(A\sqrt{h}/A_t)_f$. The two diagrams apply to an insulation on each side of the wall with one and two 13 mm gypsum plaster sheets, type Gyproc, of density 790 kg·m⁻³, respectively. The calculated $T_{v,max}$ values are to be compared with the corresponding maximum temperature, permitted in the Swedish Building Code, which implies 200° C as an average temperature and 240° C as a temperature over limited areas of the unexposed side of the partition [2].



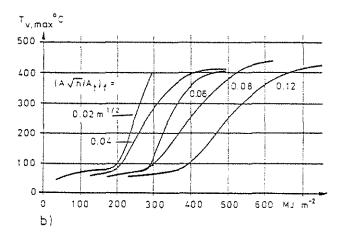


Figure 24. Maximum temperature $T_{v,max}$ during a complete fire process according to Fig. 6 on the unexposed side of a steel-gypsum plaster sheeting wall as a function of the effective fire load density q_f and the effective opening factor $(A\sqrt{h}/A_t)_f$ of the fire compartment. The wall is insulated on each side with one (fig a) or two (fig b) 13 mm gypsum plaster sheets, type Gyproc, of density 790 kg·m⁻³ [4], [6]

3.7 Design Load Effect and Design Load-Bearing Capacity of Fire Exposed Steel Structures

In the design, it is to be proved that the design load-bearing capacity of the fire exposed structure does not decrease below the design load effect during the complete process of fire development. The design load effect then is to be chosen on the basis of the most unfavourable combination of dead load, live load, snow load and wind load.

Table All in the appendix refers the load values, specified in the Swedish Building Code for a differentiated, analytical, structural fire engineering design [2], [4], [6]. The specified load values are differentiated with respect to whether a complete evacuation of people can be

assumed or not in the event of fire. The values include a safety factor which roughly considers the probability of a fully developed fire and the probability of the presence of the maximum load at the fire occasion.

By applying the design tables A3 to A10, the maximum steel temperature $T_{s,max}$ can be determined comparatively quickly for an uninsulated or insulated steel structure, exposed to a complete compartment fire with gas temperature-time characteristics according to Fig.11. The corresponding design load-bearing capacity of the structure then is obtained by design diagrams of the type exemplified in Fig. 25, 26 and 27.

Fig. 25 and 26 [4], [6] give the design load-bearing capacity ($\rm M_{cr}$, $\rm P_{cr}$, $\rm q_{cr}$) of fire exposed beams of constant I cross section at different types of loading and support conditions, as a function of the steel beam temperature T_s. The design curves in Fig. 25 apply to a slow rate of heating - assumed to be 4 $^{\rm OC\cdot min^{-1}}$, followed by a cooling with a rate of 1.33 $^{\rm OC\cdot min^{-1}}$ - and Fig. 26 gives the correction ΔB of the load-bearing capacity coefficient B due to a more rapid rate of heating. In the formulas for the load-bearing capacity

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\sigma_s = yield stress of steel material at room temperature (MPa), L = span of beam (m), W = elastic modulus of beam cross section (m^3).
```

The design curves in Fig. 25 and 26 have been determined on the basis of the deformation curve of the fire exposed beams calculated by an analytical model, presented in [27], which takes into account the softly rounded shape of the stress-strain curve of steel at elevated temperatures as well as the influence of creep strain. As can be seen from Fig. 26, this influence of creep begins to be noticeable for ordinary structural steels at temperatures in excess of about 450°C. The load-bearing capacity of the beams is defined by the limit deflection criterion according to ROBERTSON and RYAN [28].

The diagrams in Fig. 27 [4] determine the variation with the steel temperature T_s of the relationship between the buckling stress σ_{cr} and the slenderness ratio λ for fire exposed columns, axially loaded in compression. The diagrams apply to steel having a yield stress at room temperature σ_s = 220, 260 and 320 MPa, respectively, and are valid under the

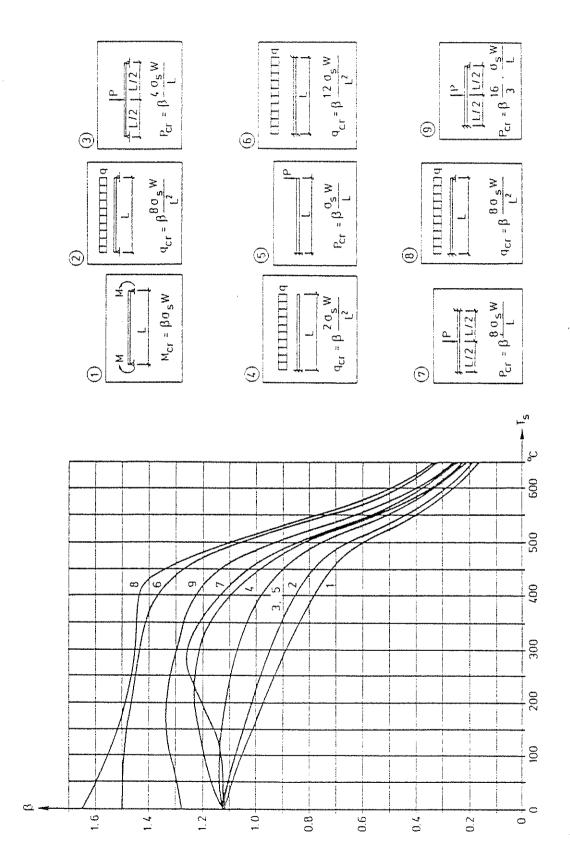


Figure 25. Coefficient B for determination of critical load (Mcr, Pcr, q_{cr}) for fire exposed beams of I cross section at different types of loading and support conditions, as a function of the steel beam temperature T_s . The curves have been calculated for a slow rate of heating of 4 ${}^{0}\text{C} \cdot \text{min}^{-1}$ and a subsequent cooling, assumed to be one third of the rate of heating [4], [6]

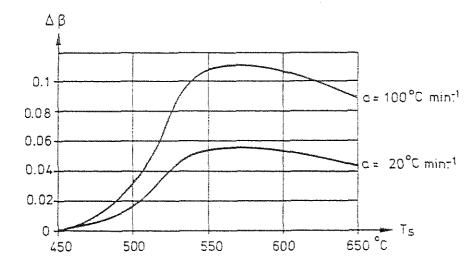


Figure 26 . Increase $\Delta\beta$ of coefficient β , determined according to Fig. 25, for a rate of heating a \geq 4 C·min , as a function of the steel beam temperature T $_{c}$ [4], [6]

presumption that the column is unrestrained with respect to longitudinal expansion during the fire exposure. The $\sigma_{\rm Cr}^{-\lambda}$ curves have been computed for an initially deflected and excentrically loaded column on the basis of data on the change of the 0.5 % proof stress $\sigma_{0.5}^{-}$ and the secant modulus with the temperature, obtained in tension tests at a very slow rate of loading. This implies that a considerable influence of short-time creep at elevated temperatures is included.

For a fire engineering design of columns, partly restrained to a longitudinal expansion, reference is made to [4].

The design curves, reproduced in Fig. 25, 26 and 27, are generally based on the assumption of a uniformly distributed temperature over the cross section of the steel structure at any time t during the fire exposure. By this assumption, the design curves are directly connected to Tables A3, A5, A7 and A9, determining the design temperature state of the steel structure.

If the analytical, differentiated design of fire exposed steel structures will be further developed in future towards a more accurate determination of the design temperature state, with regard taken to the temperature variation over the cross section of the steel structure, this will also require a more refined basis of design for the transfer of the design temperature state to the design load-bearing capacity of the fire exposed structure. The first attempts of developing such a more refined design

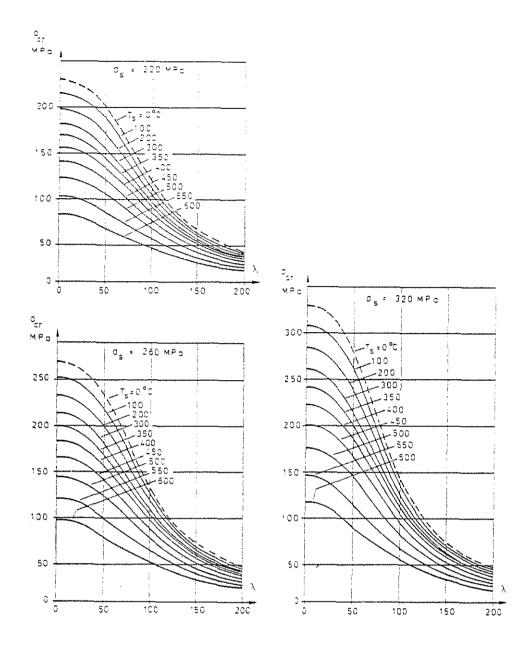
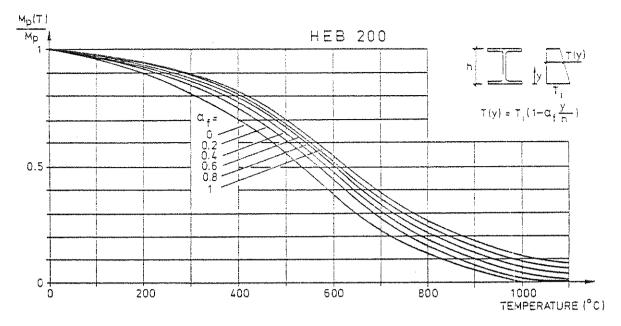


Figure 27. Variation with steel temperature T of the relationship between buckling stress σ_{Cr} and slenderness ratio λ for fire exposed steel columns, axially loaded in compression, free to expand longitudinally and made of steel having a yield stress at room temperature σ_{S} = 220, 260 and 320 MPa, respectively [4], [6]

basis now can be noticed in the literature. As a fragmentary example of this development, Fig. 28 [29] shows the calculated variation of the plastic bending moment of a fire exposed steel I cross section as a function of the maximum temperature for various linear temperature distributions over the cross section.



