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*Published in:*

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2019

*Document Version:*

Peer reviewed version (aka post-print)

[Link to publication](#)

*Citation for published version (APA):*

Wiggermann, V., Vavasour, I. M., Hernandez-Torres, E., Helms, G., MacKay, A. L., & Rauscher, A. (2019). Non-negative least squares fitting of multi-exponential T2 decay data: Are we able to accurately measure the fraction of myelin water? In *Non-negative least squares fitting of multi-exponential T2 decay data: Are we able to accurately measure the fraction of myelin water?* (Vol. 27). Article 4402 (Proc Intl Soc Magn Reson Med; Vol. 27). International Society for Magnetic Resonance in Medicine.  
<http://indexsmart.mirasmart.com/ISMRM2019/PDFfiles/4402.html>

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6

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LUND UNIVERSITY

PO Box 117  
221 00 Lund  
+46 46-222 00 00

# Non-negative least squares fitting of multi-exponential T2 decay data: Are we able to accurately measure the fraction of myelin water?

Vanessa Wiggermann<sup>1,2,3</sup>, Irene M Vavasour<sup>3,4</sup>, Enedino Hernandez-Torres<sup>2,3</sup>, Gunther Helms<sup>5</sup>, Alexander L MacKay<sup>1,3,4</sup>, and Alexander Rauscher<sup>1,2,3,4</sup>

<sup>1</sup>Physics and Astronomy, University of British Columbia, Vancouver, BC, Canada, <sup>2</sup>Pediatrics, University of British Columbia, Vancouver, BC, Canada, <sup>3</sup>UBC MRI Research Centre, University of British Columbia, Vancouver, BC, Canada, <sup>4</sup>Radiology, University of British Columbia, Vancouver, BC, Canada, <sup>5</sup>Lund University, Lund, Sweden

## Synopsis

The ability to determine the myelin water fraction (MWF) *in vivo* is essential to assessments of neurodevelopmental myelination and myelin damage in neurodegenerative diseases. The analysis of multi-exponential T2 decay data relies on the non-negative-least-squares (NNLS) fitting, which may be sensitive to the chosen fitting parameters. We performed simulations to explore the outcomes of NNLS under different parameter selection. The lowest allowed T2 was found to have the largest effect on correctly estimating the T2 of different water pools as well as the MWF. Lower refocusing FAs led to further underestimation of the MWF.

## Introduction

The ability to determine the myelin water fraction (MWF) *in vivo*<sup>1</sup> is essential to assessments of neurodevelopmental myelination and myelin damage in neurodegenerative diseases. Multi-echo spin-echo imaging has been shown to correlate with optical density measurements of myelin lipids<sup>2,3</sup>. However, as MW imaging has been extended to 48-echoes, applied at higher magnetic fields<sup>3</sup> and investigated post-mortem during fixation<sup>4</sup>, selection of post-processing parameters for the non-negative least squares fitting (NNLS) needs to be revisited. We used simulations to explore the outcomes of NNLS fitting for different parameter selections in a given water environment at 3T and drew parallels to *in vivo* data.

## Methods

Independent decay data were computed by multi-echo spin-echo simulations of the magnetization of 256x256 spins in with given T<sub>1</sub> and T<sub>2</sub>-properties, taken from literature to mimic white matter values<sup>5,6</sup>. Various resonance frequencies were assigned to the different water compartments<sup>7</sup>, after computing the local magnetic environment from tissue magnetic susceptibilities. All T<sub>1</sub>'s, T<sub>2</sub>'s and resonance frequencies were assigned to each spin by random sampling from a Gaussian distribution. Finally, Gaussian noise was added to the images. The voxel and its properties are shown in **Figure 1**. The MWF, i.e. the amount of MW relative to all water within a voxel, was 21%. Decay data were computed assuming a signal-to-noise ratio of 300, imperfect refocusing flip angles (FA=30,150,170,180°) and MWT<sub>2</sub>-times (5,10,15,20 ms) using a 32-echo sequence with TE/ΔTE/TR=10/10/1000ms. Decay curves were analyzed by fitting the measured decay curve with decay curves estimated by the extended-phase-graph algorithm to estimate FA in the presence of stimulated echoes<sup>8,9</sup>, while minimizing χ<sup>2</sup> with respect to FA. Regularized NNLS was employed with varying numbers of T<sub>2</sub>-components (nT<sub>2</sub>) to fit the decay curves. The estimated parameters, i.e. the FA, the geometric mean T<sub>2</sub> of the intra/extracellular water (GMT<sub>2</sub> IEW), GMT<sub>2</sub> of the MW and the MWF were computed under varying nT<sub>2</sub>s (20,32,40,80,120) and different T<sub>2</sub>-ranges for which the shortest T<sub>2</sub> was varied (T<sub>2,1</sub>=5-15ms, T<sub>2,end</sub>=2s).

