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Published in:

Physical Review A (Atomic, Molecular and Optical Physics)

DOI:

10.1103/PhysRevA.82.033410

2010

Link to publication

Citation for published version (APA):

He, X., Dahlström, M., Rakowski, R., Heyl, C. M., Persson, A., Mauritsson, J., & L'Huillier, A. (2010). Interference effects in two-color high-order harmonic generation. *Physical Review A (Atomic, Molecular and Optical Physics)*, 82(3). https://doi.org/10.1103/PhysRevA.82.033410

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Interference effects in two-color high-order harmonic generation

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We study high-order harmonic generation in argon driven by an intense 800 nm laser field and a small fraction of its second harmonic. The intensity and divergence of the emitted even and odd harmonics are strongly modulated as a function of the relative delay between the two fields. We provide a detailed analysis of the underlying interference effects. The interference changes drastically when approaching the cutoff region due to a switch of the dominant trajectory responsible for harmonic generation.

PACS numbers: 32.80.Rm, 32.80.Qk, 42.65.Ky

High-order harmonic generation (HHG) from the interaction of an intense infrared (IR) laser field and a gas target provides a coherent table-top radiation source in the extreme ultraviolet (XUV) range, of interest for a number of applications, in particular the production of attosecond light pulses [1, 2]. The underlying physics of HHG is well described by the so-called three-step model [3–5]. An electron wave packet is created by tunneling through the Coulomb barrier deformed by the laser field. It is subsequently accelerated by the laser field, returns to the atom and recombines to the ground state, leading to the production of an XUV light burst. This process is repeated every half-cycle of the IR laser field, resulting in an attosecond pulse train (APT) with a pulse separation of one half IR period and to a spectrum of odd harmonics.

There is a growing interest to achieve even better control of the generation process [6], e.g. to obtain higher conversion efficiency or to tailor attosecond pulses or pulse trains for specific applications. Two-color HHG driven by an IR laser and its second harmonic (blue) provides subcycle control of the generating electric field, with the interesting property that two consecutive halfcycles become different, and not simply opposite in sign. This breakdown of the electric field inversion symmetry has been used for several applications e.g. the generation of even and odd high-harmonics with increased conversion efficiency [7, 8] and the production of attosecond pulse trains with one pulse per IR cycle [9, 10]. In some conditions, when the intensity of the second harmonic is much weaker than that of the fundamental laser field, even harmonics can be used to provide information about the generation process [11–13].

In this letter, we investigate both experimentally and theoretically high-order harmonic generation driven by a two-color laser field consisting of a a 800 nm fundamental and a fraction of its second harmonic. The even and odd harmonic intensities are found to be modulated as a function of IR-blue delay, forming in some cases a rich interference pattern (Fig. 1). We investigate how these oscillations depend on harmonic energy and intensity of the blue field and how the spatial profiles of the emit-

ted harmonics are affected. We provide an interpretation based on quasiclassical calculations.

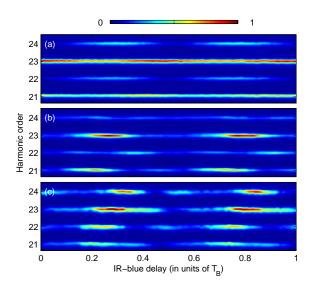


FIG. 1: $21^{\rm st}$ to $24^{\rm th}$ harmonic spectra as a function of the relative delay between the IR and blue fields for different intensity ratios, increasing from about half a percent in (a) to a few percent in (b) and (c). The IR intensity is estimated to be 1.8×10^{14} W/cm², based on the cutoff position. The color code indicates the harmonic intensities in arbitrary units.

Experiments were performed using an amplified $10\,\mathrm{Hz}$ titanium sapphire laser system delivering $40\,\mathrm{fs}$ pulses at $800\,\mathrm{nm}$ with energy up to $1\,\mathrm{J}$. The results presented in this article are obtained with only a small fraction (less than $10\,\mathrm{mJ}$) of this energy. The laser beam was sent through a $1.3\,\mathrm{mm}$ -thick type I KDP (Potassium Dihydrogen Phosphate) crystal to generate the second harmonic. A Michelson interferometer was used to separate and delay the second harmonic and to make the polarizations of the two laser fields parallel to each other. The relative delay was adjusted with a $500\,\mu\mathrm{m}$ -thick glass plate. After recombination of the two colors, the beam was focused by a spherical mirror with a $2\,\mathrm{m}$ focal length into a cylindrical gas cell with $1\,\mathrm{mm}$ diameter and $15\,\mathrm{mm}$ length, filled with Ar gas. Variable apertures were placed in the

fundamental and second harmonic beams to adjust intensities and focusing geometries. These conditions are such that phase matching is optimized and energies per harmonic reaching 100 nJ have been measured. The harmonic spectra were detected by a flat-field XUV spectrometer, located 1.5 m from the source and allowing us to obtain spatial and spectral information simultaneously [14].