<u>Figure 28</u>. Calculated variation of plastic bending moment $M_p(T)$ in terms of various linear temperature distribution over height of a steel I cross section [29]

4. Concluding Remarks

A differentiated procedure is presented for an analytical fire engineering design of load-bearing steel structures and partitions. The procedure is a direct design method based on gas temperature-time characteristics of a complete compartment fire, which depends on the fire load density, the ventilation of the fire compartment and the thermal properties of the structures enclosing the fire compartment. The practical use for the design procedure has been approved by the National Swedish Board of Physical Planning and Building.

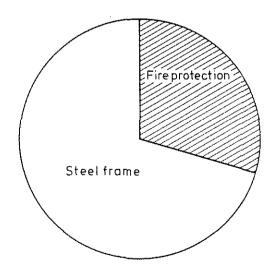
For the practical application of the design procedure, a comprehensive design basis in the form of diagrams and tables has been worked out for a direct determination of the maximum steel temperature during a complete compartment fire and the corresponding design load-bearing capacity of the fire exposed structure. Included in this paper is also a worked out example, providing a rough impression of the more important features of the methodology.

Compared with the conventional fire engineering design, based on classification and results of standard fire resistance tests, the presented analytical design procedure has a more logical structure, based on well-defined functional requirements and performance criteria. Of the ensuing advantages, the following are seen to be the main ones:

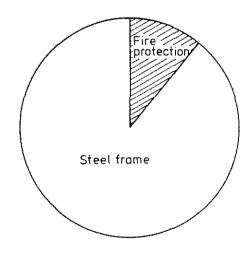
- 1. More consistent safety levels. This point has been elaborated in chapter 2.
- 2. Better economy. The cost of structural fire protection is, as a rule, hard to itemize and the cost saving consequences have been quantified only in a few cases. Rough estimates indicate that while the cost for conventional structural fire protection may exceed 30 per cent of the cost for the steel frame material, the corresponding percentage may be as low as 10 with the design procedure based on analytical modelling, see Fig. 29. The latter figure is based on the assumption that the advantages are fully exploited of integrating the design of the structural steel fire protection into the overall design process (inner and outer walls are used as fire protection whenever possible, concrete floor slabs are placed on the lower flange of the girders, inherently providing a smaller area to insulate, etc.).

Finally, it is recognized that the design system presented is not homogeneous with respect to the present basis of knowledge for the different design steps. Naturally, this can be put forward as a criticism of the system. However, such a remark is not essential. Instead, this fact ought to be used as an important guide on how to systematize a future research work for making possible a successive improvement of the system.

COSTS FOR FIRE PROTECTION



Fire protection—according to conventional standard design method



Fire protection according to integrated, rational design method

Figure 29.

Example

Introduction_

The following example is solved in order to illustrate the practical application of the design procedure and to outline the computational scheme. The calculations may, for two reasons, seem somewhat lengthy and elaborate. Firstly, the problem to be solved has been chosen in order to include and emphasize several of the more important aspects of the design methodology. Secondly, for pedagogic reasons the calculations have been presented in a rather detailed manner. Several more worked out examples, giving a more balanced view of the practicality of the approach, may be found in Ref. 4.

Background Data

A two-storey high school building is designed with a load-carrying steel frame of columns and simply supported girders according to Fig. 30. The material in columns and girders is steel quality 1412 with a nominal yield strength at room temperature $\sigma_{\rm S}$ = 260 MPa.

The dimension of the center columns is HE 200 A and the girders in the floor-slab system are of size HE 280 B. Relevant data are given i Fig. 30. The center distance for girders and columns in the longitudinal direction of the building is $4\ m.$

The concrete floor assembly system is designed according to the figure. The dead weight of the system is 7.0 kN m $^{-2}$. The dead weight of the upper floor assembly system, including the weight of the roof, is 7.0 kN m $^{-2}$. The attic cannot be used for storage.

The fire compartment is defined by the materials in walls, floor and ceiling, by its geometric dimensions and the ventilation characteristics of door and windows. The horizontally bounding structures are the concrete slabs, inner walls are light-weight concrete with a density = 500 kg m^{-3} . For the outer walls, two alternatives are to be studied

- alternative (a) sheet steel mineral wool with density 50 kg m $^{-3}$ sheet steel
 - (b) from inside 13 mm gypsum plaster board with density 790 kg m $^{-3}$ 100 mm mineral wool with density 50 kg m $^{-3}$ brick with density 1800 kg m $^{-3}$

484 kN

The task is to investigate if center columns and floor girders must be fire insulated. If so, determine the required insulation when using Unitherm fire retardant paint.

A design condition is that complete evacuation of the building in case of fire cannot be guaranteed.

Step 1. Determination of the Design, Static Load

(a) Floor assembly girders Dead weight of floor assembly system Live load according to Table All Total, excluding dead weight of girders Load per unit girder length, including estimated dead weight for girders 7.0 kN m^{-2} 9.0 kN m^{-2}

(b) Upper central column Dead weight of upperceiling assembly system, including roof Snow load = normal design snow load 1 kN m $^{-2}$ Total Load per column = $7 \cdot 4 \cdot 8.0$ (Dead load of column neglected)

(c) Lower central column Dead weight of upper floor assembly system, including roof Snow load as (b) Dead weight of ceiling assembly system, including girders Live load according to (a) Total Load per column (dead load of column neglected)

Step 2. Determination of Effective Fire Load Density and Effective Ventilation Factor

7-4-17.3

The total bounding area of the fire compartment, including door and windows, is

$$A_{t} = 2L_{1}L_{2} + 2L_{1}L_{3} + 2L_{2}L_{3} = 2 \cdot 2.5 \cdot 7.0 + 2 \cdot 2.5 \cdot 16.0 + + 2 \cdot 7.0 \cdot 16.0 = 35.0 + 80.0 + 224.0 = 339 m2$$
 (a)

Design fire load density for movable furnishings is given by Table Al, $q_1 = 117 \text{ MJ m}^{-2}$. To this must be added the fire load from the combustible flooring. The weight of the flooring is 1.5 kg m⁻² with an effective calorific value = 21 MJ kg⁻¹. This gives a contribution to the fire density =

$$q_{floor} = \frac{1.5 \cdot 21 \cdot 7 \cdot 16}{339} = 10 \text{ MJ m}^{-2}$$

Wall and ceiling lining materials are assumed incombustible. The total fire load density will be

$$q = q_1 + q_{floor} = 117 + 10 = 127 \text{ MJ m}^{-2}$$
 (b)

When determining the opening factor of the fire compartment, all window panes are assumed to be broken as a consequence of the fully developed fire. If the door is assumed closed and intact during the complete fire process, the opening factor will be

$$A = A_1 + A_2 + ... = 1.5(5 \cdot 1.5 + 3.0) = 15.75 \text{ m}^2$$

 $h = 1.5 \, \text{m}$

$$\frac{A\sqrt{h}}{A_{+}} = \frac{15.75 \sqrt{1.5}}{339} = 0.0569 \text{ m}^{1/2}$$
 (c)

If the door is assumed open from outbreak of the fire, the opening factor equals

$$A = 15.75 + 0.9 \cdot 2.1 = 15.75 + 1.89 = 17.64 \text{ m}^2$$

$$h = \frac{\Sigma A_{\nu} h_{\nu}}{\Sigma A_{\nu}} = \frac{15.75 \cdot 1.5 + 1.89 \cdot 2.1}{17.64} = 1.56 \text{ m}$$

$$\frac{A_{\nu} h_{\nu}}{A_{+}} = \frac{17.64 \sqrt{1.56}}{339} = 0.0650 \text{ m}^{1/2}$$
(d)

The Tables A3 and A5, which give the relation between maximal steel temperature $T_{s,max}$ and the combination of fire load density and opening

factor, indicate that the alternative with the lower opening factor value will give the higher steel temperature. Accordingly, the value of 0.0569 $\rm m^{1/2}$ for the opening factor will be chosen as basis for further calculations.

Effective Fire Load Density and Effective Opening Factor

The concept of effective fire load density q_f and effective opening factor $(A\sqrt{h}/A_t)_f$ translates the values of fire load density and opening factor for the existing fire compartment to those of fire compartment type A, see Table A2. The purpose is to get an equivalent gastemperature-time curve from the number of curves computed for fire compartment type A and keep the volume of the design data base within reasonable limits.