## Results

The FA estimation was independent of nT<sub>2</sub>. The computed FAs differed from the true FAs by 2.46±1.49, 3.00±0.51, 1.99±0.58 and 2.36±0.51 for 130,150,170,180°, respectively. **Figure 2** shows the estimated GMT<sub>2</sub> IEW values. As FA decreased, the GMT<sub>2</sub> IEW moved further away from the reference: 69.70±0.71ms (180°), 69.74±0.62ms (170°), 68.85±1.08ms (150°), 67.93±1.38ms (130°). For MWT<sub>2</sub> values, lower refocusing FAs resulted in greater deviations from the true GMT<sub>2</sub> IEW. This was explored in more detail in **Figure 3**, by comparing the computed T<sub>2</sub>-distributions. For all FAs, the GMT<sub>2</sub> of MW and IEW were well determined when T<sub>2,1</sub> was less than T<sub>2</sub> of MW. When T<sub>2</sub> MW was shorter than the first allowed T<sub>2</sub>, the MW peak was incompletely described and the estimated MWT<sub>2</sub> depended on the value of T<sub>2,1</sub>. However, the GMT<sub>2</sub> IEW was accurately estimated. Finally, we compared the estimated MWF, with respect to FA, nT<sub>2</sub>'s and T<sub>2,1</sub> (**Figure 4**). Again, MWFs were well estimated if T<sub>2,1</sub> was less than MWT<sub>2</sub>. Note that once the MW peak was fully captured, further shortening of T<sub>2,1</sub> did not change the MWF. With decreasing FA, the MWF was underestimated. When assessing the impact of changed analysis parameters on *in vivo* data acquired at 3T with the imaging parameters matching the simulation parameters (**Figure 5**), we noted visually an improvement in the assessed MWF when lowering T<sub>2,1</sub> from 14 to 12ms. Both GMT<sub>2</sub> IEW and MWF were in line with the observations of the simulation, with stronger effects observed for single voxels. FAs in the regions-of-interest were 151.7,164.3,154.3° in the internal capsule, white matter and globus pallidus, respectively.

## Discussion

Although the true FAs were well captured by the extended-phase-graph algorithm, MWF may be under-estimated, even when the MWT<sub>2</sub> was within the T<sub>2</sub>-range. The GMT<sub>2</sub> of IEW and MW shortened slightly at lower FAs if T<sub>2,1</sub><MWT<sub>2</sub>, but MWT<sub>2</sub> estimation failed if T<sub>2,1</sub> was chosen too long. FAs at 3T are generally greater than 150, but regions of low FA as well as further T<sub>2</sub>-shortening at higher magnetic field strength, or due to fixation, will be problematic for estimating MWF correctly. *In vivo* data showed good correspondence with the simulations. Single-voxel data were affected by the choice of parameters, but averages within regions containing multiple voxels provided stable estimates.

## Conclusions

The MWF was robustly estimated with respect to many parameters. Successfully measuring the MWF however depends on the actual MWT<sub>2</sub>, which is unknown, and the chosen T<sub>2</sub>-range, relative to the MWT<sub>2</sub>. By lowering the T<sub>2</sub>-range, the MW signal is better captured. Further work should investigate how

underestimations of the MWF at lower, known FAs can be recovered.

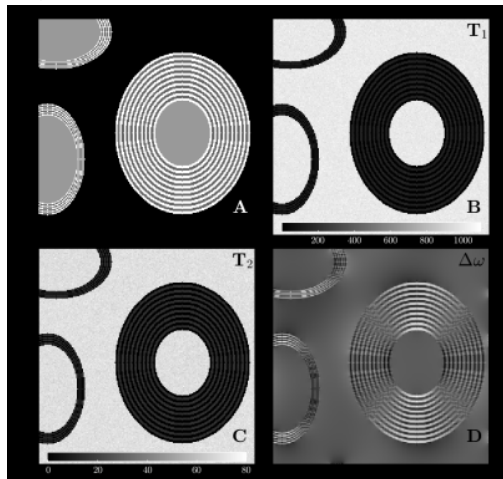
## Acknowledgements

No acknowledgement found.

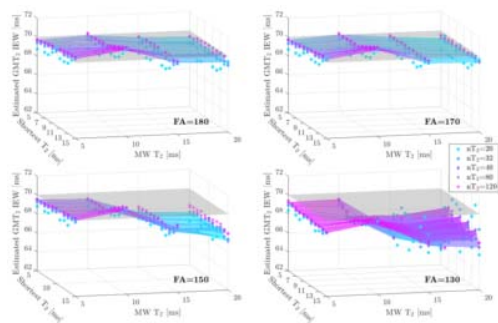
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## Figures