Fig. 1 (a-c) presents the spectra of the $21^{\rm st}$ to $24^{\rm th}$ harmonics as a function of relative delay in units of the period of the blue field $T_B = 1.3$ fs. The color code indicates the intensity of the emitted light. When the blue intensity is less than a percent of the IR [panel (a)], the odd and even harmonics oscillate with opposite phase twice per blue cycle [11–13]. When the blue intensity is increased to a few percent [Fig. 1 (b)-(c)], even and odd harmonics become comparable in strength and vary more strongly with the IR-blue delay (τ) .

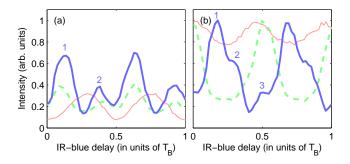


FIG. 2: Intensities of the 22nd (a) and 23rd harmonics (b), normalized to the maximum value of the 23rd harmonic for the three cases in Fig. 1. The thin red line, green dashed line and thick blue line correspond to (a), (b) and (c).

Fig. 2 compares the intensities of the $22^{\rm nd}$ (a) and $23^{\rm rd}$ (b) harmonics as a function of τ for the three different intensities of the blue field used in Fig. 1. At low intensity (thin red line), the odd and even harmonics oscillate out of phase. When the blue intensity is increased, the patterns become more complex, exhibiting multiple maxima per half blue period. The number and position of these maxima depend on the blue intensity, as well as harmonic order. These results arise from the interferometric nature of the HHG process, which will be analyzed in more detail in the following.

To understand the interference structure shown in Figs. 1 and 2, let us consider the radiation emitted every IR cycle over a certain energy range. It comprises predominantly two bursts, one each half-cycle. In absence of the blue field, they are identical except for a change of sign. We further assume that the emitted bursts are identical from one IR cycle to the next. The radiation emitted from the interaction of an intense laser field comprising n periods with an atom can be generally expressed

as

$$s(t) = \sum_{j=1}^{j=n} a_+(t) \otimes \delta(t - jT) + a_-(t) \otimes \delta\left(t - jT - \frac{T}{2}\right), (1)$$

where $a_+(t)$ and $a_-(t)$ are the fields emitted in the first and second half period respectively, and T is the IR field period. If the blue field is weak, it mainly affects the phase of the emitted radiation. $a_\pm(t) \approx \pm a(t) \exp[\pm i\sigma(t)]$, where a(t) is the pulse emitted from the first (positive) half period due to the interaction with the fundamental field only, and $\sigma(t)$ is a slow function over time. The Fourier transform of the pulse train can then be approximated as

$$S(\Omega) \approx A(\Omega) \sum_{i=1}^{j=n} e^{ij\Omega T + i\sigma(\Omega)} - e^{ij\Omega T + i\frac{\Omega T}{2} - i\sigma(\Omega)}, \quad (2)$$

where $A(\Omega)$ is the Fourier transform of a(t) and $\sigma(\Omega) = \sigma[t_r(\Omega)]$. $t_r(\Omega)$ represents the time at which the component at frequency Ω of the light burst is emitted, *i.e.* the return time of the corresponding classical electron trajectory. The Ω dependence accounts for the chirp of the emitted radiation [15]. The power spectrum reduces to the form

$$|S(\Omega)|^2 \approx 4 |A(\Omega)|^2 \left| \frac{\sin(\frac{n\Omega T}{2})}{\sin(\frac{\Omega T}{2})} \right|^2 \left| \sin\left[\frac{\Omega T}{4} - \sigma(\Omega)\right] \right|^2, \quad (3)$$

which has a straightforward interpretation. The first factor is the spectrum emitted by a single attosecond pulse, the second factor modulates this broad spectrum, leading to a comb of even and odd harmonics. Finally the last factor cancels the even harmonic components when there is no second harmonic ($\sigma = 0$). When a second harmonic field is present, it modulates the amplitude of both even and odd harmonics. For the even harmonics ($\Omega = q\omega$ where ω is the IR frequency and q is an even integer), $|S(q\omega)|^2 \propto |\sin[\sigma(q\omega)]|^2$, while for the odd harmonics (q odd), $|S(q\omega)|^2 \propto |\cos[\sigma(q\omega)]|^2$.