Alternative (a)

Bounding structures of the fire compartment comprise the following material types and areas:

concrete floor assembly, area $2 \cdot 7 \cdot 16.0 = 224 \text{ m}^2$ inner walls of lightweight concrete, area $\sim 2.5 \cdot 7.0 + 2.5 \cdot 16.0 = 57.5 \text{ m}^2$ (door closed)

outer wall sheet steel - 100 mm mineral wool - sheet steel, area $2.5\cdot7.0+2.5\cdot16.0-1.5\cdot(5\cdot1.5+3.0) = 41.8 \text{ m}^2$

The relative proportions are 69, 18 and 13 percent respectively. The existing fire compartment can, with regard to thermal characteristics, be described as a combination of fire compartment type B (100 percent concrete), type C (100 percent light weight concrete) and type H (100 percent sheet steel with mineral wool insulation). The value of $K_{\rm f}$ is given by

$$K_f = \frac{69}{100} (K_f)_B + \frac{18}{100} (K_f)_C + \frac{13}{100} (K_f)_H = 0.69 \cdot 0.85 + 0.18 \cdot 3.0 + 0.13 \cdot 3.0 = 1.52$$

The fire compartment can also be seen as a combination of fire compartments B, D and H. In this case $\rm K_{\it f}$ will be given by

$$K_{f} = \frac{13}{100}(K_{f})_{H} + \frac{18}{50}(K_{f})_{D} + \frac{69-18}{100}(K_{f})_{B} = 0.13\cdot3.0 + 0.36\cdot1.35 + 0.51\cdot0.85 = 1.31$$
(e)

These are the two possible alternatives to derive a K_f -value. According to the comments in Table A2 the lowest of the derived K_f -values is to be used in the further calculations. The effective values of fire load density q_f and opening factor $(A\sqrt{h}/A_t)_f$ are now given by

$$q_f = K_f q = 1.31 \cdot 127 = 166 \text{ MJ m}^{-2}$$
 (f)

$$(A\sqrt{h}/A_t)_f = K_f A\sqrt{h}/A_t = 1.31 \cdot 0.0569 = 0.0745 \text{ m}^{1/2}$$
 (g)

Alternative (b)

In this alternative, the bounding structures comprise concrete floor slab, area $2 \cdot 7.0 \cdot 16.0 \approx 224 \text{ m}^2$ inner walls of lightweight concrete, area $\sim 2.5 \cdot 7.0 + 2.5 \cdot 16.0 = 57.5 \text{ m}^2$ outer wall 13 mm gypsum plaster board with density 790 kg m⁻³ - 100 mm mineral wool with density 50 kg m⁻³ - brick with density 1800 kg m⁻³, area = 41.8 m^2 .

With regard to its thermal characteristics, the enclosure may be seen as a combination of fire compartments of type B, D and E. A linear interpolation will give as a result that fire compartment type D is to be included as a negative term. This is not permitted according to the comments in Table A2. As a consequence, the factor K_f will have to be derived with the thermal effects of the fire compartment outer wall approximated.

An assumption that the wall material is lightweight concrete will give results on the conservative side. The factor $\mathbf{K}_{\mathbf{f}}$ is then derived from the following expression

$$K_f = \frac{31}{50}(K_f)_D + \frac{69-31}{100}(K_f)_B = 0.62 \cdot 1.35 + 0.38 \cdot 0.85 = 1.16$$
 (h)

Other combinations are possible, but give higher $\mathrm{K}_{\mathrm{f}}\text{-values}.$

The effective values of the fire load density $\mathbf{q_f}$ and opening factor $(\mathbf{A}\sqrt{h}/\mathbf{A_t})_{\mathbf{f}}$ will be

$$q_f = K_f \cdot q = 1.16 \cdot 127 = 147 \text{ MJ m}^{-2}$$
 (i)

$$(A\sqrt{h}/A_t)_f = K_f \cdot (A\sqrt{h}/A_t) = 1.16 \cdot 0.0569 = 0.066 \text{ m}^{1/2}$$
 (j)

Step 3. Maximum Steel Temperature

(a) Floor assembly girders

As an initial attempt will be calculated the maximum steel temperature with the girders unprotected.

According to the table in section 3.3 the value of the resultant emissivity ε_{γ} may be chosen = 0.5. As only the lower flange of the girders is exposed to fire, the $F_{\rm S}/V_{\rm S}$ -ratio is expressed by - cf. Table A4 -

$$F_s/V_s = b/bt = 1/t = 1/0.018 = 55.6 \text{ m}^{-1}$$
 (k)

For a fire compartment with enclosing structures designed according to alternative (a), Table A3 gives, with $q_f = 166$ MJ m $^{-2}$, $(A\sqrt{h}/A_t)_f = 0.0745$ m $^{1/2}$, $\epsilon_r = 0.5$ and $F_s/V_s = 55.6$ m $^{-1}$, the following values for the maximum steel temperature T_s , max

For the girders situated in fire compartment alternative (b) and with $q_f = 147$ MJ m⁻², $(A\sqrt{h}/A_t)_f = 0.0660$ m^{1/2}, $\epsilon_r = 0.5$ and $F_s/V_s = 55.6$ m⁻¹ the corresponding interpolations give

Fig. 25, indicating the relation between load carrying capacity and steel temperature for a fire-exposed steel girder, shows that the computed values of $T_{s,max}$ are too high to be acceptable. The girders will have to be protected and in a first attempt is chosen a two coat Unitherm fire retardant paint.

According to Table A6, the effective d_i/λ_i -value for this insulation system is d_i/λ_i = 0.065 m² °C W⁻¹.

The maximum steel temperature is taken from Table A5 valid for insulated fire-exposed steel members. For the girders situated in fire compartment alternative (a) the computational scheme is as follows - q_f = 166 MJ m⁻², $(A\sqrt{h}/A_t)_f$ = 0.0745 m^{1/2}

$$\frac{A_{i}}{V_{s}} = \frac{1}{t} = \frac{1}{0.018} = 55.6 \text{ m}^{-1} \qquad \text{(Table A8)} \qquad (n)$$

$$\frac{A_{i}\lambda_{i}}{V_{s}d_{i}} = \frac{55.6}{0.065} = 855 \text{ Wm}^{-30}\text{C}^{-1}$$

$$\left(\frac{A\sqrt{h}}{A_{t}}\right)_{f} \qquad \frac{A_{i}\lambda_{i}}{V_{s}d_{i}} \qquad T_{s,max}$$

$$\frac{600}{1000} \qquad 285$$

$$0.06 \qquad 855 \qquad 330 \qquad \longleftarrow \text{ interpolated value}$$

$$\frac{1000}{0.08} \qquad 375 \qquad (o)$$

$$\frac{600}{0.08} \qquad 245$$

$$0.08 \qquad 855 \qquad 290 \qquad \longleftarrow \text{ interpolated value}$$

$$\frac{1000}{1000} \qquad 330$$

$$T_{s,max} = 300^{\circ}\text{C for } (A\sqrt{h}/A_{t})_{f} = 0.0745 \text{ m}^{1/2}$$

Corresponding calculations for fire compartment alternative (b) give - with $q_f=147$ MJ m⁻² and $(A\sqrt{h}/A_t)_f=0.060$ m^{1/2} -

(b) Columns

The F_s/V_s -ratio of the center column is given by - cf. Table A4

$$\frac{F_s}{V_s} = \frac{2h + 4b - 2d}{\text{cross section area}} = \frac{0.38 + 0.80 - 0.013}{53.8 \cdot 10^{-4}} = 217 \text{ m}^{-1}$$
 (q)

This F_s/V_s -value is considerably larger than the F_s/V_s -ratio for the floor assembly girders. Other circumstances being equal, the maximum steel temperature T_s will be higher than the corresponding temperature of the girders. The fact that the resultant emissivity is higher for the column, fire exposed in all sides, than for the girder - cf. section 3.3 - also works in the same direction. It follows that the centre columns must be protected.

As a first attempt, an insulation with two-coat Unitherm fire retardant paint is chosen. According to Table A6, the $\rm d_i/\lambda_i-value$ is = 0.065 $\rm m^2$ °C W⁻¹. The $\rm A_i/V_s-value$ is given by

$$\frac{A_i}{V_s} = \frac{2h + 4b - 2d}{cross section area} = 217 \text{ m}^{-1}$$
 (r)

Hence

$$\frac{A_i \lambda_i}{V_S d_i} = \frac{217}{0.065} = 3340 \text{ W m}^{-3} \text{ oc}^{-1}$$

The maximum steel temperature T $_{s,max}$ is calculated on the basis of Table A5a for the case of columns placed inside fire compartment alternative (a) - q_f = 166 MJ m $^{-2}$, $(A_t/\bar{h}/A_t)_f$ = 0.0745 m $^{1/2}$

and for the columns inside fire compartment alternative (b) with $\rm q_f=147~MJ~m^{-2}$, $\rm (A\sqrt{h}/A_t)_f=0.0660~m^{1/2}$

With the center columns insulated with a three coat Unitherm fire retardant paint, the effective $d_i/\lambda_i = 0.085~\text{m}^2~\text{O}\text{C}~\text{W}^{-1}$ (cf. Table A6), and an analogous calculation gives the maximum steel temperatures

$$T_{s,max} = 545^{\circ}C \tag{u}$$

for fire compartment alternative (a)

$$T_{s,max} = 530^{\circ} C \tag{v}$$

for fire compartment alternative (b).