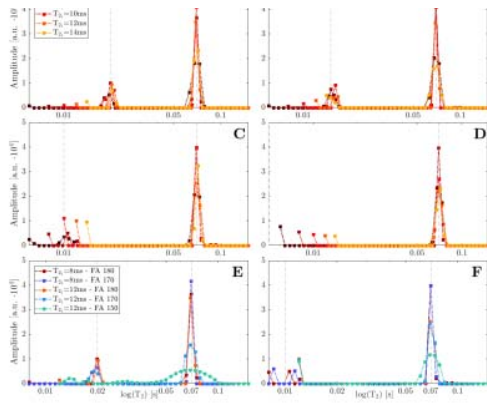


**Figure 1: Assumed 2D-voxel with different compartments of varying, compartment-specific  $T_1$ 's,  $T_2$ 's and resonance frequencies.** (A) shows the model voxel, in which the myelin water fraction, i.e. the fraction of water within the myelin lipid bilayers relative to all water present in the voxel was approximately 21%. (B) and (C) display the respective  $T_1$  and  $T_2$  of the different tissues, all shown in units of [ms]. It was assumed that myelin water has a shorter  $T_1$  and  $T_2$  than other water compartments. (D) The distribution of resonance frequencies across the voxel.

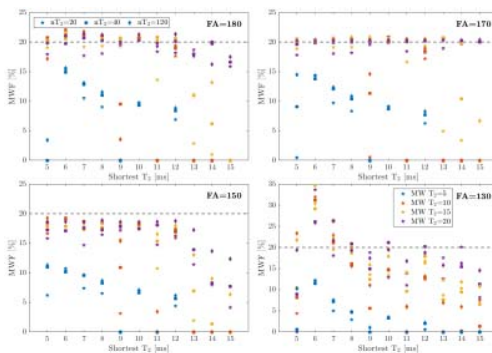


**Figure 2: GMT<sub>2</sub> IEW estimation at different FAs,  $nT_2$ s,  $T_2$ -ranges and MW  $T_2$ s.** The gray plane represents the true  $T_2$  value of 70ms. The coloured plane corresponds to the FA estimation using 40  $nT_2$  values, which is the standard used in in vivo analyses. GMT<sub>2</sub> for IEW was well estimated, particularly at higher refocusing FAs. At lower FAs, voxels with longer MW  $T_2$  times showed more deviation from the reference. However, variations were small, with FA=130 still estimating GMT<sub>2</sub> of IEW 2ms lower than the true value.

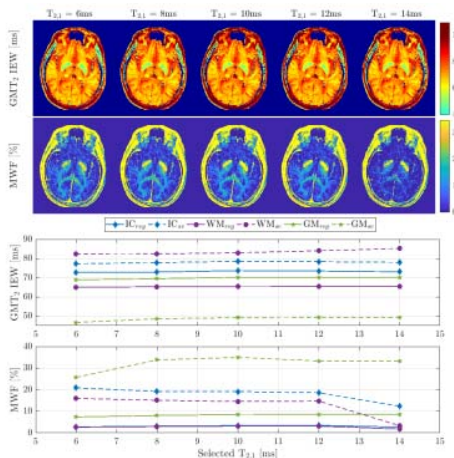




**Figure 3:** (A-D)  $T_2$ -distributions obtained from different  $T_2$ -ranges for varying MWT<sub>2</sub> at optimal refocusing (FA=180) and  $nT_2=80$ . The vertical broken lines indicate the true MW and IEW  $T_2$ . The MWT<sub>2</sub> was reduced from A to D, corresponding to 20ms,15ms,10ms,5ms. The MWF peak was incompletely displayed when the MWT<sub>2</sub> is lower than allowed by the  $T_2$ -range. In this case, all signal attributed of MWT<sub>2</sub>-component is assigned to  $T_{2,1}$ , thus inaccurately representing the MWT<sub>2</sub>. Despite small variations, the IEWT<sub>2</sub> is reliably determined independent of the  $T_2$ -range. (E-F) display how lower FAs change the distribution, but preserve the GMT<sub>2</sub> values of the water pools if  $T_{2,1} > MWT_2$ .



**Figure 4:** MWF estimation with respect to the FA,  $nT_2$ ,  $T_2$  range and MWT<sub>2</sub>. Values related to different  $nT_2$ s are shown with different symbols and MWF values related to different MWT<sub>2</sub>'s are distinguished using different colors. For instance, MWF values assuming a MWT<sub>2</sub> of 5ms (blue) are consistently underestimated even at FA=180, because the  $T_2$ -range did not account for values <5ms. In contrast, MWFs of voxels with MWT<sub>2</sub> of 10ms are well captured, if  $T_{2,1}$  is  $\leq 10$ ms or just above (12ms). As the FAs reduce, the MWF is underestimated.



**Figure 5:** Impact of the selection of different  $T_2$ -ranges for *in vivo* data analysis. The resulting GMT<sub>2</sub> IEW maps and MWF maps are shown in the upper two rows, and the bottom rows display the average GMT<sub>2</sub> IEW and MWF within small regions ('\_reg') of the internal capsule (IC), white matter (WM) and globus pallidus (GM) as well as single voxel ('\_sv') data. Visually, the MWF improved when lowering  $T_{2,1}$  from 14 to 12ms. This was reflected in the single voxel measurements, which showed an increase in MWF when lowering  $T_{2,1}$ . Averages over region-of-interests, however, were much less affected.