The phase change induced by the blue field can be calculated using quasiclassical considerations. By treating the blue field as a perturbation, $\sigma(\Omega)$ is found to be [13],

$$\sigma(\Omega) = \frac{e}{\hbar} \int_{t_r}^{t_r} dt' \ x_R(t_r, t') E_B(t'), \tag{4}$$

where t_i is the ionization time and e the electron charge. x_R denotes the position at time t' of an electron that starts its motion in the IR field $[E_R(t) = E_R^0 \sin(\omega t)]$ at time t_i . Finally, E_B is the second harmonic field $E_B(t) = E_B^0 \sin(2\omega t + \phi_B)$. Eq. (4) can be rewritten as

$$\sigma(\Omega) = \sigma_0 \sin[\phi_B + \delta(\Omega)],\tag{5}$$

with $\sigma_0 = eE_B^0 \Delta(\Omega)/\hbar$. $\Delta(\Omega)$ and $\delta(\Omega)$ are the frequency-dependent modulus and argument of the

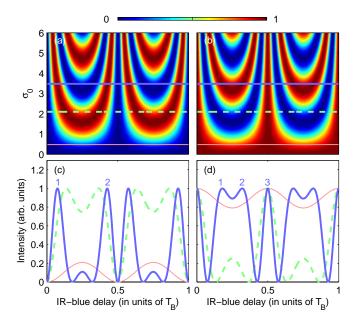


FIG. 3: Harmonic intensity as a function of σ_0 and IR-blue delay for even (a) and odd (b) harmonics. The σ_0 corresponding to the intensities used in Fig. 1 (a-c) are indicated by the thick blue solid (1a), green dashed (1b) and thin red lines (1c). Panels (c) and (d) show the corresponding lineouts.

Fourier transform at 2ω of the electron trajectory in the IR field.

Figure 3(a,b) shows the calculated intensity of two consecutive harmonics (even and odd) as a function of σ_0 and delay, expressed here as $(\phi_B + \delta)/2\pi$, while (c,d) presents lineouts at three different σ_0 , indicated by the corresponding lines in (a) and (b). The odd and even harmonic intensities strongly varies with delay in opposite phase with each other, so that the total intensity remains constant. The number of maxima increases with σ_0 , *i.e.* with the blue field intensity.

When the blue field is weak ($\sigma_0 \ll 1$), the intensity of the even harmonic varies as $|\sin(\phi_B + \delta)|^2$, while the odd harmonic intensity varies as $|\cos(\phi_B + \delta)|^2$ [thin red line in Fig. 3(d)]. At moderate blue intensity, corresponding to the conditions of Fig. 1(b), the even harmonic intensity (green dashed line) show two peaks of equal strength over a delay of $T_B/2$, while the odd harmonics show one strong and one weak peak. This behavior compares well to that observed experimentally in Fig. 2 where two (one) peaks are visible in the even (odd) harmonics. We estimate σ_0 to be just above $\pi/2$ in this case. At higher blue intensity, as in Fig. 1(c), the even harmonic intensity (thick blue line) show two peaks (1,2), while the odd harmonics presents a broad peak with two maxima (1,2)and an additional sharp peak (3). The same qualitative behavior is observed experimentally [blue line in Fig. 2]. σ_0 is thus estimated to be slightly above π . From this analysis, we can estimate the ratios of the blue to IR

intensities to be 0.4, 5 and 20 % in Fig. 1(a), (b), (c). The relative strength of the experimental peaks in Fig. 2 is not accurately modeled using Eq. (3) since we include neither amplitude effects nor propagation in our calculation.

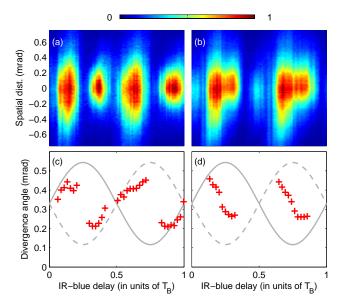


FIG. 4: Spatial profiles for the $22^{\rm nd}$ (a) and $23^{\rm rd}$ (b) harmonics as a function of delay, in the conditions of Fig. 1(c). The experimental divergence angles (red symbols) are compared to the theoretical half-cycle divergences in (c) and (d) for the $22^{\rm nd}$ and $23^{\rm rd}$ harmonics respectively.

Complementary information on the generation process can be obtained by studying the spatial distributions of the $22^{\rm nd}$ and the $23^{\rm rd}$ harmonics [Fig. 4(a,b)]. In the one-color case, the divergence of the $q^{\rm th}$ harmonic Θ_q can be estimated using Gaussian optics by the simple expression [14],

$$\Theta_q = \frac{\lambda_q}{\pi w_q} \sqrt{1 + 4\alpha_q^2 I_R^2 \frac{w_q^4}{w_R^4}} \approx |\alpha_q| I_R \frac{\lambda_q w_q}{\pi w_R^2}, \quad (6)$$

where I_R is the peak IR intensity, w_R , w_q are the radii of the IR and $q^{\rm th}$ harmonic fields and λ_q the $q^{\rm th}$ harmonic wavelength. $\alpha_q I_R$ is the single-atom phase, corresponding to the phase accumulated by the electron on its trajectory, often called "dipole phase". When $\alpha_q I_R$ is large, it dominates the diffraction limit in Eq. (6) and the divergence takes the simple expression shown on the right side in Eq. (6). For the short trajectory, we have $|\alpha_q|\approx 2.7\times 10^{-14}~{\rm cm}^2/{\rm W}$ for the $23^{\rm rd}$ harmonic [14, 16].