Step 4. Calculation of Critical Loads

(a) Floor assembly girders

The calculations in the last section demonstrated that the maximum steel temperature of the floor assembly beams, insulated with a two coat Unitherm fire retardant paint, was nearly identical for the two fire compartment alternatives. The maximum value is - cf. Eqs. (o) and (p)

$$T_{s,max} = 300^{\circ}C$$

The corresponding smallest value of the load carrying capacity or the critical load is obtained from Fig. 25. As the maximum temperature does not exceed 450° C, the influence of creep deformation and variation in heating up rate can be neglected, implying that Fig. 26 lacks relevance in this instance.

For existing loading and supporting conditions, curve No. 2 in Fig. 25 is applicable, and the value of the critical load $q_{\rm cr}$ is given by

 $\beta = 0.95$

$$q_{cr} = \beta \frac{8\sigma_s W}{12} = 0.95 \frac{8 \cdot 260 \cdot 10^3 \cdot 1.38 \cdot 10^{-3}}{7^2} = 55.7 \text{ kN m}^{-1}$$
 (x)

which exceeds the design load = 37 kN m^{-1} - see step 1. The conclusion is, that with the chosen fire protection, the floor assembly girders will be able to fulfil their load carrying function throughout the complete fire exposure.

(b) Columns

The columns are assumed to be unbraced between the floor assembly levels. Buckling in the weak axis direction will be decisive. It is further assumed that the support condition of the columns are such that the effective buckling length L is equal to the centrum distance between the floor assemblies, 2.8 m.

The slenderness ratio λ of the center columns will be, with i $_{\mbox{min}}$ devoting the least radius of gyration of the cross-sectional area

$$\lambda = \frac{L}{i_{min}} = \frac{2.8}{0.0498} = 56 \tag{y}$$

With known values for the slenderness ratio λ and maximum steel temperature $T_{s,max}$ the allowable buckling stress σ_{cr} is obtained from Fig. 27. (The steel quality of the columns corresponds to a nominal yield strength at room temperature σ_{s} = 260 MPa).

For the center columns inside fire compartment alternative (a) and insulated with a two coat Unitherm fire retardant paint, the following values are obtained

$$T_{s,max} = 605^{\circ}C$$
, Eq. (s)
 $\sigma_{cr} = 62 \text{ MPa}$
 $N_{cr} = \sigma_{k}A = 62.53.8.10^{-4} = 0.335 \text{ MN} = 335 \text{ kN}$ (z)

The minimum value of the buckling load $N_{\rm cr}$ in this case falls below the calculated design load N=484 kN. The insulation with a two-coat Unitherm fire retardant paint is insufficient for fire compartment alternative (a). An increase in the Unitherm-insulation to a three-coat painting gives

$$T_{s,max} = 545^{\circ}C$$
, Eq. (u)
 $\sigma_{cr} = 87 \text{ MPa}$
 $N_{cr} = 87 \cdot 53.8 \cdot 10^{-4} = 0.470 \text{ MN} = 470 \text{ kN}$ (aa)

and the fire protection is still insufficient. The difference from the required capacity of 484 kN is quite small however. It is surmised that an increase in the insulating capacity, i.e. the $\rm d_i/\lambda_i$ -value, from 0.085 $\rm m^2$ °C w⁻¹, valid for the three coat Unitherm treatment, to 0.09 m² °C W⁻¹ should give adequate protection. With sprayed mineral wool as fire insulation material, this insulating capacity is obtained with a layer thickness d_i of 10 mm, see Table A6, which gives the variation of thermal conductivity λ_i with temperature for a number of insulating materials. Assuming that the average insulation temperature approximately is equal to maximum steel temperature $T_{s,max} \approx 525^{\circ} \text{C}$, Table A6 gives

$$\lambda_{i} = 0.10 \text{ W m}^{-1} \text{ oc}^{-1}$$

$$\frac{d_i}{\lambda_i} = \frac{0.01}{0.10} = 0.1 \text{ m}^2 \text{ oc W}^{-1}$$

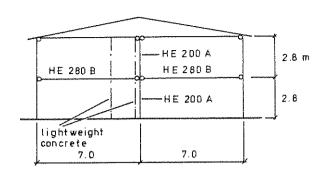
Consequently, adequate fire protection for the columns is offered by the application of 10 mm sprayed mineral wool.

For the centre columns inside fire compartment alternative (b) and protected with a three-coat Unitherm fire retardant paint the calculations show

$$T_{s,max} = 530^{\circ}C$$
, Eq. (v)
 $\sigma_{cr} = 93 \text{ MPa}$
 $N_{cr} = 93 \cdot 53.8 \cdot 10^{-4} = 0.500 \text{ MN} = 500 \text{ kN}$ (ab)

i.e. a minimum buckling load exceeding the required design load $N = 484 \, \mathrm{kN}$. A protection with a three coat-Unitherm fire retardant paint is obviously sufficient under these conditions.

It is assumed, when calculating the buckling loads, that the columns are free to longitudinally expand during the thermal exposure from the fire. For design situation where this assumption is not valid, the calculations must be based on design curves, specifically taking into account the effect of a partially restrained thermal expansion. Reference is made to [4].



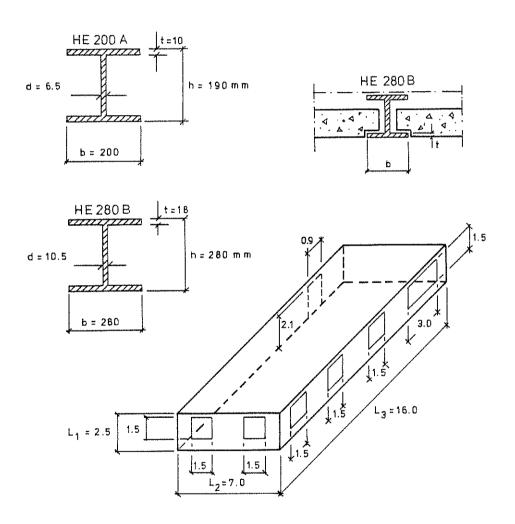


Figure 30.

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APPENDIX

Table A1. Fire load characteristics according to recent Swedish investigations – fire load density q defined according to Eq (3) with $\mu_{\nu}{=}1$

Type of fire	Average		Standard		Design	
compartment	Mcal·m ⁻²	{MJ·m ⁻² }	Mcal·m ⁻²	n {MJ·m ⁻² }	Mcal·m 2	{MJ·m ⁻² }
1 Dwellings 1)						
1a Two rooms and a kitchen	35.8	{150}	5.9	{24.7}	40.0	{168}
10 Three rooms and a kitchen	33.1	{139}	4.8	{20.1}	35.5	{149}
2 Offices ²⁾						
2a Technical offi- ces	29.7	{124}	7.5	{31.4}	34.5	{145}
2b Administrative offices	24.3	{102}	7.7	{32.2}	31.5	{132}
2c All offices, investigated	27.3	{114}	9.4	{39.4}	33.0	(138)
3 Schools ²)	<u> </u>	, <u> </u>				
3a Schools - junior level	20.1	{84.2}	3.4	{14.2}	23.5	{98.4}
3b Schools - middle level	23.1	{96.7}	4.9	{20.5}	28.0	{117}
3c Schools - senior level	14.6	{61.1}	4.4	{18.4}	17.0	{71.2}
3d All schools, investigated	19.2	{80.4}	5.6	{23.4}	23.0	{96.3}
4 Hospitals	27.6	{116}	8.6	{36.0}	35.0	{ 147}
5 Hotels ²⁾	16.0	{67.0}	4.6	{19.3}	19.5	`{81.6}

¹⁾ Floor covering excluded

²⁾ Only moveable fire load components included

Table A2. Coefficient K_f for transforming a real fire load density q and a real opening factor of a fire compartment $A\sqrt{h}/A_t$ to an effective fire load density q_f and an effective opening factor $(A\sqrt{h}/A_t)_f$ corresponding to a fire compartment, type A

$$q_f = K_f q$$
 $(A\sqrt{h}/A_t)_f = K_f A\sqrt{h}/A_t$

Type of fire		0peni	ng factor	· A√ħ/A _t	m ^{1/2}	
compartment	0.02	0.04	0.06	0.08	0.10	0.12
Type A	1	1	1]		1
Type B	0.85	0.85	0.85	0.85	0.85	0.85
Type C	3.00	3.00	3.00	3.00	3.00	2.50
Type D	1.35	1.35	1.35	1.50	1.55	1.65
Type E	1.65	1.50	1.35	1.50	1.75	2.00
Type F ¹⁾	1.00-	1.00-	0.80-	0.70-	0.70-	0.70-
	0.50	0.50	0.50	0.50	0.50	0.50
Type G	1.50	1.45	1.35	1.25	1.15	1.05
Type H	3.00	3.00	3.00	3.00	3.00	2.50

The lowest value of K_f applies to a fire load density $q > 500 \text{ MJ} \cdot \text{m}^{-2}$, the highest value to a fire load density $q \le 60 \text{ MJ} \cdot \text{m}^{-2}$. For intermediate fire load densities, linear interpolation gives sufficient accuracy.

The different types of fire compartment are defined as follows

<u>Fire compartment, type B</u>: Bounding structures of concrete.

Fire compartment, type C: Bounding structures of lightweight concrete (density $\rho = 500~\text{kg}\cdot\text{m}^{-3}$).

Fire compartment, type D: 50% of the bounding structures of concrete, and of 50% lightweight concrete (density ρ = 500 kg·m⁻³).

Fire compartment, type E: Bounding structures with the following percentage of bounding surface area: 50% lightweight concrete (density ρ = 500 kg.m^{-3}),

33% concrete.

17% of from the interior to the exterior: plasterboard panel (density $\rho=790~{\rm kg\cdot m^{-3}}$), 13 mm in thickness - diabase wool (density $\rho=50~{\rm kg\cdot m^{-3}}$), 10 cm in thickness - brickwork (density $\rho=1800~{\rm kg\cdot m^{-3}}$), 20 cm in thickness.

Fire compartment, type F: 80% of the bounding structures of sheet steel, and 20% of concrete. The compartment corresponds to a storage space with a sheet steel roof, sheet steel walls, and a concrete floor.

Fire compartment, type G: Bounding structures with the following percentage of bounding surface area: 20% concrete, 80% of from the interior to the exterior: double plasterboard panel (density ρ =790 kg·m⁻³), 2xl3 mm in thickness - air space, 10 cm in thickness - double plasterboard panel (density ρ = 790 kg·m⁻³), 2xl3 mm in thickness.

Fire compartment, type H: Bounding structures of sheet steel on both sides of diabase wool (density ρ = 50 kg·m⁻³), 10 cm in thickness.

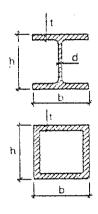
For fire compartments, not directly represented in the table, the coefficient K_f can either be determined by a linear interpolation between applicable types of fire compartment in the table or be chosen in such a way as to give results on the safe side. For fire compartments with surrounding structures of both concrete and lightweight concrete, then different values can be obtained of the coefficient $\mathsf{K}_f,$ depending on the choice between the fire compartment types B, C, and D at the interpolation. This is due to the fact that the relationships, determining $\mathsf{K}_f,$ are non-linear. However, the $\mathsf{K}_f\text{-values}$ of the table are such that a linear interpolation always gives results on the safe side, irrespective of the alternative of interpolation chosen. In order to avoid an unnecessarily large overestimation of K_f , that alternative of interpolation is recommended which gives the lowest value of K_f . At the determination of K_f , it is not allowed to combine types of fire compartments in such a way, that any of them gives a negative contribution to K_f .

Table A3. Maximum steel temperature T_{s,max} (0 C) for unisolated steel structure as a function of effective fire load density q (Mcal·m-2) {MJ·m-2}, effective opening factor $A\sqrt{h}/A_{t}$ (m^{1/2}), F_s/V_s ratio (m-1), and resultant emissivity ϵ_{r} [4]

q	ΑVñ	F _s		s,mai		q	<u>AV</u> h	Fs		s.max			Α√ħ	F _s	Т,	s,max			<u>AV</u> h	Fs	T,	.max	
"	A,	V _s	0,3	€, 0,5	ε, 0,7	"	At	Vs	ε, 0,3	ε, 0,5	ε, 0,7	q	A	V.	ε, 0,3	ε, 0,5	ε, 0,7	q	Ar	v,	ů, 0,3	ε, 0,5	ε, 0.7
	0,01	50 75 100 125 150 200 400	325 365 395 410 425 435 450 335	345 385 410 425 435 445 450 380	370 405 425 435 440 445 450		0,01	50 75 100 125 150 200 400	400 435 450 460 470 475 480	420 445 460 476 475 460 485	440 460 470 475 480 485 515			25 50 75 100 125 150 200	390 465 495 495 500 505 505	425 480 500 505 505 516 510 515	445 490 500 505 510 510 513			75 100 125 150 300	455 510 525 530 530 535 535	490 525 530 535 540 540 540	500 530 535 535 540 540 540 540
	0,02	75 100 125 150 200 400	410 445 480 500 540 575	445 490 520 540 560 585	475 520 545 565 575 585		0,02	75 100 125 150 200 400	500 540 565 585 605 625	540 575 600 605 620 680	563 595 610 615 625 630	20	0,02	56 75 100	500 560 595 615 625 635	550 600 620 630 640 645	575 620 630 640 645 650	25 (105)		50 75 100 125 50 75	555 610 640 650 570 650	600 640 650 655 645 720	625 650 655 660 700 760
		50 75 100	285 350 405	320 400 460	365 450 510	-	0,04	50 75 100	400 490 550	455 550 610	516 600 655	[84]	6,04	100 50 75	650 495 355	650 565 650	650 625 70 0		0,06	25 50 75	355 525 640	420 500 690	510 700 780
10	0,04	125 150 200 300	450 495 550 625	515 555 605 660	555 595 645 690	15 (63)		125 150 56 75	600 635 340 425	655 680 400 490	696 710 475 575		0,06	100 25 50 75	650 285 440 540	700 340 505 610	740 415 600 700		0,08	75 100 25	480 590 660 240	590 700 775 260	655 770 - 365
[42]	0,06	50 75 100 125	235 305 365 415	275 370 410 450	336 425 485 545	***************************************	0,06	100 125 150 200	500 550 590 650	550 600 630 700	630 680 720 755		0.05	100 50 75 100	G15 390 485 5G5	675 496 596 670	755 530 670 785	,	0,12	50 75 100 125	400 500 590 650	460 550 655 720	590 700 800
	0.08	150 200 300 50 75 100 125	450 520 615 206 270 330 360	455 550 680 250 330 400 450	580 660 735 300 400 460 510		0,08	50 75 100 125 150 200	300 380 450 500 555 625 260	375 465 545 595 650 725 290	430 535 605 670 710 785		0,12	125 150	630 200 310 425 490 550 600	715 235 375 480 560 620 665	790 305 500 610 700 775		0,01	25 50 75 100 125 150 300 400	505 545 555 560 560 565 565	525 555 560 560 565 565 565	540 560 560 566 565 565 570 570
		150 200 300 50	410 480 600 170	510 590 700 200	580 660 760 260		0,12	75 100 125 150	340 390 450 500	390 460 540 600	500 600 675 750			25 50 75 100	490 510 520	460 505 515 520	480 515 520 520	30 {126]	0,02	50 75 100	600 - 650 660	640 670 675	666 670 675
	6,12	75 100 125 150 200 300	220 240 260 310 380 450	260 310 380 430 500 620	350 400 540 626 700 800		0, 61	200 25 50 75 100 125	355 430 460 475 480	385 450 475 480 485	410 465 480 485 490		0,01	150 200 400 50	520 523 530 530 530 530	525 525 530 530 575 620	525 526 530 530 605 635		0,04	50 75 25 50 75	705	705 780 500 680 775 665	750 800 580 760 -
	0,01	50 75 100 125 150	365 410 430 440 450	355 425 445 450 455	405 435 450 460 460			150 200 400 50 75	485 485 490 460 530	490 495 500 515 570	495 500 500 550 595		0,62	100 125 150 200 50	615 630 645 650 525	635 645 650 660	650 650 655 665		0,08	75 25 50 75 100 25	290 460 590 663	775 540 660 740 560	440 650 770 -
	0,02	200 400 50 75 100	455 465 455 455 500 525	460 470 435 500 540 555	405 - 470 470 535 560		0,62	100 125 150 200 400	565 505 610 625 635	600 610 620 635 645	615 636 635 645	22,5 {94,5}	0,04	100 25 50	620 680 320 480 565 655	590 740 380 550 650 725	735 760 460 645 740 785	45 {190}	0,12	50 25 50 75 100	540 210 360 450	760 270 440 555 650	325 520 640 730
		125 150 200 400 50	550 570 600	570 590 605	575 580 600 605 450		0, 04	50 75 100 125 25	450 545 600 650	515 000 660 700	575 655 705 740 370		0,68	50	430 540 610 215	540 650 730 255	605 725 780 350	90 (350)	0,30	125 25 50 75	595 425 650	735 545 790	790 635 890
12,5		75 100	415 485 535 570 636	485 550 600 625 665	540 660 640 665 700	17,5 [73,5]	0,06	50 75 100 125 50	255 390 490 565 620 345 440	300 455 555 620 670 435 530	550 655 710 750 490 600		0,12	50 75	360 465 540 625 650	415 540 615 675 746	540 650 750 800			<u> </u>	<u> </u>	······································	
[52,5]		75 100 125 150	365 425	495	495 560 610 650 705		0,08	100 125 150 25 50	500 565 615 160	605	670		·		···								
	0,08	300 75 100 125 150 200	670 250 325 385 435 485 550	740 315 400 473 530 585 660	770 360 455 535 600 650 730		0,12	75 100	350 425 475 525	430 505 575 645	550 650 725 775												
	0,12	300 50 75 100 125 150 200	655 200 240 280 340 350 500 600	770 250 320 460 450 510 600 720	330 410 510 620 690 760																		

Table A4. F_S/V_S for different types of fire exposed, uninsulated steel structures

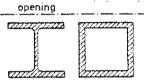
Column within a fire compartment



$$\frac{F_s}{V_s} = \frac{2h + 4b - 2d}{cross section area}$$

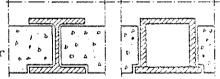
$$\frac{F_s}{V_s} = \frac{2h + 2b}{cross section area}$$

Column, immediately outside a window opening



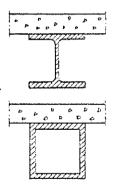
$$\frac{F_s}{V_s} = \frac{2h + b}{\text{cross section area}}$$