As shown in Eq.(2), the addition of a weak blue field affects the phase of each half-cycle contribution by $\pm \sigma$. The divergence of the q^{th} harmonic is then expected to vary between $\Theta_q(1 \pm \sigma/|\alpha_q|I_R)$, the limits being reached when one half-cycle is dominant. These limits are indicated by the grey lines in Fig. 4 (c,d), calculated by using the experimentally determined one-color divergence

 $\Theta_q=0.33$ mrad. The two lines (solid and dashed) show the variation of the divergence for two (positive or negative) half cycles. Our experimental results for the 22nd and the $23^{\rm rd}$ harmonics are indicated by the red symbols. As expected, the measured divergence angles are comprised between the theoretical values for two consecutive half-cycle contributions. The variation of the measured divergence can be interpreted as follows: In (c), one half-cycle (corresponding to the dashed line) is dominant from $\tau = 03T_B$ to $0.7T_B$, while the other half-cycle prevails for the other delays. In contrast in (d), no half cycle dominates on the other, resulting in divergences well within the theoretical half-cycle limits. In fact, the experimental data in (d) clearly shows how dominance is shifted from one half-cycle towards the other, confirming the interpretation of (c).

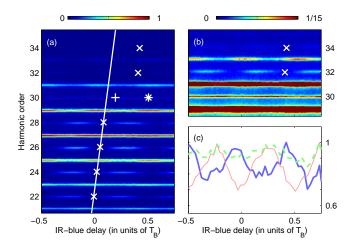


FIG. 5: (a) Harmonic spectra as a function of delay. (b) High energy region using a saturated color scale. The white crosses indicate the position of the nodes of the oscillations obtained by Fourier transform analysis. (c) $30^{\rm th}$ harmonic intensity as a function of delay, spatially integrated (green dashed), integrated over the wings of the profile (thin red line) and over the central area (thick blue line). The + and * symbols refer to the nodes of the thick and thin lines in (c).

Finally, we investigate how the interference pattern depends on Ω , *i.e.* harmonic order, from the plateau to the cutoff region. Fig. 5 shows the harmonic spectra as a function of delay, in the weak blue intensity case [corresponding to Fig. 1(a)]. The phases of the oscillations of the even harmonics are indicated by the white crosses. In the plateau spectral region [Fig. 5(a)], the phase increases approximately linearly with harmonic frequency, with a slope that is approximately equal to the derivative of $t_r(\Omega)$ according to

$$\frac{\partial}{\partial\Omega}\left(\frac{t_r}{T}\right) \approx \frac{\partial}{\partial\Omega}\left(\frac{\delta}{2\pi T_B}\right). \tag{7}$$

We find a good agreement with the prediction for HHG in Ar from the short trajectory [18]. In Fig. 5 (b), we exam-

ine the behaviour of higher-order harmonics, approaching the cutoff region. Surprisingly, the 30th harmonic hardly oscillates, while the 32nd and 34th oscillate almost out of phase with the 28th. To understand the apparent lack of oscillation of the 30th harmonic, we analyse its spatial profile. In Fig. 5 (c), we present the 30th harmonic intensity obtained by integrating over the outer (central) part of the spatial profile, plotted as a thick (thin) line. This allows us to unravel two different oscillations almost opposite in phase. The phase obtained by integrating the wings of the spatial profile is close to that obtained for the 32^{nd} and 34^{th} harmonics in Fig. 5 (b). We interpret this result as due to the long trajectory which becomes dominant when approaching the cutoff region. The switch between the two trajectories occurs at the 30th harmonic in our experiment. This harmonic has comparable (and approximately out of phase) contributions from the two trajectories and it, therefore, only weakly oscillates over τ . Phase matching calculations performed using our experimental conditions show a switch from the short trajectory to the long trajectory when approaching the cutoff region and thus confirm this interpretation.

In summary, we have experimentally identified and theoretically analyzed interference effects in two-color HHG. Adding a weak blue field allows us to control the intensity and divergence of the harmonic emission. An interesting switch between the short and long trajectories of the harmonic emission has been identified when approaching the cutoff region. This seems to be a general feature of harmonic generation in optimized phase matched conditions.

This research was supported by the Marie Curie Incoming International Fellowship OHIO, the European Research Council (ALMA), the Knut and Alice Wallenberg Foundation, the Joint Research Programme ALADIN of Laserlab-Europe II and the Swedish Research Council.

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