Floor structure, composed of steel beams with a concrete slab, supported on the lower flange of the beams



$$\frac{F_s}{V_s} = \frac{b}{bt} = \frac{1}{t}$$

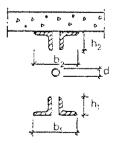
Beams with a floor slab, supported on the upper flange of the beams



$$\frac{F_s}{V_s} = \frac{2n + 3b - 2d}{cross section area}$$

$$\frac{F_s}{V_s} = \frac{2h + b}{\text{cross section area}}$$

Floor slab beams of truss type (F_s/V_s is determined for each part of the truss)



$$\frac{F_s}{V_s} \text{ (lower flange)} = \frac{2b_1 + 2h_1}{\text{cross section area}}$$
of lower flange

$$\frac{F_s}{V_s} \text{ (upper flange)} = \frac{b_2 + 2h_2}{\text{cross section area}}$$
of upper flange

$$\frac{F_s}{V_s} \text{(diagonal)} = \frac{4}{d}$$

Table A5. Maximum steel temperature T_{s,max} ($^{\circ}$ C) for insulated steel structures as a function of effective fire load density q_f (MJ m⁻²), effective opening factor ($A\sqrt{h}/A_t$)_f ($m^{1/2}$) and the design parameter $A_i\lambda_i/(V_sd_i)$ (W m⁻³ h⁻¹ oC⁻¹) [6]

$$(A\sqrt{h}/A_t)_f = 0.01 \text{ m}^{1/2}$$

$\mathfrak{q}_{\mathbf{f}}$	$A_i \lambda_i$	$/(V_{ m s}/c$	$l_i)$										
	50	100	200	400	600	1000	1500	2000	3000	4000	6000	8000	10000
13	30	40	50	70	90	115	140	160	190	210	235	260	280
19	35	45	65	95	115	150	180	205	245	265	295	320	340
25	40	55	80	115	145	180	220	245	285	305	335	360	375
50	60	90	135	190	225	280	325	350	390	410	430	440	450
75	80	125	180	250	295	355	400	430	455	470	480	490	490
100	100	155	225	310	365	430	470	490	510	520	530	530	535
125	115	185	270	370	425	485	520	535	550	555	560	560	565

$$(A\sqrt{h}/A_t)_f = 0.02 m^{1/2}$$

q f	$A_i \lambda_i$	/(V _s d	l _i)										
1	50	100	200	400	600	1000	1500	2000	3000	4000	6000	8000	10000
13	25	30	40	60	70	90	110	130	165	185	215	245	270
25	35	45	65	90	120	155	190	220	270	300	335	375	405
38	40	55	85	125	160	205	250	290	345	380	420	460	485
50	45	70	105	155	195	250	305	345	400	435	480	515	535
100	75	115	175	250	305	385	450	490	550	580	610	630	635
150	100	155	235	330	405	490	555	595	640	660	680	690	695
200	125	195	290	415	495	585	645	680	710	725	735	740	745
250	145	235	355	490	570	655	705	730	755	765	775	780	780

$$(A\sqrt{h}/A_t)_f = 0.04 \text{ m}^{1/2}$$

q_{f}	$A_i \lambda_i$	/(V _s d	$ \mathbf{l_i}\rangle$										
·	50	100	200	400	600	1000	1500	2000	3000	4000	6000	8000	10000
25	25	35	50	70	85	115	140	170	210	245	290	330	365
50	35	50	75	115	150	200	245	290	350	395	450	505	540
75	45	65	100	155	200	260	325	380	450 -	500	565	615	650
100	50	80	125	190	245	320	395	450	525	575	640	685	715
200	85	135	210	310	385	490	575	635	710	755	800	825	835
300	115	180	275	410	500	615	700	755	815	845	875	890	895
400	140	225	345	505	605	720	800	845	890				
500	170	270	415	585	685	790	860	895					

 $(A\sqrt{h}/A_t)_f = 0.06 \text{ m}^{1/2}$

qf	$A_i \lambda_i$	$/(V_s)d$	l _i }										
~	50	100	200	400	600							8000	10000
38	30	35	50	75	95	125	160	190	240	280	330	380	420
75	35	50	80	125	165	220	275	325	395	450	515	580	625
113	45	70	110	170	220	290	365	425	510	570	645	705	740
150	55	85	135	210	270	355	440	500	590	655	730	780	810
300	90	140	225	335	420	540	635	705	790	840	890		
450	120	190	295	440	540	670	765	825	895				
600	150	240	370	545	650	780	865						
750	175	285	445	625	730	850							

 $(A\sqrt{h}/A_t)_f = 0.08 \text{ m}^{1/2}$

q	$A_i \lambda_i$	$/(V_s d$	$l_i^{})$										
	50	100	200	400	600	1000	1500	2000	3000	4000	6000	8000	10000
50	30	35	55	80	100	135	170	205	260	300	355	410	455
100	35	55	85	130	170	235	295	350	425	485	560	625	675
150	45	70	115	180	230	310	390	455	545	610	695	755	800
200	55	85	140	220	280	380	470	535	635	700	780	835	870
400	90	145	230	350	440	565	670	745	835	890			
600	120	195	305	460	565	705	805	865					
800	150	245	380	565	675	810							
1000	180	295	455	650	760								

 $(A\sqrt{h}/A_t)_f = 0.12 m^{1/2}$

	50	100	200	400	600	1000	1500	2000	3000	4000	6000	8000	10000
	- 0.0			~ ~									
75	30	40	55	85	105	140	180	220	280	330	390	450	495
150	40	55	90	140	185	250	320	375	465	525	615	685	740
225	45	75	120	190	245	330	420	490	590	660	755	820	870
300	55	90	145	230	300	405	500	575	680	755	840		
600	95	150	240	365	465	600	710	790	890				
900	125	200	315	480	595	735	845						
200	155	250	395	585	705	845							
500	185	305	470	670	785								

 $(A\sqrt{h}/A_t)_f = 0.30 \text{ m}^{1/2}$

q f	$\underline{A_i}\lambda_i$	$/(V_s)$	$l_i)$										
	50	100	200	400	600	1000	1500	2000	3000	4000	6000	8000	10000
188	30	40	60	90	115	155	205	245	320	375	445	515	570
375	40	60	95	150	200	275	355	420	515	590	695	770	835
563	50	75	125	200	265	365	460	540	655	735	845		
750	60	95	155	250	320	440	550	630	750	830			
1500	95	155	250	390	495	640	765	850					
2250	130	210	330	510	630	785	900						
3000	160	260	415	615	740	890							
3750	190	315	490	700	820								

Table A6. Thermal conductivity λ_i (kcal·m $^{-1}$ oC $^{-1}$ h $^{-1}$) {Wm $^{-1}$ oC $^{-1}$ } of some insulation materials as a function of the insulation tempeture [4]

	Tempe	rature	°C								
	0	100	200	300	400	500	600	700	800	900	1000
Sprayed mineral wool Cafco Blaze-Shield Type DC/F	0,045 {0,053}	0,047 {0,055}	0,050 {0,058}	0,058 {0,068}	0,066 {0,077}	0,077 {0,090}	0,095 {0,110}	0,120 {0,140}	0,145 {0,170}	0,170 {0,198}	0,210 {0,245}
Sprayed mineral wool Type Pyroguard 101	0,044 {0,051}	0,055 {0,064}	0,059 {0,069}	0,066 {0,077}	0,071 {0,083}	0,079 {0,092}	0,089 {0,104}	0,103 {0,120}	0,123 {0,144}	0,150 {0,175}	0,190 {0,220}
Fire retardant plaster Type Jimoterm	0,203 {0,236}	0,145 {0,169}	0,144 {0,168}	0,143 {0,167}	0,141 {0,165}	0,138 {0,161}	0,138 {0,161}	0.156 {0.182}	0,182 {0,212}	0,186 {0,217}	
Fire retardant plaster Tyne Pyrodur	0,085 {0,099}	0,090 {0,105}	0,095 {0,110}	0,100 {0,116}	0,105 {0,122}	0,130 {0,128}	0,115 {0,134}	0,115 {0,134}	0,120 {0,140}	0,125 {0,146}	0,130 {0,152}
Slabs of vermiculite based material Type Vermit fire insulation slab	0,077 {0,090}	0,085 {0,099}	0,092 {0,108}	0,100 {0,116}	0,112 {0,130}	0,117 {0,137}	0,125 {0,146}	0,133 {0,155}	Q.145 {Q.169}	Q.157 {Q.183}	0,171 {0,199}
Mineral wool slabs with a density of γ≈150 kg/m ³ Type Minwool slab 3060 or Rockwool slab 337	0,030 {0,035}	0,044 {0,051}	0,058 {0,068}	0,081 {0,094}	0,109 {0,127}	0,149 {0,173}	0,187 {0,218}	0,235 {0,275}	0,280 {0,325}	0,365 {0,425}	0,470 {0,550}
Gypsum plaster slabs Type Gyproc	0,180 {0,210}	0,180 {0,210}	0,120 {0,140}	0,135 {0,157}	0,155 {0,181}	0,170 {0,198}	0,190 {0,220}	0,205 (0,240)	0,225 {0,260}	0,250 {0,290}	0,275 {0,320}
Prefabricated gypsum plaster sections Type GPG	0,250 {0,290}	0,130 {0,152}	0,124 {0,145}	0,133 {0,155}	0,135 {0,157}	0,130 {0,152}				-	
Prefabricated gypsum plaster sections Type Perlitgips	0,180 {0,210}	0,105 {0,122}	0,084 {0,098}	0,106 {0,123}	0,115 {0,134}	0,122 {0,142}			_		•

Fire retardant paints

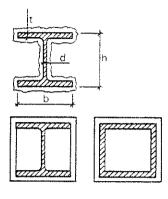
Most fire retardant paints change in thickness on exposure to fire. Information relating only to the variation of the thermal conductivity with temperature does not therefore provide a sufficient basis for design. The insulation capacity of the paint, expressed in terms of a fictive d_i / Δ_i value, must be known. For Unitherm fire retardant paint, the following values can be used in determining the maximum steel temperature. Two-coat Unitherm application, $d_i / \lambda_i = 0.075 \, \text{m}^{2-0} \text{C}$ h/kcal $|0.064 \, \text{m}^{2-0} \text{C/W}|$. Three-coat Unitherm application, $d_i / \lambda_i = 0.10 \, \text{m}^{2-0} \text{C}$ h/kcal $|0.086 \, \text{m}^{2-0} \text{C/W}|$. These values have been determined using the results of standard fire tests. The values are clearly on the safe side and should be applicable also to other types of paint which are found in fire tests to exhibit at least the same fire resistance as Unitherm fire retardant paint.

Table A7. Maximum steel temperature $T_{s,max}$ (O C) for a steel structure insulated with mineral wool slabs, type Minwool 3060 or Rockwool 337 (ρ_i = 150 kg m $^{-3}$), as a function of effective fire load density q (Mcal·m $^{-2}$) {MJ·m $^{-2}$ }, effective opening area A/h/A_t (m $^{1/2}$), structural parameter A_i/V_s (m $^{-1}$), and insulation thickness d_i (mm)

q	$\frac{AVh}{A_t}$	$\frac{A_i}{\overline{V}_s}$		T _{s,m}		9	AVA	A;	+	s,ma		q	AVh	Ąį		s max	***********		ΑVħ	A;		īs,ma	κ.
	Aı	V ₅	<i>d</i> ; 30	<i>d_i</i> 50	<i>d_i</i> 70		A	\overline{V}_s	<i>d</i> ; 30	<i>d_i</i> 50	<i>d_i</i> 70		A	\overline{V}_s	<i>d</i> _i 30	<i>d_i</i> 50	<i>ö;</i> 70	q	At	\overline{V}_s	<i>d_i</i> 30	<i>d_i</i> 60	<i>d;</i> 70
	0,01	200 300 400	325 350 415	250 300 335	200 245 275			100 125 150	370 415 455	275 310 345	215 245 270			50 75 100	400 500 565	285 375 440	220 295 350			50 75 100	415 540 620	295 390 465	220 300 365
20 [84]	0,02	200 300 400 300	295 355 400 300	215 265 300 205	165 210 240 150		0,02	200 300 400 100	515 585 625 300	400 475 525 205	320 390 435		0,02	125 150 200 300	640 640 690 735	530 595 660	400 440 505 580			125 150 200	680 725 785	530 580 650	420 465 540
	0,04 0,06	400 400 125	350 320 330	250 260 250	180 135 200		0,04	125 150 200	340 380 450	240 270 320	180 205 240			400 75 100	760 355 425	695 250 305	625 190 230			300 400 50 75	320 425	745 800 220 295	635 690 165 220
	0,01	150 200 300 400	355 395 450 480	270 315 970 465	225 260 310 340	40 {169}		300 400 125 150	535 600 295 330	400 450 195 220	300 350 140 165		0,04	125 150 200 300	485 525 600 690	350 390 450 550	279 300 350 430		0,06	100 125 150 200	510 570 625 710	360 410 460 530	270 315 355 420
25	0,02	150 200 300 400	300 350 415 465	225 260 315 355	175 205 250 285			200 300 400 200	400 495 550 356	265 340 395 225	. 200 240 285 155	60		400 75 100 125	740 300 360 415	200 250 285	455 150 185 215	90		300 400 75	- 375	635 700 250	510 570 190
[105]	0,04	200 300 400	300 375 430	210 265 310	150 195 225		0,08	300 400 75	440 500 365	280 340 265	200 230 205	[250]	0,06	150 200 300	465 540 650	325 385 475	240 285 360	[380]	Q, QB	100 125 150 200	450 515 570 650	310 365 400 480	230 270 300 360
	0,06	300 400 75 100	330 390 310 355	210 250 230 270	150 170 175 215		0,02	100 125 150 206	480 520 580	315 360 400 460	250 290 320 370			100 125 150	710 320 370 415	540 215 250 265	150 180 200			300 400 100 125	765 - 325 375	585 655 230 275	450 515 175 200
	0,01	125 150 200 300	396 420 466 500	305 335 375 425	245 270 315 365			300 400 100 125	645 680 325 375	540 590 230 265	450 500 175 200		0,08	200 300 400 200	500 605 680 350	340 435 500 230	250 305 350 175		0,12	150 200 300	425 500 615	305 365 475	230 275 350
		400 125 150	520 320 355	460 235 260	405 185 205	45	0,04	150 200 300	415 485 580	300 350 435	225 270 335		0,12	300 400 50	445 505 340	295 350 240	225 265 186		0,30	400 300 400 25	695 290 340 355	540 205 245 240	405 160 190
30 {126}	0,02	200 300 400 150	405 480 530 300	305 370 420 216	335 155	[190]	0,06	400 125 150 200	325 365 435	495 220 250 300	385 160 185 220		0,04	75 100 125 150	450 525 580 620	315 385 435 490	245 295 340 375		0,04	50 75 100 125	560 680 750	410 525 610 670	315 426 495 560
	0,04	200 300 400 200	350 440 500 305	250 315 365 200	485 235 270 140			300 400 150 200	535 600 320 385	375 430 210 250	275 320 150 175			200 300 400 75	695 780 - 360	555 650 700 250	440 525 580 185			150 200 300 400	-	715 785 	610 685 765
	0,06	300 400 300 400	395 450 330 390	250 300 210 250	180 210 150 175		-, 00	300 400 300 400	480 550 325 375	315 375 230 270	225 260 175 200	75 {315}	0,06	100 125 150 200	500 550 630	300 350 390 460	225 260 295 350	120		25 50 75	260 430 565	175 300 400	130 225 305
		100 125 150 200	325 365 405 455	240 270 300 350	190 215 240 280			50 75 100 125	320 410 475 530	225 300 355 400	175 235 280 320			300 400 75 100	730 795 320 395	560 630 215 265	495 495 155 190	{500}	0,06	150 200	650 725 775	485 545 600 675	370 425 480 560
		300 400 125	535 575 300	420 470 215	340 385 155		0,02	150 200 300 400	565 620 680	445 500 580	360 415 490		0,08	125 150 200	450 500 580	305 350 410 520	225 250 300 380			300 50 75 100	360 470 565	775 245 325 400	185 250 300
35 [147]	0,04	150 200 300 400	340 400 490 550	240 290 355 410	180 215 270 310			75 100 125	710 300 355 410	210 255 300	545 160 190 225			300 400 125 150	700 770 305 340	580 220 250	440 160 190		0,08	125 150 200 300	635 690 770 -	460 510 595 705	350 395 465 570
	0,06	150 200 300 400	300 350 450 500	190 235 300 350	145 165 210 250	50 [210]	.,.,	150 200 300 400	455 525 620 680	330 390 475 535	250 300 365 420		0,12	200 300 400 400	430 535 610 290	300 .395 450 210	220 280 325 150			400 75 100 125	350 425 485	775 250 310 360	635 190 235 270
		200 300 400	300 385 450	200 250 300	135 175 200		0,00		310 360 400 475	210 240 275 325	155 175 205 240	 			*****				0,12	150	540 620 740	405 480 590 660	305 365 460 520
								300 400 125	575 640 310 355	410 475 210 235	300 350 150 170								0,30	200 300 400	330 420 490	230 300 355	15 (235 275
							0,08	200 300 400	425 530 600	285 355 420	200 260 300						ı			1		•	
							0,12	200 300 400	295 365 425	200 255 300	150 200 230												

Table A8. A_i/V_s for different types of fire exposed, insulated steel structures

Column in a fire compartment



$$\frac{A_{i}}{V_{g}} = \frac{2h + 4b - 2d}{\text{steel cross section area}}$$

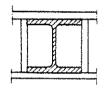
 $\frac{A}{V} = \frac{2h + 2b}{\text{steel cross section area}}$

Column against a wall with a sufficient fire resistance



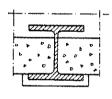
$$\frac{A_{.}}{V_{s}} = \frac{2h + b}{\text{steel cross section area}}$$

Column within a wall with a sufficient fire resistance



$$\frac{A_{i}}{V_{c}} = \frac{b}{bt} = \frac{1}{t}$$

Floor structure, composed of steel beams with a concrete slab, supported on the lower flange of the beams



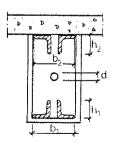
$$\frac{A_{i}}{V_{s}} = \frac{b}{bt} = \frac{1}{t}$$

Beams with a floor slab, supported on the upper flange of the beams



$$\frac{A_{i}}{V_{s}} = \frac{2h + b}{\text{steel cross section area}}$$

Floor slab beams of truss type (A₁/V_s is determined for each part of the truss)



$$\frac{\frac{A}{1}}{V_{S}} \text{ (lower flange)} = \frac{2b_{1} + 2h_{1}}{\text{cross section area}}$$
of lower flange

$$\frac{A_{i}}{V_{s}} \text{ (upper flange)} = \frac{b_{2} + 2h_{2}}{\text{cross section area}}$$
of upper flange

$$\frac{A}{V_{c}}$$
 (diagonal) = $\frac{4}{d}$

Table A9. Maximum steel beam temperature $T_{s,max}$ (o C) for a steel beam construction according to Fig. 20, with an insulation in the form of a suspended ceiling, as a function of effective fire load density q (Mcal·m-2) {MJ·m-2}, effective opening factor $A\sqrt{h}/A_{t}$ ($m^{1/2}$), structural parameter F_{s}/V_{s} (m^{-1}), and insulation parameter d_{j}/λ_{j} ($m^{2.0}$ C·h·kcal-1)°. The maximum temperature in the suspended ceiling is given in brackets [4]

q	AVII AL	F, V,	Maximum steel temperature $\tau_{s \text{ max}}$ and () maximum suspended celling temperature (σ_i/λ_i) fict		q	AVA At	$\frac{F_s}{\overline{V}_s}$	Maximum steel temperature $r_{s,max}$ and () maximum suspended ceiling temperature $(d_i/\lambda_i)\gamma_{1 ct}$				
			0,05 0,10		0,30	1			0,05	0,10	0,20	0,30
15 {63}	0,02	50 100 200 300	130 90 180 130 230 (470) 170 260 190	65 (440) 90 115 (410	50 70 90 (390)	60 [250]	0,02	50 100 200 300	425 450 455 455	315 340 350 (570) 350	200 240 250 (530) 250	160 185 200 (500) 200
	0,04	50 100 200 300	100 70 150 (565) 100 200 (565) 140 240 170	45 (530) 65 90 110	40		0,04	50 100 200 300	340 400 435 445	225 285 320 (630) 330	145 185 220 (590) 230	110 140 165 (560) 180
	0,08	50 100 200 300	190 125	35 50 65 (590 90	60		Ç, 08	50 100 200 300	250 340 415 445	160 225 285 (700) 315	100 130 185 (650) 210	155
	0,12	50 100 200 300	40 35 60 (735) 45 120 (735) 70 155 100 200 140	(690) 30 (650 40 (650 50 60	25 30 (620) 40 45 75		0,12	50 100 200 300	190 (780) 285 375 420	120 (725) 185 (725) 250 290	75 (580) 110 (580) 155 185	80 (GGO) 110 130
	0,02	100 200 300	260 (510) 185 300 (510) 225 320 245	(470) 125 155 (435 170	100 (420) 120 (420)	90	0,04	100 200 300	510 515 (740) 515	370 385 (680) 385	250 270 (630) 270	190 210 (600) 215
25	0,04	50 100 200 200	325 235	75 100 (565) 135 155	115	(380)	0,08	50 100 200 300	345 430 480 (790) 495	225 290 340 (730) 360	130 180 225 (675) 250	100 130 170 (G50) 190
[105]	0,08	50 100 200 300	115 75 160 (680) 110 240 (680) 160 285 195	50 70 (635) 100 (595 - 120	40 55 75 (570) 90	120	0,04	50 100 200 300	560 570 575 (780) 575	400 420 425 (715) 425	260 290 300 (660) 300	230
	0,12	50 100 200 300	235 160	40 (690) 60 80 (650 100	75	[50 c]	0,08	50 100 200 30 0	425 495 520 (810) 525	280 345 375 385	160 210 250 (695) 260	120 160 195 (670) 205
	0,02	50 100 200 300	385 295	145 175 (520) 200 (480 210	165							
108}		50 100 200 300	390 200	105 140 (600) 180 (560 195	150							
	0.08	30 100 200 300	170 110 243 335 (715) 160 220 380 260	70 100 (665) 140 165	55 75 105 (600) 120			•				
	0,12	50 100 200 300	130 85 200 (750) 130 290 (750) 190 (340 225	55 85 (700) 115 143	45 60 (630) 85 (100			- { (0,05 m² °C 0,10	zitz	0,043 m³ 0,086 0,172 0,258	°C/W » » »

Table AlO. Summary results of standard fire resistance tests on some types of suspended ceilings and connected values, derived from the test results, for $(d_i/\lambda_i)_{eff}$ and critical temperature of the ceilings [4]

No	Make	A	Resistance time in standard fire test (min)	Remarks	Estimate $\frac{(d_i/\lambda_i)_{fl}}{(\frac{m^2}{\text{cch}})}$		Estimated critical suspended ceiling temperature(^O C)
1 2	Gyproc	2x13 mm gypsum plaster slabs no glass fibre reinforcement 1x13 mm gypsum plaster slabs	30-4ú	All tests were discontinued because the suspended celling fell down. The critical temperature had not been	0,075	0, 064	625
3		0.25% g f r 1x16 mm gypsum plaster slabs	48	reached in the steel girders	0.075	0,064	650
4		0, 25% g i r 2x13 mm gypsum plaster slabs	49		0,10	0.086	650
5		0.25% g f r 3x13mm gypsum plaster slabs	60		0.15	0,129	650
6		0.25% g f r 2x20 mm gypsum plaster slabs	75-80		0,25	0,215	625
7	WST	0.25% g f r 2x13 mm gypsum plaster slabs with 13 mm mineral wool	80	All tests were discontinued for the same reason as above. The gypsum	0,30	0,258	625
6	-	between them 2x13 mm gypsum plaster slabs with 13 mm mineral wool	45	plaster slabs were not reinforced	0,30	0,258	550
9		between them 2x13 mm gypsum plaster slabs	50		0,30	0,258	550
10		with 43 mm straw between them 2x13mm gypsum plaster slabs	47		0,30	0,258	550
		with 43 mm straw between them	54		0,30	0,258	550
11	Ingenjörs- firma Zero	Soundex special suspended ceiling tiles. Cast glass fibre reinforced gypsum plaster files with "ridges" in a grid pattern. The thickness 18 mm, at the ridges 38 mm		Parts of the celling fell down after 90 minutes. Max, steel temperature approx. 440°C	0,15	0,129	700
12	Consentus	Armstrong 13 mm thick	30	No visible damage to suspended celling. Max steel temperature	0, 05	0.043	550
13		Mineral wool acoustic 16 mm thick	80	about 450 °C	0,075	0,064	>(725) ²
i-i		Type minaboard 13 mm thick	85		0,075	0.064	>(725) ^a >(675) ^a
15		Deflamit-Asbestolux k (9 mm Deflamit + 15 mm mineral wool ÷ 8 mm eternit)	50	No visible damage to suspended ceiling. Max steel temperature about 300 °C	0,20	0,172	·
16		Celotex Acoustiformat 15 mm thick glass fibre slab	90	No visible damage to suspended ceiling. Max steel temperature	0,10	0,086	(725) ^a
17	Rockwoo!	Rockion Decor 85i (15 mm thick mineral wool slab)	GC	about 450 °C. The test was dis- continued because the suspended celling fell down. The critical temperature had not been reached in the steel girders.	0,20	0,172	600

a No damage to the suspended ceiling. Calculated temperature in the suspended ceiling when the test was discontinued.

Table All. Load values to be applied in a differentiated, analytical, structural fire engineering design [2], [4], [6].

It is to be proved that the load-bearing structure or structural member does not collapse during the complete process of fire development for the most unfavourable combination of dead load, live load, snow load and wind load. On the assumption that the design fire load density is chosen according to Table Al, the following load values are to be applied. The values include a safety factor which roughly takes into account the probability of a fully developed fire and the probability of the presence of the maximum load at the fire occasion.

(a) Complete evacuation of occupants not certainly anticipated Following values shall be applied for the live load.

Type of fire compartment	Permanent loading kN.m ⁻²	Movable loading kN.m ⁻²	
Dwellings, hotels and hospitals	0.5	1.0	
Offices	0.5	1.5	
Schools (lecturing rooms)	0.5	1.5	
Schools (corridors)	0.5	2.5	
Assembly-rooms	1.0	2.0	
Libraries	1.0	2.0	

For the snow load, permanent and movable loading values shall be in accordance to the general loading regulations.

For the wind load, values shall be applied which correspond to a velocity pressure = 50% of the velocity pressure specified in the general loading regulations.

(b) Complete evacuation of occupants certainly anticipated Following values shall be applied for the live load. Snow and wind load according to (a).

Type of fire compartment	Permanent loading kN.m-2	Movable loading kN.m ⁻²
Dwellings, hotels and hospitals	0.5	0.5
Offices	0.5	0.8
Schools (lecturing rooms)	0.5	0.8
Schools (corridors)	0.5	0.8
Assembly-rooms	1.0	0.8
Libraries	1.0	2.0

Due consideration shall be taken to the local increase of the live load in connection with an evacuation of the building or a removal of people to a safe place of refuge within the building.